

# Allometric equations for predicting mineralomass in high-forest chestnut stands in Portugal

M.S. Patrício<sup>1,a</sup> and M. Tomé<sup>2</sup>

<sup>1</sup>Departamento de Ambiente e Recursos Naturais, Instituto Politécnico de Bragança, ESA-CIMO. Campus de Stª Apolónia, 5300-253 Bragança, Portugal; <sup>2</sup>Centro de Estudos Florestais, Instituto Superior de Agronomia, Universidade de Lisboa, Tapada da Ajuda, 1349-017 Lisboa, Portugal.

## Abstract

The assessment of nutrients in biomass tree-components is a time-consuming and expensive process, often involving tree felling, not always possible or desirable. Thus, mineralomass prediction equations are an important tool for the quantification of the nutrients exported in management and harvesting activities towards its replacement and sustainable management, as well as to evaluate the effect of other disturbances in the balance of ecosystems. Thus, given the importance of the relationship of biomass and nutrients (mineralomass) for dynamic and sustainable management of chestnut woodlands, above-ground mineralomass was studied in sweet chestnut (*Castanea sativa* Mill.) high-forest stands located in northern Portugal. Nutrient-specific prediction equations that allow estimating the mineralomass (N, P, K, Ca, Mg, S, B and C) stocked in the trees above the ground, considering the tree as a whole (stem + bark + branches + leaves + flowers) and separately for each tree component: stem-wood, stem-bark, branches, leaves and flowers, based on tree dendrometric variables, DBH (diameter breast height) and total height, were developed. Linear and non-linear regression estimation methods were used. Data analysis was based on information collected in destructive analysis of 34 felled trees, distributed by the existing diameter classes (10-65 cm) in three adult chestnut stands. Several linear and nonlinear equations were fitted by the least squares method to select models. A simultaneous fit by SUR method using iterative seemingly unrelated regression (ITSUR) was used for the final selected models. The best-fitting models are presented.

**Keywords:** *Castanea sativa* Mill., allometric models, above-ground tree mineralomass, silviculture, forest management

## INTRODUCTION

Land-use management, as forest tending and harvesting, can have a strong impact on nutrient cycling and ecosystem sustainability. The knowledge of the distribution of nutrients in the different sections making up the above-ground biomass is of great importance for making realistic predictions about the export of nutrients under different forest management systems (Augusto et al., 2000). The information of the content of mineral elements in the tree-component biomass is essential to understand their status and flow in the whole system, as well as to assess the productive capacity of ecosystems and management implications for forest sustainability. However, the evaluation of biomass and nutrients in tree-components is a time-consuming and expensive process, often involving tree felling, not always possible or desirable. Moreover, laboratory analyses are costly and time-consuming.

Nowadays, the use of allometric equations for the prediction of tree biomass is quite common. These equations, when available for a given species, allow the estimation of total biomass or tree-component biomass using dendrometric variables easier to measure, such as diameter at breast height (DBH) and total height. One of the methods to estimate the

<sup>a</sup>E-mail: sampat@ipb.pt



quantity of a mineral in the biomass (mineralomass) is to multiply the estimated biomass by these allometric equations by the concentration of the respective mineral element obtained through laboratory analysis. However, the concentration of minerals in tree-biomass components for a given species varies considerably between sites and it is not always available in the literature. So, it is essential to provide tools to estimate directly the amount of minerals stored on the tree-component biomass because the concentration of the minerals in itself does not present an acceptable functional relationship with dendrometric variables of the tree.

Thus, given the importance of the relationship of biomass and nutrients for dynamic and sustainable management of chestnut woodlands, above-ground mineralomass was studied in sweet chestnut (*Castanea sativa* Mill.) high-forest stands located in northern Portugal. The aim of this study is to provide allometric equations for chestnut high-forest woodlands for estimating the mineralomass using the dendrometric variables DBH and total height ( $h$ ) of the tree. These nutrient-specific prediction equations will allow estimating the mineralomass (N, P, K, Ca, Mg, S, B and C) stocked in the trees above the ground, considering the tree as a whole (stem + bark + branches + leaves + flowers) and separately for each tree component: stem-wood, stem-bark, branches, leaves and flowers, based on tree dendrometric variables (DBH,  $h$ ) to be applied to the sustainable management of sweet chestnut high-forest stands..

## **MATERIALS AND METHODS**

### **General characteristics of the sites**

This study was based on biomass information collected in the three mature chestnut high-forest stands located in three mountains of northern Portugal: Bornes (41°29'42"N, 6°55'12"W and 800 m a.s.l.), Marão (41°14'46"N, 7°55'04"W and 900 m a.s.l.) and Padrela (41°31'47"N, 7°35'22"W and 850 m a.s.l.) which have been monitored over time. Sampling followed a west-to-east transect across to northern Portugal from a more-Atlantic-to-less-maritime influence. General characteristics of these sites can be found in Patrício et al. (2009, 2012, 2014).

### **Field data**

In order to obtain biomass data, 34 trees were felled according to the existent diameter classes. The methodology of biomass collection was described in Patrício et al. (2005). These samples of tree-biomass components were analyzed to determine their mineral concentrations.

### **Treatment of the samples in laboratory**

The collected biomass samples of leaves, flowers and barks were dried in a stove at  $70\pm 2^\circ\text{C}$ , while the log samples and branches, were dried at  $103\pm 2^\circ\text{C}$  (until constant weight) for determining the water content and estimating the dry matter. After the drying process the biomass samples were finely ground. Sub-samples of these were taken for later chemical analysis. Subsamples of biomass tree-components were subjected to wet digestion with sulphuric acid (Houba et al., 1986) subsequently followed by colorimetric method measurements of N and P concentration using a segmented flow autoanalyzer (SanPlus, Skalar, Breda, The Netherlands). For the K, Ca, Mg and S determinations, samples were digested with nitric-perchloric acid (Mills and Jones, 1996) and B by dry ash (Miller, 1998). Ca and Mg were determined by atomic absorption spectrophotometry (AAS 3100, Perkin-Elmer, USA), K by flame photometry (flame photometer PFP7, Jenway, UK) and S by the turbidimetric method (Coutinho, 1996). Total organic C was determined with a PRIMAC-SC carbon analyzer (Skalar, Breda, The Netherlands). Residual ash was determined by incineration at  $450^\circ\text{C}$  for 6 h in a muffle furnace.

Dataset used in mineralomass modelling was characterized in Table 1 and biometric variables of 34 sampled trees in Table 2.

Table 1. Mean value and respective standard deviation (in brackets) of the mineralomass ( $n=34$  trees) for the minerals considered in the analysis.

Mineral	M_Wood (kg)	M_Bark (kg)	M_Bliv (kg)	M_Ltot (kg)	M_Tot (kg)
N	0.489 (0.572)	0.203 (0.155)	0.379 (0.476)	0.225 (0.199)	1.451 (1.489)
P	0.047 (0.062)	0.017 (0.015)	0.048 (0.062)	0.015 (0.011)	0.140 (0.151)
K	0.105 (0.161)	0.085 (0.085)	0.201 (0.205)	0.074 (0.065)	0.500 (0.427)
Ca	0.307 (0.414)	0.594 (0.436)	0.394 (0.389)	0.036 (0.028)	1.448 (1.143)
Mg	0.107 (0.114)	0.065 (0.047)	0.129 (0.166)	0.037 (0.030)	0.379 (0.379)
S	0.059 (0.081)	0.008 (0.008)	0.016 (0.019)	0.010 (0.008)	0.097 (0.106)
B <sup>1</sup>	0.977 (1.966)	0.461 (0.360)	0.904 (1.084)	0.116 (0.100)	2.703 (2.623)
C	226.714 (179.350)	26.034 (18.832)	73.731 (92.717)	5.289 (4.446)	354.902 (310.320)

<sup>1</sup>Mineralomass of B in g; M\_Wood, mineralomass of main stem under bark; M\_Bark, mineralomass of stem bark; M\_Bliv, mineralomass of living branches; M\_Ltot, mineralomass of leaves and flowers; M\_Tot, the total above-ground mineralomass.

Table 2. Biometric variables of the 34 sampled trees.

Variable <sup>1</sup>	Minimum	Mean	Maximum	Stand. deviation
DBH (cm)	10.25	33.98	64.20	14.14
$h$ (m)	11.55	21.91	30.40	4.63

<sup>1</sup>DBH, diameter breast height;  $h$ , total height.

### Data analysis

To model the mineralomass ( $M$ ) by tree-components, the following candidate allometric equations were tested, where  $d$  represent the DBH and  $h$  the total height of the tree:

- (1)  $M = \beta_0 + \beta_1 d^2 h$
- (1.1)  $M = \beta_1 d^2 h$
- (2)  $M = \beta_0 + \beta_1 d + \beta_2 d^2$
- (2.2)  $M = \beta_1 d + \beta_2 d^2$
- (3)  $M = \beta_1 d^2$
- (4)  $M = \beta_1 d + \beta_2 h$
- (5)  $M = \beta_1 (d^2 h)^{\beta_2}$
- (6)  $M = \beta_1 d^{\beta_2}$

Other equations, namely that used to fit biomass equations for chestnut high-forest (Patrício et al., 2005) were tested but they were eliminated because no significant parameters were found.

The same data used to develop biomass equations for sweet chestnut (Patrício et al., 2005) were on the base of this study. Thus, the following mineralomass of tree components: bark (M\_Bark), leaves and flowers (M\_Ltot), living branches (M\_Bliv), main stem under bark (M\_Wood), main stem over bark (M\_Stem) and the total above-ground mineralomass (M\_Tot), were considered for analytical purposes.

The mineralomass equations were fitted by the ordinary least squares method (OLS) associated with both the PROC REG (linear models) and PROC NLIN (non-linear models)

procedures of SAS/STAT. The modified Gauss-Newton iterative method was applied in the non-linear model fitting.

To consider the logical constraint between the sum of the predicted mineralomass for tree components and the prediction for the total tree, a system of additive equations was used. A system of additive equations provides more accurate biomass (mineralomass) estimates than the common approach of separately fitting total tree and component biomass (mineralomass) equations using log transformed data through least squares regression (Bi et al., 2004). A simultaneous fit by SUR method using iterative seemingly unrelated regression (ITSUR) by PROC MODEL procedure of SAS/STAT was used for the final selected models.

The models were evaluated in terms of measures of fit and prediction ability: modelling efficiency (EM), mean square error (MSE), models parameter significance,  $R^2$  of prediction ( $R^2_{pred}$ ), mean of PRESS residuals (m\_PRESS), and mean of the absolute values of the PRESS residuals (ma\_PRESS) as well as the percentiles 95% (P95) and 5% (P5) of the PRESS residuals. The normality of the studentized residuals was analyzed using normal QQplots. The presence of heteroscedasticity associated with the error term of the models was checked by plotting the studentized residuals against the predicted values.

The regression assumptions departure was solved with non-linear iteratively reweighted least squares (IRWLS) using the Huber function with the maximum value of  $r=1$  and weighting factors. The procedure was repeated for each mineral.

## RESULTS AND DISCUSSION

The models 1 to 6 were fitted to the mineralomass data as described in the methodology. Given the high number of equations tested, we only present the selected equations with all significant parameters, after weighting. Table 3 presents fitting, precision and bias statistics for the selected models. The plot analysis of the studentized residuals was also taken into consideration in model selection.

The analysis accomplished, based on the criteria previously mentioned, led to the selection of the following equations for each tree component (Table 4).

The final models were simultaneously fitted by SUR method with the ITSUR procedure. Next, we present the final models for each mineral (Table 5). We also present the modeling efficiency (EM) of the equations, a measure similar to the adjusted  $R^2$  in linear models. The EM obtained by SUR method is generally lower than that obtained by OLS, but with a smaller standard error of the coefficients and with the guarantee of the additivity of the mineralomass of the tree components to obtain the total mineralomass of the tree.

These equations predicted the mineralomass of the tree components in kg, based on the diameter at 1.30 m ( $d$ ), with bark, except for the wood, in cm and the total height ( $h$ ) in m. The mineralomass of boron is estimated in g.

Table 3. Fitting and prediction statistics of the models with the best performance for the mineralomass by tree component and by mineral, after weighing.

Min.	Model	Comp.	MSE	EM	mPRESS	maPRESS	R <sup>2</sup> <sub>pred</sub>	P95	P5
N	(1.1)	M_Bark	0.507 10 <sup>-7</sup>	0.957	-0.003	0.033	0.862	0.065	-0.101
	(3)	M_Ltot	0.718 10 <sup>-5</sup>	0.837	0.007	0.076	0.715	0.264	-0.163
	(3)	M_Bliv	0.2357 10 <sup>-4</sup>	0.767	0.043	0.181	0.477	0.832	-0.260
	(3)	M_Wood	0.284 10 <sup>-4</sup>	0.830	0.054	0.180	0.417	0.530	-0.286
	(3)	M_Stem	0.257 10 <sup>-3</sup>	0.944	0.096	0.611	0.803	2.853	-1.168
	(1.1)	M_Tot	0.536 10 <sup>-5</sup>	0.900	0.083	0.431	0.720	1.929	-0.829
P	(3)	M_Bark	0.216 10 <sup>-7</sup>	0.895	0.522 10 <sup>-3</sup>	0.005	0.632	0.016	-0.010
	(3)	M_Ltot	0.372 10 <sup>-7</sup>	0.831	0.665 10 <sup>-3</sup>	0.005	0.672	0.015	-0.008
	(3)	M_Bliv	0.608 10 <sup>-7</sup>	0.660	0.006	0.027	0.309	0.102	-0.040
	(3)	M_Wood	0.825 10 <sup>-6</sup>	0.600	0.004	0.036	0.174	0.133	-0.097
	(3)	M_Stem	0.466 10 <sup>-5</sup>	0.882	0.004	0.081	0.634	0.211	-0.193
	(3)	M_Tot	0.005	0.803	0.008	0.066	0.509	0.327	-0.145
K	(1.1)	M_Bark	0.350 10 <sup>-7</sup>	0.822	0.005	0.031	0.578	0.099	-0.049
	(3)	M_Ltot	0.144 10 <sup>-5</sup>	0.763	0.004	0.033	0.633	0.081	-0.056
	(3)	M_Bliv	0.786 10 <sup>-5</sup>	0.752	0.016	0.096	0.524	0.274	-0.135
	(1.1)	M_Wood	0.156 10 <sup>-3</sup>	0.428	0.025	0.078	0.088	0.192	-0.143
	(1.1)	M_Stem	0.002	0.868	0.034	0.393	0.618	1.034	-0.753
	(3)	M_Tot	0.036	0.925	0.023	0.171	0.719	0.398	-0.274
Ca	(3)	M_Bark	0.392 10 <sup>-4</sup>	0.852	-0.009	0.224	0.242	0.580	-0.629
	(3)	M_Ltot	0.337 10 <sup>-6</sup>	0.749	0.002	0.016	0.451	0.049	-0.021
	(3)	M_Bliv	0.359 10 <sup>-4</sup>	0.707	0.027	0.198	0.401	0.631	-0.492
	(1.1)	M_Wood	0.352 10 <sup>-3</sup>	0.773	0.023	0.148	0.538	0.673	-0.258
	(1.1)	M_Stem	0.088	0.891	0.119	2.260	0.498	5.256	-6.362
	(1)	M_Tot	0.414 10 <sup>-5</sup>	0.882	0.020	0.286	0.870	0.687	-0.565
Mg	(3)	M_Bark	0.752 10 <sup>-6</sup>	0.779	0.408 10 <sup>-3</sup>	0.024	0.357	0.064	-0.048
	(3)	M_Ltot	0.229 10 <sup>-6</sup>	0.822	0.002	0.014	0.719	0.040	-0.022
	(3)	M_Bliv	0.283 10 <sup>-5</sup>	0.759	0.016	0.059	0.465	0.232	-0.083
	(1.1)	M_Wood	0.229 10 <sup>-4</sup>	0.874	0.006	0.037	0.681	0.151	-0.071
	(3)	M_Stem	0.001	0.893	0.025	0.243	0.637	0.845	-0.540
	(1)	M_Tot	0.479 10 <sup>-6</sup>	0.818	0.023	0.125	0.642	0.326	-0.203
S	(1.1)	M_Bark	0.321 10 <sup>-9</sup>	0.835	0.128 10 <sup>-4</sup>	0.003	0.510	0.010	-0.009
	(3)	M_Ltot	0.155 10 <sup>-7</sup>	0.852	0.143 10 <sup>-3</sup>	0.003	0.692	0.009	-0.009
	(3)	M_Bliv	0.351 10 <sup>-7</sup>	0.797	0.001	0.007	0.619	0.036	-0.010
	(1.1)	M_Wood	0.260 10 <sup>-4</sup>	0.616	0.008	0.036	0.314	0.183	0.054
	(1.1)	M_Stem	0.956 10 <sup>-4</sup>	0.775	0.008	0.074	0.461	0.239	-0.126
	(1.1)	M_Tot	0.397 10 <sup>-7</sup>	0.827	0.008	0.034	0.631	0.159	-0.060
B <sup>1</sup>	(3)	M_Bark	0.119 10 <sup>-4</sup>	0.915	0.004	0.129	0.780	0.273	-0.292
	(3)	M_Ltot	0.491 10 <sup>-5</sup>	0.684	0.001	0.055	0.507	0.236	-0.090
	(3)	M_Bliv	0.125 10 <sup>-3</sup>	0.786	0.088	0.397	0.562	1.154	-0.513
	(3)	M_Wood	0.150 10 <sup>-3</sup>	0.806	0.011	0.407	0.576	0.997	-1.191
	(3)	M_Stem	0.168 10 <sup>-3</sup>	0.927	0.083	1.475	0.822	4.063	-3.473
	(1.1)	M_Tot	0.237 10 <sup>-4</sup>	0.915	-0.006	0.831	0.819	2.335	-2.487
C	(5)	M_Bark	0.437 10 <sup>-3</sup>	0.963	0.071	3.074	0.950	8.348	-7.686
	(3)	M_Ltot	0.004	0.838	0.152	1.976	0.712	5.862	-3.541
	(3)	M_Bliv	0.887	0.757	8.031	35.97	0.560	188.41	-52.166
	(5)	M_Wood	0.012	0.978	-1.141	26.027	0.933	64.273	-40.100
	(5)	M_Stem	0.090	0.982	-3.611	52.653	0.946	156.17	-103.88
	(6)	M_Tot	0.860	0.984	-0.942	34.370	0.972	66.810	-107.67

<sup>1</sup>Mineralomass of B in g; Mineralomass of the remaining minerals in kg. MSE, mean square error; EM, modelling efficiency; m\_PRESS, mean of PRESS residuals; ma\_PRESS, mean of the absolute values of the PRESS residuals; R<sup>2</sup><sub>pred</sub>, R<sup>2</sup> of prediction; P95 and P5, percentiles 95% and 5% of the PRESS residuals.

Table 4. Equation for each mineral (nitrogen, phosphorus, potassium, calcium, magnesium, sulfur, boron, carbon), subdivided by tree component.

<b>Nitrogen</b>	<b>Phosphorus</b>	<b>Potassium</b>
N_Bark = 0.6260 10 <sup>-5</sup> d <sup>2</sup> h	P_Bark = 0.1250 10 <sup>-4</sup> d <sup>2</sup>	K_Bark = 0.2400 10 <sup>-5</sup> d <sup>2</sup> h
N_Ltot = 0.1768 10 <sup>-3</sup> d <sup>2</sup>	P_Ltot = 0.1230 10 <sup>-4</sup> d <sup>2</sup>	K_Ltot = 0.6220 10 <sup>-4</sup> d <sup>2</sup>
N_Bliv = 0.2505 10 <sup>-3</sup> d <sup>2</sup>	P_Bliv = 0.3070 10 <sup>-4</sup> d <sup>2</sup>	K_Bliv = 0.1370 10 <sup>-3</sup> d <sup>2</sup>
N_Wood = 0.3232 10 <sup>-3</sup> d <sup>2</sup>	P_Wood = 0.3217 10 <sup>-4</sup> d <sup>2</sup>	K_Wood = 0.2430 10 <sup>-5</sup> d <sup>2</sup> h
N_Stem = 0.00193 d <sup>2</sup>	P_Stem = 0.1713 10 <sup>-3</sup> d <sup>2</sup>	K_Stem = 0.3036 10 <sup>-4</sup> d <sup>2</sup> h
N_Tot = 0.4138 10 <sup>-4</sup> d <sup>2</sup> h	P_Total = 0.1030 10 <sup>-3</sup> d <sup>2</sup>	K_Total = 0.4060 10 <sup>-3</sup> d <sup>2</sup>
<b>Calcium</b>	<b>Magnesium</b>	<b>Sulfur</b>
Ca_Bark = 0.4152 10 <sup>-3</sup> d <sup>2</sup>	Mg_Bark = 0.4750 10 <sup>-4</sup> d <sup>2</sup>	S_Bark = 0.2466 10 <sup>-6</sup> d <sup>2</sup> h
Ca_Ltot = 0.2824 10 <sup>-4</sup> d <sup>2</sup>	Mg_Ltot = 0.2991 10 <sup>-4</sup> d <sup>2</sup>	S_Ltot = 0.7520 10 <sup>-5</sup> d <sup>2</sup>
Ca_Bliv = 0.2671 10 <sup>-3</sup> d <sup>2</sup>	Mg_Bliv = 0.8383 10 <sup>-4</sup> d <sup>2</sup>	S_Bliv = 0.1063 10 <sup>-4</sup> d <sup>2</sup>
Ca_Wood = 0.8670 10 <sup>-5</sup> d <sup>2</sup> h	Mg_Wood = 0.3080 10 <sup>-5</sup> d <sup>2</sup> h	S_Wood = 0.1550 10 <sup>-5</sup> d <sup>2</sup> h
Ca_Stem = 0.2041 10 <sup>-3</sup> d <sup>2</sup> h	Mg_Stem = 0.2325 10 <sup>-4</sup> d <sup>2</sup> h	S_Stem = 0.4420 10 <sup>-5</sup> d <sup>2</sup> h
Ca_Total = 0.1062+0.3777 10 <sup>-4</sup> d <sup>2</sup> h	Mg_Total = 0.0336+0.9950 10 <sup>-5</sup> d <sup>2</sup> h	S_Total = 0.2580 10 <sup>-5</sup> d <sup>2</sup> h
<b>Boron</b>	<b>Carbon</b>	
B_Bark = 0.3386 10 <sup>-3</sup> d <sup>2</sup>	C_Bark = 0.0076 (d <sup>2</sup> h) <sup>0.7880</sup>	
B_Ltot = 0.9340 10 <sup>-4</sup> d <sup>2</sup>	C_Ltot = 0.0045 d <sup>2</sup>	
B_Bliv = 0.6070 10 <sup>-3</sup> d <sup>2</sup>	C_Bliv = 0.0490 d <sup>2</sup>	
B_Wood = 0.7160 10 <sup>-3</sup> d <sup>2</sup>	C_Wood = 0.0138 (d <sup>2</sup> h) <sup>0.9360</sup>	
B_Stem = 0.00438 d <sup>2</sup>	C_Stem = 0.0342 (d <sup>2</sup> h) <sup>0.9299</sup>	
B_Total = 0.9437 10 <sup>-4</sup> d <sup>2</sup> h	C_Total = 0.0630 d <sup>2.3754</sup>	

\_Bark, equation for stem bark; \_Ltot, equation for leaves and flowers; \_Bliv, equation for living branches; \_Wood, equation for main stem under bark; \_Stem, equation for main stem over bark; \_Total, equation for total above-ground.

Table 5. Final equation model and modeling efficiency (EM) for each mineral (nitrogen, phosphorus, potassium, calcium, magnesium, sulfur, boron, carbon).

<b>Mineral</b>	<b>Equation</b>	<b>EM</b>	<b>Mineral</b>	<b>Equation</b>	<b>EM</b>
Nitrogen	N_Bark = 0.5877 10 <sup>-5</sup> d <sup>2</sup> h	0.8871	Magnesium	Mg_Bark = 0.4300 10 <sup>-4</sup> d <sup>2</sup>	0.4369
	N_Ltot = 0.1700 10 <sup>-3</sup> d <sup>2</sup>	0.7266		Mg_Ltot = 0.3000 10 <sup>-4</sup> d <sup>2</sup>	0.7398
	N_Bliv = 0.2930 10 <sup>-3</sup> d <sup>2</sup>	0.5437		Mg_Bliv = 0.9700 10 <sup>-4</sup> d <sup>2</sup>	0.5323
	N_Wood = 0.3660 10 <sup>-3</sup> d <sup>2</sup>	0.4609		Mg_Wood = 0.3100 10 <sup>-5</sup> d <sup>2</sup> h	0.7125
	N_Total	0.7209		Mg_Total	0.7246
Phosphorus	P_Bark = 0.1400 10 <sup>-4</sup> d <sup>2</sup>	0.6318	Sulfur	S_Bark = 0.2441 10 <sup>-6</sup> d <sup>2</sup> h	0.5537
	P_Ltot = 0.1200 10 <sup>-4</sup> d <sup>2</sup>	0.6954		S_Ltot = 0.7388 10 <sup>-5</sup> d <sup>2</sup>	0.7147
	P_Bliv = 0.3400 10 <sup>-4</sup> d <sup>2</sup>	0.3639		S_Bliv = 0.1100 10 <sup>-4</sup> d <sup>2</sup>	0.6622
	P_Wood = 0.3800 10 <sup>-4</sup> d <sup>2</sup>	0.2128		S_Wood = 0.1872 10 <sup>-5</sup> d <sup>2</sup> h	0.3827
	P_Total	0.4951		S_Total	0.5925
Potassium	K_Bark = 0.2812 10 <sup>-5</sup> d <sup>2</sup> h	0.5853	Boron	B_Bark = 0.3330 10 <sup>-3</sup> d <sup>2</sup>	0.8000
	K_Ltot = 0.6600 10 <sup>-4</sup> d <sup>2</sup>	0.6634		B_Ltot = 0.9200 10 <sup>-4</sup> d <sup>2</sup>	0.5354
	K_Bliv = 0.1480 10 <sup>-3</sup> d <sup>2</sup>	0.5638		B_Bliv = 0.655 10 <sup>-3</sup> d <sup>2</sup>	0.6128
	K_Wood = 0.7100 10 <sup>-4</sup> d <sup>2</sup>	0.0932		B_Wood = 0.7940 10 <sup>-3</sup> d <sup>2</sup>	0.6011
	K_Total	0.7427		B_Total	0.7830
Calcium	Ca_Bark = 0.4730 10 <sup>-3</sup> d <sup>2</sup>	0.2546	Carbon	C_Bark = 0.010008 (d <sup>2</sup> h) <sup>0.760258</sup>	0.9491
	Ca_Ltot = 0.2600 10 <sup>-4</sup> d <sup>2</sup>	0.4772		C_Ltot = 0.004172 d <sup>2</sup>	0.7175
	Ca_Bliv = 0.2491 10 <sup>-3</sup> d <sup>2</sup>	0.4221		C_Bliv = 0.041554 d <sup>2</sup>	0.5124
	Ca_Wood = 0.8796 10 <sup>-5</sup> d <sup>2</sup> h	0.5882		C_Wood = 0.010784 (d <sup>2</sup> h) <sup>0.960756</sup>	0.9314
	Ca_Total	0.7998		C_Total	0.9103

\_Bark, equation for stem bark; \_Ltot, equation for leaves and flowers; \_Bliv, equation for living branches; \_Wood, equation for main stem under bark; \_Total, equation for total above-ground.

## CONCLUSIONS

At the end of this study two types of mineralomass equations for high-forest chestnut management were provided: 48 total tree and tree component equations, separately fitted, and 8 systems of additive mineralomass equations, both for N, P, K, Ca, Mg, S, B and C. This kind of equations is very useful for forestry management purposes. These mineralomass equations, applicable to data of individual trees of forest inventories, are useful for assessing the impact of a wide variety of ecological problems on ecosystems, like forest fires, carbon sequestration, harvesting effects and forestry management on nutrient balance and site sustainability.

## ACKNOWLEDGEMENTS

This work was supported by the AGRO Program, Project 267: Sustainable Management of Chestnut Woodlands in High-forest and Coppice Systems.

## Literature cited

- Augusto, L., Ranger, J., Ponette, Q., and Rapp, M. (2000). Relationships between forest tree species, stand production and stand nutrient amount. *Ann. For. Sci.* 57 (4), 313–324 <https://doi.org/10.1051/forest:2000122>.
- Bi, H., Turner, J., and Lambert, M.J. (2004). Additive biomass equations for native eucalypt forest trees of temperate Australia. *Trees (Berl.)* 18 (4), 467–479 <https://doi.org/10.1007/s00468-004-0333-z>.
- Coutinho, J. (1996). Automated method for sulphate determination in soil-plant extracts and waters. *Com. Soil Sci. Plant Anal.* 27 (3-4), 727–740 <https://doi.org/10.1080/00103629609369590>.
- Houba, V.J.G., Van Der Lee, J.J., Novozamski, I., and Walinga, I. (1986). *Soil and Plant Analysis Procedures* (Wageningen: Wageningen University), pp.262.
- Miller, R.O. (1998). High-temperature oxidation: dry ashing. In *Handbook and Reference Methods for Plant Analysis*, Y.P. Kalra, ed. (Boca Raton, Florida: CRC Press), p.53–56.
- Mills, H.A., and Jones, J.B., Jr. (1996). *Plant Analysis Handbook II* (Athens, Georgia, USA: MicroMacro Publishing, Inc.), pp.422.
- Patrício, M.S., Monteiro, M.L., and Tomé, M. (2005). Biomass equations for *Castanea sativa* high-forest in the Northwest of Portugal. *Acta Hort.* 693, 727–732 <https://doi.org/10.17660/ActaHortic.2005.693.98>.
- Patrício, M.S., Pereira, E., Nunes, L.F., and Monteiro, M.L. (2009). Carbon and nutrient inputs by litterfall into three chestnut high forest stands in northern Portugal. *Acta Hort.* 815, 69–74 <https://doi.org/10.17660/ActaHortic.2009.815.9>.
- Patrício, M.S., Nunes, L.F., and Pereira, E.L. (2012). Litterfall and litter decomposition in chestnut high forest stands in northern Portugal. *For. Syst.* 21 (2), 259–271 <https://doi.org/10.5424/fs/2012212-02711>.
- Patrício, M.S., Nunes, L.F., and Pereira, E.L. (2014). Evaluation of soil organic carbon storage in a sustainable forest chestnut context. *Acta Hort.* 1043, 161–165 <https://doi.org/10.17660/ActaHortic.2014.1043.21>.

