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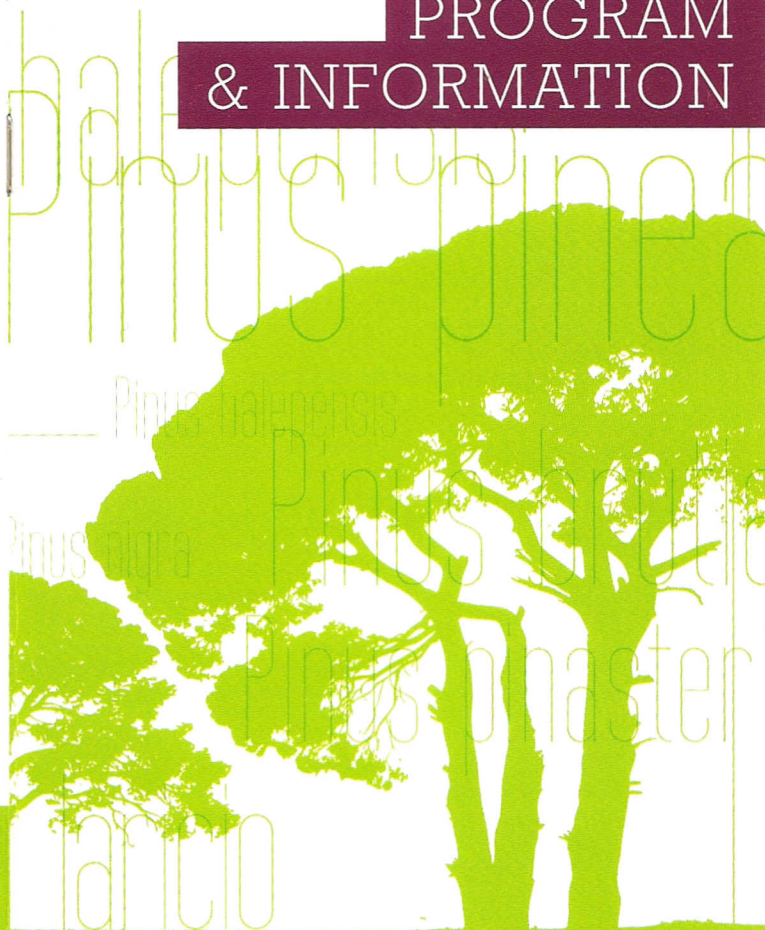
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# Prediction of annual tree growth and survival for thinned and unthinned even-aged maritime pine stands in Portugal from data with different time measurement intervals

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## 1. INTRODUCTION

The Portuguese national forest strategy (Direcção Geral dos Recursos Florestais, 2006) proposed a specialization of the Portuguese forest territory according to three main functions: wood production, multifunctional systems and protected areas. Wood production is mostly related with pure even-aged stands of two species, the maritime pine (*Pinus pinaster*, Ait.) and the blue gum (*Eucalyptus globulus* Labill.). Sustainable forest management of these productive areas requires adequate prediction of wood stocks and growth. An annual individual tree survival and growth model is presented for pure even-aged stands of maritime pine in Portugal, using data with irregularly spaced measurement intervals and considering thinning effects. The model is distance-independent and assuming variable rates of growth and survival.

**A PROBLEM** Available data sets for fitting individual tree models frequently have measurement intervals greater than 1 year and many times these intervals are irregularly spaced. Also thinning can occur between measurements. This causes difficulty when modelling annual tree growth and survival.

## 2. MATERIAL AND METHODS

### Data from thinning experiments

- ▶ 145 growth series
- ▶ Irregularly time-spaced measurements
- ▶ 40367 observations for diameter growth
- ▶ 20520 observations for height growth

### Modelling approach

**Logistic regression:**  
 $p_i = (1 + \exp(d_i \cdot X_i \cdot \rho))^{-1}$  - (annual survival probability of the *i*th tree)  
 $p_{i,j} = \prod_{t=1}^j p_{i,t}$  - (survival probability for the period of duration *j*)

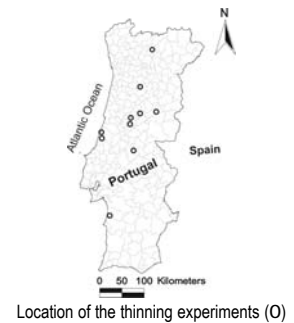
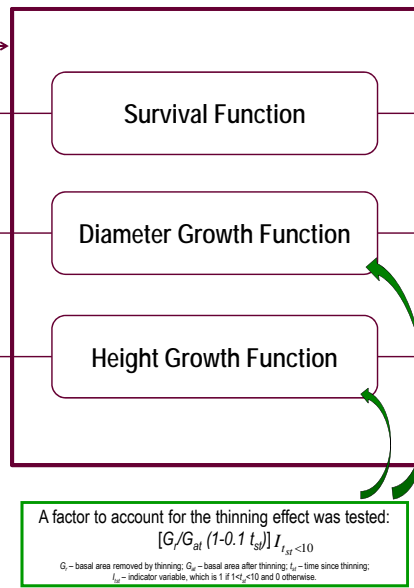
**Cao (2000) methodology:**  
 Models structured as a series of equations from the start to the end of the growth period of duration *j*. Two modelling approaches were tested:

1. Modelling future value of *y* using difference equations:  
 $-y_{1j} = f(y_{0j}, t_j, X_{0j}, \beta) + \epsilon_{1j}$   
 - if  $I_{1j} = 1$ , then  $y_{2j} = f(y_{1j}, t_j, X_{1j}, \beta) + \epsilon_{2j}$ , else  $y_{2j} = y_{1j}$ ,  
 ...  
 - if  $I_{1j} = 1$ , then  $y_{5j} = f(y_{4j}, t_j, X_{4j}, \beta) + \epsilon_{5j}$ , else  $y_{5j} = y_{4j}$ ,  
 $-y_{5j} = y_{4j} + \eta_{5j}$

2. Modelling increment of *y* using Zeide (1993) differential equations:  
 $- \Delta y_{1j} = f(y_{0j}, t_j, X_{0j}, \beta) + \epsilon_{1j}$   
 $y_{1j} = y_{0j} + \Delta y_{1j}$   
 $- \Delta y_{2j} = f(y_{1j}, t_j, X_{1j}, \beta) + \epsilon_{2j}$   
 $y_{2j} = y_{1j} + \Delta y_{2j}$   
 ...  
 $- \Delta y_{5j} = f(y_{4j}, t_j, X_{4j}, \beta) + \epsilon_{5j}$   
 $y_{5j} = y_{4j} + \Delta y_{5j}$   
 $-y_{5j} = y_{0j} + \sum_{t=1}^5 \Delta y_{tj} + \eta_{5j}$

*y<sub>i</sub>* - diameter or height of *i*th tree in the period *f* (*i* - age; *X* - stand variables (competition, site, ...); *β* - model parameters;  $\epsilon_i$  and  $\eta_i$  - random error;  $I_{1j}$  - indicator variables (*i*-1) for the growth period.

### Individual tree growth and survival model



### Parameter estimation

Simultaneous fit in SAS/ETS PROC MODEL (SAS Institute Inc., 2008), with the SUR (seemingly unrelated regression) method. An algorithm was used to continuously update stand-related explanatory variables. A fixed cutoff was used to convert survival probability in a living or dead tree.

Independent fit in SAS/ETS PROC MODEL (SAS Institute Inc., 2008), using non linear generalized least squares and the updated stand variables.

## 3. RESULTS

Selected equations (Modelling approach 2 performed slightly better)

The survival probability function:  
 $p_i = (1 + \exp(-9.267 - 0.204 di + 0.066 G + 0.077 G_{>d}))^{-1}$

The diameter growth function:  
 $\Delta d_j = \exp(1.296 + 0.204 \ln(d_{0j}) + m \ln(t_j))$   
 where,  
 $m = -0.903 + 0.101 d/d_0 + 0.006 h/d_0 - 0.007 G_{>d} + 0.145 (G/G_{at})(1 - 0.1 t_{st}) I_{t_{st} < 1.0}$

The height growth function:  
 $\Delta h_j = \exp(1.275 + 0.274 \ln(h_{0j}) + m \ln(t_j))$   
 where,  
 $m = -1.490 + 0.207 d/h + 0.022 h/d_0 + 0.093 G_{>d}/G$

*d<sub>i</sub>* - diameter (cm); *h<sub>i</sub>* - height (m); *G* - stand basal area (m<sup>2</sup> ha<sup>-1</sup>); *G<sub>>d</sub>* - basal area of trees larger than the subject tree (m<sup>2</sup> ha<sup>-1</sup>); *t<sub>j</sub>* - stand age; *d<sub>0j</sub>* - quadratic mean diameter (cm); *h<sub>0j</sub>* - dominant height (m); *m* - parameter related to the decline component, being a power function of age.

## 4. DISCUSSION

In the selected equations, tree survival and growth are predicted using tree attributes, stand variables reflecting the competition levels and also variables related to the site. The parameters present logical signs which is important for biological realism.

The area under the receiving operating characteristic curve (ROC) for the survival probability function was 0.94, indicating a very good discrimination capacity between the categories live and dead.

The variable that was tested, accounting for the thinning intensity and the duration of its effect, was significant to explain diameter growth. However no evidence of significant effect was found for the height growth. The diameter and height growth functions presented a promising performance as evaluated using PRESS residuals.

The obtained results in the evaluation of the individual tree growth and survival model recommend the use of this model for practical applications.

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