



Development and evaluation of a robot trilateration localization system using four beacons

Stefany Yumie Kawashima - 54156

Dissertação apresentada à Escola Superior de Tecnologia e de Gestão de Bragança para obtenção do Grau de Mestre em Engenharia Industrial - Electrotécnica.

Trabalho orientado por:

Prof. M.Sc. José Luís Sousa de Magalhães Lima

Prof. M.Sc. Marcos Banheti Rabello Vallim

Esta dissertação não inclui as críticas e sugestões feitas pelo Júri.

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Dedicatória

Dedico este trabalho ao meu pai que ficaria muito orgulhoso de saber que sua filha se tornou engenheira.

Agradecimentos

Agradeço primeiramente à Deus. Agradeço ao meu pai e minha mãe por todo o investimento e dedicação nesses últimos 27 anos. Agradeço todos os meus professores desde o primeiro dia na escola. Agradeço a Universidade Tecnológica Federal do Paraná e ao Instituto Politécnico de Bragança por esta oportunidade incrível. Agradeço ao professor José Luis e ao Arezki e João que estiveram a puxar por mim e me auxiliar ao decorrer de todo o trabalho. Agradeço ao meu noivo por me cobrar para que eu terminasse e todo o apoio que ele me deu. Por último e não menos importante, agradeço a mim mesma por não desistir.

Resumo

KAWASHIMA, S. Y. Esta dissertação tem como objetivo investigar a localização de robôs móveis em um ambiente de *software* virtual (Simtwo) usando quatro beacons e um sensor LiDAR. A localização de robôs desempenha um papel crucial em várias indústrias e aplicações, como robótica, automação e navegação. Uma localização precisa é vital para que os robôs móveis possam navegar e desempenhar tarefas de forma eficaz. Para alcançar a localização, beacons artificiais são usados como pontos de referência. Para fazer isso, um método comumente usado é a trilateração, que requer pelo menos três beacons para serem reconhecidos simultaneamente, juntamente com a distância entre elas e o robô. Usando essa técnica e um algoritmo de identificação de beacons, este trabalho calculará a posição global estimada e erros associados de um robô em uma simulação virtual da *Robot Factory* no Simtwo.

Palavras-chave: Robôs móveis, LiDAR, Trilateração, Localização de Robôs

Abstract

KAWASHIMA, S. Y. This dissertation aims to investigate the localization of robots in a virtual software environment (Simtwo) using four beacons and a LiDAR sensor. The localization of robots plays a crucial role in various industries and applications, such as robotics, automation, and navigation. Accurate localization is vital for mobile robots to navigate and perform tasks effectively. In order to achieve localization, artificial beacons are used as reference points. In order to do that, one commonly used method is trilateration, which requires at least three beacons to be recognized simultaneously along with the distance between them and the robot. Using this technique and a beacon identification algorithm, this work will calculate an estimated global position and respective errors of the robot in a virtual simulation of Robot Factory on Simtwo.

Keywords: Mobile robots, LiDAR, Trilateration, Robot Localization

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Acronyms

AGV Automated Guided Vehicle. 17

IPB Instituto Politécnico de Bragança. iii

LiDAR Light Detection And Ranging. 3

SLAM Simultaneous Localization and Mapping. 9

UTFPR Universidade Tecnológica Federal do Paraná. iii

Chapter 1

Introduction

Since the creation of the first mobile robot in 1968, called *Shakey* (shown in Figure 1.1), the number of this type of robot is increasing [15].



Figure 1.1: Picture of the first mobile robot, known as *Shakey* [5].

Mobile robots are gaining more visibility in applications in robotics. These applications have a wide range, since industrial robots [15], even robots for missions in other planets [9], remote areas or difficult access locations like underwater regions [16] and high radioactivity [12]. In each one of these applications areas mentioned, the robot requires autonomy and mobility. In order to do its tasks, it needs to move inside any type of environment. This

environment is known as Robotics Navigation [12].

The Robotics Navigation deals with three main questions: where the robot is, where should it go and how it should move to reach its destination. In order to do that, robots may be produced in a way to recognize the environment and the reference points to do its tasks.

Besides that, the robots should know how to deal with obstacles to reach their destination safely. To do that, while its navigate, the robots uses sensors to estimate its position and orientation on the environment that it is. However, the use of these sensors may be have measurement errors and uncertainties [2].

1.1 Context

The problem of localization is a fundamental key to the autonomy of mobile robots. If a robot doesn't know where it is, determining its next actions can be challenging. In order to determine its location, a robot has access to relative and absolute measurements of its position, providing feedback to its system about its movement actions and the situation of the environment it is in. Given this information, the robot needs to determine its location with the highest possible accuracy. What makes this task difficult is the presence of uncertainties both in its movement and in the robot's sensor measurements. The information embedded in these uncertainties needs to be optimally combined [12].

Accurate localization is vital for mobile robots to navigate and perform tasks effectively. In order to achieve localization, beacons can be used as reference points. However, the number of beacons that can be placed in the environment is limited. This limitation has led researchers to develop localization algorithms that work with specific beacon placements and numbers. One commonly used method is trilateration, which requires at least three beacons to be recognized simultaneously along with the distance between them and the robot. This method allows the robot to calculate its precise position based on the intersection of the spheres created by the distances from the beacons.[17]

In this work, the SimTwo software will be employed to perform the localization of a

robot using a Light Detection And Ranging (LiDAR) sensor. Four beacons will be used to estimate the location using the trilateration technique within a factory environment.

1.2 Objectives

1.2.1 General Objective

Presenting the SimTwo software and its essential features, elucidating the Localization challenge through the application of trilateration methodology, and formulating an algorithm for the precise positioning of a robot with the aid of four beacons.

1.2.2 Specific Objectives

- To introduce the SimTwo tool and its primary functionalities.
- To present the issue of localization in mobile robots.
- To implement a localization technique (trilateration) for pinpointing the robot's position within the SimTwo software and computing associated errors.

1.3 Document Structure

This work is divided in seven chapters, described below.

- Chapter 1: Introduction. This chapter will present a brief general introduction to the work, showing the objectives and the work proposal.
- Chapter 2: State of Art. Concepts related to mobile robots will be reviewed, presenting a brief history, as well as general characteristics. Instances of the localization problem will be addressed, showing examples of where uncertainties are applied in the robotic context. This chapter also will present Simtwo and the trilateration methodology used to solve the localization problem.

- Chapter 3: Development. This chapter will show the algorithm used in SimTwo platform.
- Chapter 4: Results Obtained and Analysis of Results. In this chapter the results obtained will be shown and compared to the ground truth to calculate its errors.
- Chapter 5: Conclusion. Finally, the results obtained will be compared with the existing literature on the subject, discussing the difficulties and proposals for future work.

Chapter 2

State of Art

This chapter will provide a brief theoretical foundation regarding mobile robots, instances of localization problems and trilateration techniques.

2.1 Mobile robots

Navigating purposefully is a fundamental ability to most animals and every intelligent organism. A mobile robot must have this ability in order to do its tasks considering the environment, obstacles and the objectives like space robots as shown in the Figure 2.1 [12].

Mobile robotics is a specialized area of research focused on the control of self-driving and partially autonomous vehicles. What distinguishes mobile robotics from other research domains, like traditional manipulator robotics, artificial intelligence, and computer vision, is its primary focus on addressing challenges related to comprehending extensive spatial environments, surpassing the confines of what can be perceived from a single viewpoint [6].

To behave in large-scale not only needs to deal with incremental acquisition of knowledge, the estimated error, the recognition of important objects or places, and real-time responses, but it also requires the full integration of these functionalities [6].

The word *autonomous* have its roots in the Greek for "self-willed". The term "robot"



Figure 2.1: Mars Exploration Rover-a semi-autonomous exploration robot from NASA [11].

was introduced by Karel Čapek in 1923 and its derived from the Czech word "robota" that means "labour" and "robotinik", meaning "workman" [6].

2.1.1 Mobile Robot kinematics

Kinematics represents the fundamental examination of mechanical system behavior. In the field of mobile robotics, comprehending the mechanical characteristics of a robot is crucial, serving a dual purpose: aiding in the design of well-suited mobile robots for specific tasks and facilitating the development of control software tailored to a particular mobile robot hardware configuration [15].

Robot position

It is going to be considered the robot as a rigid body on wheels, operating on a horizontal plane as shown in the Figure 2.2 [15].

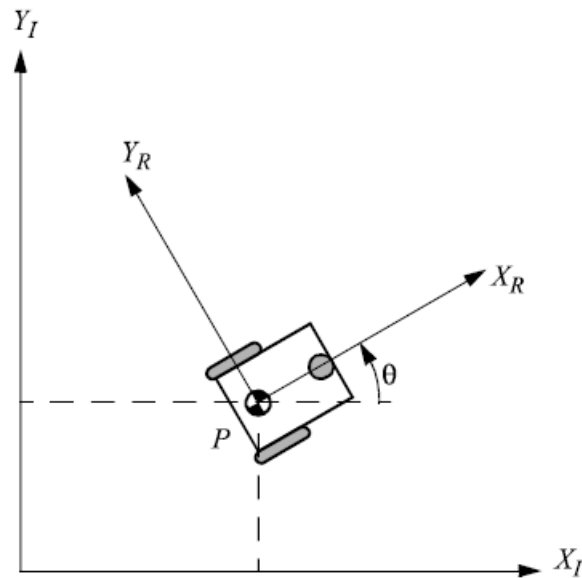


Figure 2.2: The global reference frame and the robot local reference frame [15]

To find the global position of the robot on the plane, it is going to be established the relationship between the global frame I and the robot frame R. To specify the robot position it is going to be set a point named P on the robot chassis and as the reference frame R of the robot. The position P represents the global position of the robot x and y , and the angular difference θ between frames I and R. The pose of the robot is described as:

$$\zeta = [x, y, \theta]^T \quad (2.1)$$

To describe movement, it is needed to map motion along the axes of the global reference frame to motion along the axes of the robot's reference frame. That could be done using

the orthogonal rotation matrix:

$$R(\theta) = \begin{bmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2.2)$$

This matrix can be used to map motion in the global reference frame X_I, Y_I in terms of motion of the robot's reference frame X_R, Y_R .

$$\dot{\zeta}_R = R(\theta)\dot{\zeta}_I \quad (2.3)$$

2.2 Localization problem

The challenge of robot localization revolves around answering the essential question: 'Where is the robot positioned?'. In other words, it involves the robot's ability to determine its precise coordinates, including the x and y positions and its orientation within a global reference system. The importance of localization plays a critical role in the functionality of numerous autonomous robot systems. Without a clear understanding of its own location, a robot faces significant obstacles in making decisions and executing tasks effectively. It is considered one of the most fundamental problems to provide robots with truly autonomous capabilities [12].

To enable a robot to move from one point to another, it needs to know its position and orientation (pose) at any given point in time [13]. Therefore, precise localization is a fundamental requirement when dealing with mobile robot control problems. According to [8], there are two types of localization: relative and absolute. The former is provided through sensors that measure variables related to the robot's internal dynamics. For example, incremental encoders with optical sensors are placed on the wheels or the steering axis of the vehicle. At each sampling instant, the position is estimated based on the encoder increment over a period with multiple samples.

One drawback of this method is that errors accumulate with each measurement, leading to issues of inaccuracy and imprecision in the estimated position and orientation, especially on sinuous trajectories [18].

In the case of absolute position, it is determined by a set of sensors that measure parameters of the environment in which the vehicle is operating. Typically, sonars fixed to the vehicle are used to measure distances while respecting obstacles encountered in the known environment. One of the significant challenges in using sonars is their dependency on environmental characteristics, meaning that potential changes in the scenario's parameters can lead to misinterpretations in measurements by the localization algorithm [10].

2.2.1 Problem instances

The localization have some problem instances. In the context of position tracking, the robot possesses knowledge of its initial location, and the main objective of localization is to continuously monitor and update the robot's position as it moves through its environment. This specific challenge is typically addressed using techniques known as *tracking* or *local methods* [12].

Another problem is the *wake – up* robot or *global positioning* problem. It is more difficult because the robot does not know its initial position. Methods to solve this type of problem are called *global* techniques.

One harder problem is the *kidnapped robot problem*. The robot does not know where it is because it was moved to another location without the robot being aware of this. The issue is for the robot it is to know that was kidnapped and to find the new location coordinates.

The technique used for these localization problems is known as Simultaneous Localization and Mapping (Simultaneous Localization and Mapping), which deals with simultaneous localization and mapping through four main actions: mapping, perception, localization, and modeling [14].

2.3 Trilateration

One of the solutions to the localization problem is using the trilateration method. Trilateration is a technique to determine the position of an object based on simultaneous range measurements from three stations located at known sites as shown in the figure 2.3. This is a common operation not only in robot localization, but also in other areas [17].

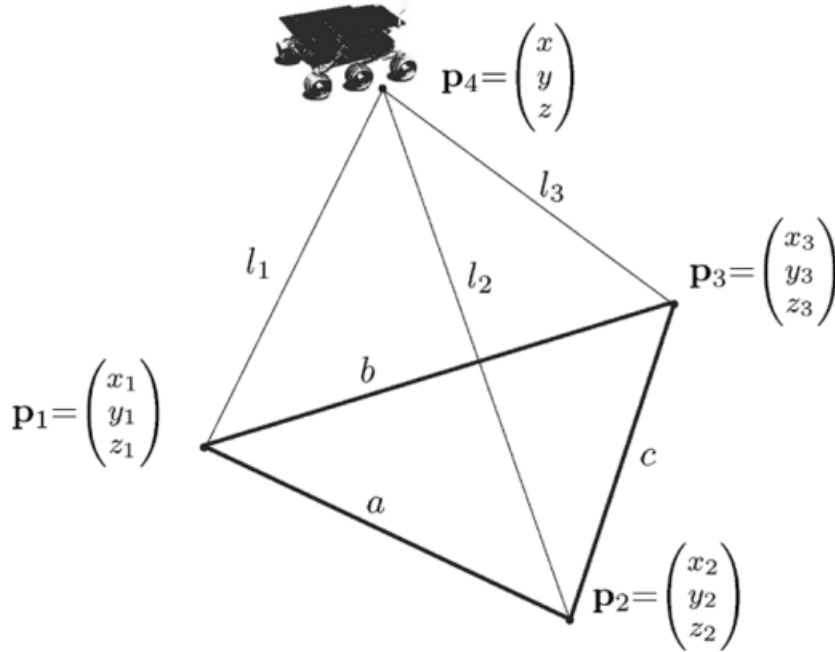


Figure 2.3: Representation of a trilateration technique applied to a robot [17]

It can be expressed as the problem of finding the intersection of three spheres, that is, finding the solutions to the following system of quadratic equations:

$$l_1^2 = (x_1 - x)^2 + (y_1 - y)^2 + (z_1 - z)^2 \quad (2.4)$$

$$l_2^2 = (x_2 - x)^2 + (y_2 - y)^2 + (z_2 - z)^2 \quad (2.5)$$

$$l_3^2 = (x_3 - x)^2 + (y_3 - y)^2 + (z_3 - z)^2 \quad (2.6)$$

Where $p_i = (x_i, y_i, z_i)$ are the coordinates of the known station i and l_i is the distance measured between the robot and the station. Considering a 2D plane, the equations can

be represented as:

$$l_1^2 = (x_1 - x)^2 + (y_1 - y)^2 \quad (2.7)$$

$$l_2^2 = (x_2 - x)^2 + (y_2 - y)^2 \quad (2.8)$$

$$l_3^2 = (x_3 - x)^2 + (y_3 - y)^2 \quad (2.9)$$

For i known stations:

$$l_i^2 = (x_i - x)^2 + (y_i - y)^2 \quad (2.10)$$

These equations are going to be developed in the next chapter.

2.4 SimTwo environment

SimTwo is a realistic simulator that allows the implementation and simulation of various types of robots in a realistic environment. It supports the following types of robots [3]:

1. Wheeled Mobile Robots:

- Differential drive
- Robots with omnidirectional wheels
- Manipulators

2. Legged Mobile Robots:

- Bipedal robots
- Quadrupeds
- Hexapods

3. Lighter than Air Vehicles:

- These are likely airships or balloons with propellers for propulsion.

4. Underwater Vehicles:

- These are likely underwater drones or submersibles with thrusters for propulsion.

5. Custom Robots:

- SimTwo allows the creation of custom robots that consist of rigid bodies connected by hinge or prismatic joints, which can be optionally actuated by electric motors. These custom robots may use classical wheels, omnidirectional wheels, or propellers for movement.

The drive and motor system can include the following components:

- **DC Motor:** The system may consist of a DC motor, optionally equipped with a gearbox and a controller.
- **Controllers:** Several types of controllers can be used in SimTwo:
 - A PID controller applied to position or velocity signals.
 - A state feedback controller.
- **DC Motor Model:** The DC motor model within SimTwo accounts for various nonlinear elements, including voltage saturation, current limitation, and Coulomb friction.

By simulating robots in a realistic environment and modeling them as systems of rigid bodies with various joint types, SimTwo provides a valuable tool for researchers, engineers, and robotics enthusiasts to test and refine their robot designs and control algorithms without the need for physical prototypes. This can save time and resources in the development and testing of robotic systems. SimTwo offers a comprehensive set of drive and control systems for simulating various robots.

In addition to the low-level control system, SimTwo provides the flexibility to feed reference signals to these controllers from a higher-level controller implemented by the user. This higher-level controller can be implemented using the following methods:

- A scripting language, which is editable and compilable within SimTwo.
- A remote program that communicates via UDP packets or over the serial port.

This modular approach to drive and control systems enables users to fine-tune and customize the behavior of their robots within the SimTwo simulator, making it a powerful tool for robotic development and testing.

2.4.1 Simtwo overview

When opened, Simtwo have several windows [7], explained below .

- Scene visual: The real time 3D visualization of the robot shown in Figure 2.4.

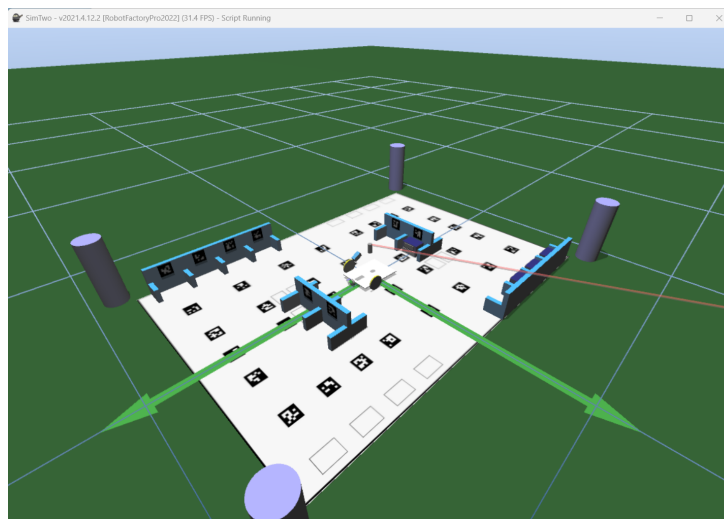


Figure 2.4: Scene Window

- Scene editor: It is the XML editor. The scene tab contains information on the scene. The track tab defines the track, including sensors. It is possible to add obstacles. The AGV tab contains the robot's editor (Figure 2.5).

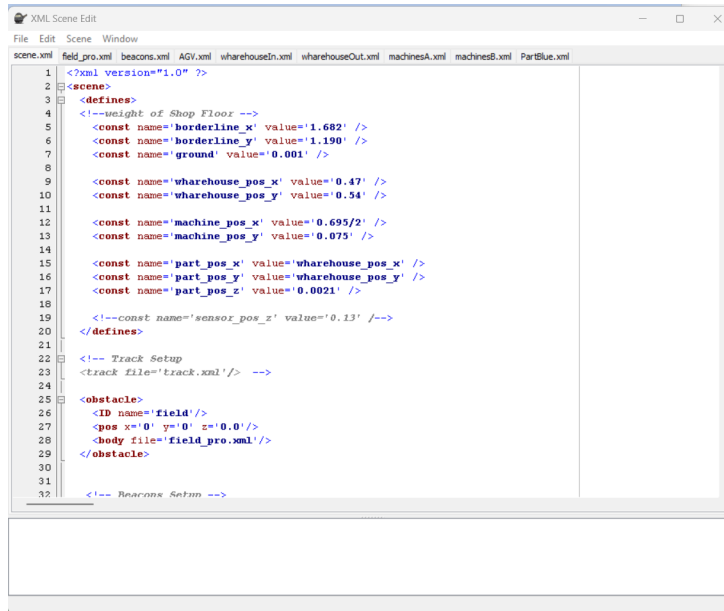


Figure 2.5: XML editor Window

- Control editor: It is the Pascal editor (Figure 2.6) to control procedure defined for the robot (speed, logic, for example).

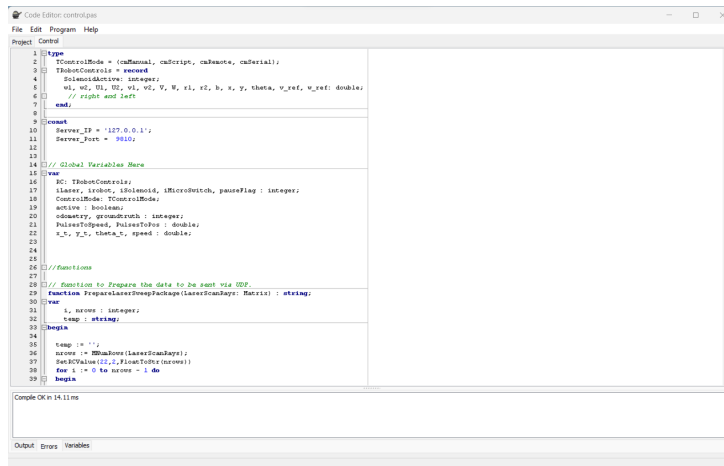


Figure 2.6: Editor Window

- Config: It is used to control the camera and scene as well as simulation speed and debugging (Figure 2.7).
- Chart: It is used to plot simulation variables (Figure 2.8).

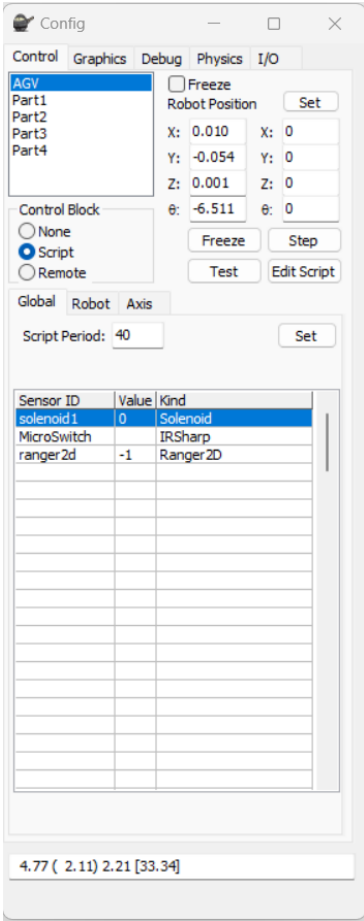


Figure 2.7: Config Window

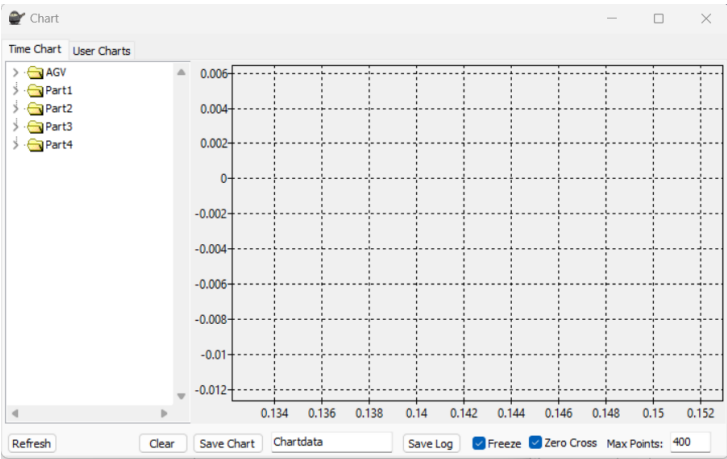


Figure 2.8: Chart Window

- Sheets: Displays real time values and it is possible to set buttons (Figure 2.9).

The screenshot shows a window titled 'Sheets' with a table of real-time data. The table has 14 columns and 31 rows. The data is as follows:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
1	1							REF		Real			Odometry	-0.004
2	Control	Manual	Manual	Remote				w1	2	w1		1.797143	Real Pos	-0.009
3								w2	2	w2		1.079605		
4	Sensors	RR	State	8	Set	0								
5			V	0	Set	1								
6			W	0										
7														
8			Vrobot	0.01										
9														
10														
11			Robot	Part1	Part2	Part3	Part4							
12	X		-0.725	-0.725	-0.575	-0.425	-0.275							
13	Y		-0.4	0.595	0.595	0.595	0.595							
14	Theta		180	0	0	0	0							
15				Type	Type	Type	Type							
16														
17														
18														
19														
20														
21														
22			360 0000											
23														
24														
25														
26														
27														
28														
29														
30														
31														
32														

Figure 2.9: Sheets Window

Chapter 3

Development

In this work it was used the SimTwo Robot Factory 2022 shown in Figure 3.1 that simulates a factory plant. In this scene, a differential Automated Guided Vehicle (AGV) robot is inserted in the plant. The AGV have the LiDAR sensor that can returns the distance between an object, for example a beacon, and the angle between its frame reference (robot's frame) and the beacon's angle. The Figure 3.1 is the Scene of the work's simulation environment in SimTwo.

In this work, in order to simplify the problem, it is going to be considered the following system shown in Figure 3.2:

The main objective is to locate the robot's global position using these four beacons. Basicly, the algorithm has 6 phases: initialization, data acquisition from the LiDAR, average distances and angles among robot and beacons, the θ value, the beacon identification and finally, the estimated robot position and respective errors. This chapter will show the core of the work, explaining the code.

3.1 Initialization

As a first step is necessary to set some variables. The initial position of the robot, according to Equation (2.1) is set as $\zeta_{initial} = [0, 0, rad(0)]^T$.

Simtwo have some control modes but in this work the manual mode is used.

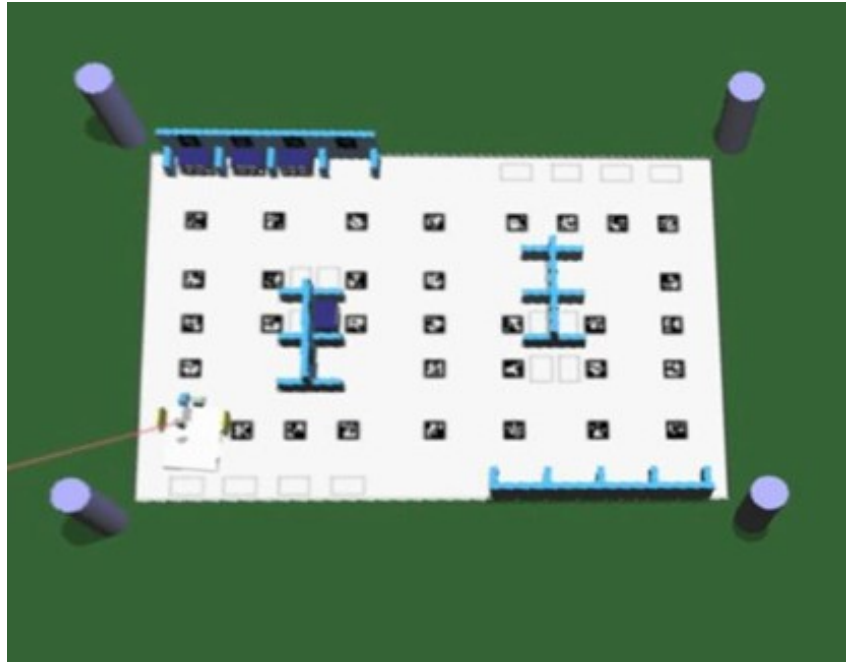


Figure 3.1: Robot Factory

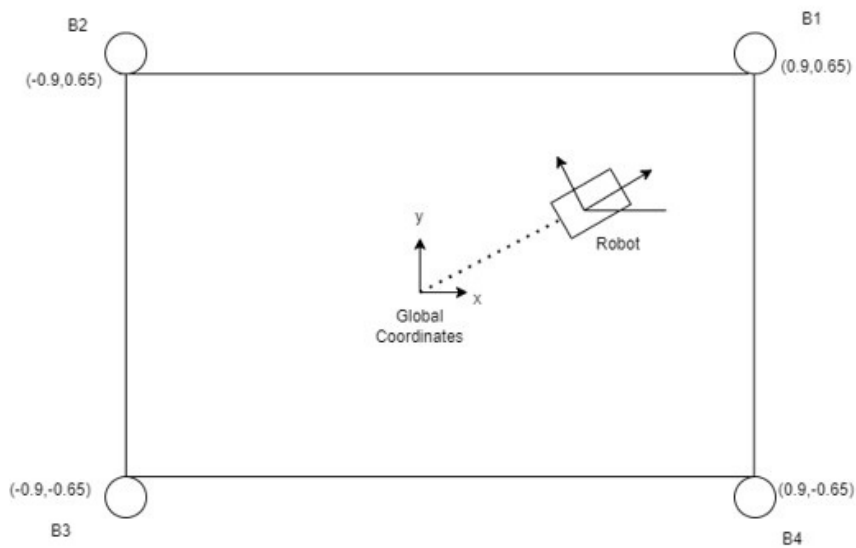


Figure 3.2: Representation of the system

```

1   procedure Initialize;
2 begin
3   irobot := GetRobotIndex('AGV');

```

```

4   iSolenoid := GetSensorIndex(irobot, 'solenoid1');
5   iLaser := GetSensorIndex(irobot, 'ranger2d');
6   iMicroSwitch := GetSensorIndex(irobot, 'MicroSwitch');
7   SetRobotPos(irobot, 0, 0, 0.001, rad(0));
8   RC.x := GetRobotPos2D(irobot).x;
9   RC.y := GetRobotPos2D(irobot).y;
10  RC.theta := GetRobotPos2D(irobot).angle;
11  active := True;
12  RC.r1 := 0.06884/2;
13  RC.r2 := 0.06884/2;
14  RC.b := 0.186;
15  pauseFlag := 0;
16  odometry := 0;
17  PulsesToSpeed := 2 * pi / (3840*0.04);
18  PulsesToPos := 2 * pi / (3840);
19  groundtruth := 0;
20  ControlMode := cmManual;
21      active := False;
22      SetMotorControllerState(irobot, 0, false);
23      SetMotorControllerState(irobot, 1, false);
24 end;

```

In this procedure, the robot is defined as 'AGV' that is the XML file, the sensors are defined and the procedure "SetRobotPos()" defines the initial position of the robot and other constants are set.

3.2 LIDAR measurements

The YDLiDAR x4 LIDAR (Figure 3.3) sensor performs 360 measurements each cycle counterclockwise, corresponding to 360 degrees. It has a range frequency of 5 kHz, a range distance between 0.12 m to 10 m and an angle resolution of 0.43° to 0.86° . Considering that the model dimensions are (1,68m x 1,18m), this LiDAR is applicable. If an object or obstacle is detected, the LiDAR returns the distance and angle value, if there is no detection, a value of -1 is returned [1].

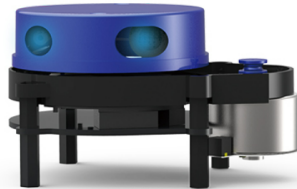


Figure 3.3: YDLiDAR X4 [1]

In the XML file the LiDAR has been previously set considering its datasheet and in the code, two arrays distance and angle were created, which store the values of distance and i (angle), respectively.

```
1   for i:= 1 to (length(distance)-1) do
2       begin
3           distance[i-1]:= Mgetv(LaserScanRays, i, 0);
4           angle[i-1]:=i;
5           j:=j+1;
6       end;
```

3.3 Average distances and angles

The main idea is to identify certain points with measurements and beginnings and ends of each beacon found. From the LIDAR readings, the points corresponding to each beacon found will be added in order to find the average distance and angle value for each beacon. The table 3.1 below shows an example of when a beacon is found.

Table 3.1: Example of beacon found

Angle	1	2	3	4	5	6
LiDAR Measurement	-1	0.1	0.12	0.11	0.1	-1

One of the problems encountered during the development of the code was the existence of a "fifth beacon" as shown in table 3.2. This occurs in the scenario where the robot starts measurements in the middle of a beacon and ends up having more measurements associated with it.

Table 3.2: Example of a middle of a beacon found

Angle	1	2	3	4	...	358	359	360
LiDAR Measurement	0.2	0.2	0.23	-1	...	-1	0.2	0.2

The developed code checks each beacon start situation:

1. When the previous value, i_{previous} , is negative and the current value, i_{current} , is positive, it indicates the beginning of a beacon, and the count of beacons found must be increased.
2. If the first reading is a positive number, there are two possible scenarios:
 - (a) Measurements started at the beginning of a beacon.
 - (b) Measurements started in the middle of a beacon.

If the second scenario occurs, at the end, the LiDAR will have found 5 beacons. In this case, it is going to be added the measurements of this fifth beacon to the first one and set the count of beacons found as 4.

3. If the LiDAR starts reading in the middle of a beacon (when both the current and previous distances are positive), the code must sum the distances until it identifies a situation where the current distance is positive, and the next one is negative.
4. After that, it is calculated the average distances for each beacon found.

The code is shown above:

```
1 for i:=1 to (length(distance)) do
2     begin
3
4         if (((distance[i-1])<0) and ((distance[i])>0)) or
5             ((distance[0])> 0) and (i =1)) then
6
7             begin
8
9                 bf:=bf+1;
10                if (i = 1) and (distance[0]> 0) then begin
11                    sumdistance [bf-1]:=sumdistance [bf-1]+distance
12                        [0];
13                    sumangle [bf-1]:=sumangle [bf-1]+angle [0];
14                    numberofpoints [bf-1]:=numberofpoints [bf-1]+1;
15                end;
16
17                sumangle [bf-1]:=sumangle [bf-1]+angle [i];
18                sumdistance [bf-1]:=sumdistance [bf-1]+distance [i
19                    ];
```

```

20     else if (((distance[i-1]) > 0) and ((distance[i])
21             > 0)) then
22     begin
23         sumdistance[bf-1]:=sumdistance[bf-1]+distance[i
24             ];
25         sumangle[bf-1]:=sumangle[bf-1]+angle[i];
26         numberofpoints[bf-1]:=numberofpoints[bf-1]+1;
27     end
28
29 end;
30
31
32 if (bf=5) then
33 begin
34
35     sumdistance[0]:=sumdistance[0]+ sumdistance[4];
36     sumangle[0]:=sumangle[0]+ sumangle[4] - 360*
37         numberofpoints[4];
38     numberofpoints[0]:=numberofpoints[0]+ numberofpoints
39         [4];
40     bf := 4;
41 end;

```

3.4 θ value

The aim is to determine the current value of θ . The initial value of θ is known, and when a rotation of γ degrees occurs, it can be expressed as follows:

$$\theta_{\text{current}} = \theta_{\text{previous}} + \gamma \quad (3.1)$$

However, the value of γ is not known; instead, the angle between the robot frame and the beacon is known. In this scenario, γ can be determined as the difference between the previous ϕ and the current ϕ :

$$\gamma = \phi_{\text{previous}} - \phi_{\text{current}} \quad (3.2)$$

By substituting these values, the following equation can be established:

$$\theta_{\text{current}} = \theta_{\text{previous}} + \phi_{\text{previous}} - \phi_{\text{current}} \quad (3.3)$$

In the first iteration, the current ϕ is computed as the average of the beacon angles. The previous ϕ is set to be equal to the current ϕ , especially in the first iteration, and the previous θ is based on a measurement provided by the software as shown in the code below.

```
1 begin
2 for m := 0 to 3 do
3   begin
4     average[m] := ((sumdistance[m]) / numberofpoints[m]) + rb
5     ;
6     averageangle[m] := (sumangle[m]) / numberofpoints[m];
7     actual_phi[m] := averageangle[m]
8   if (gama = 1) then
9     begin
10      previous_phi[m] := actual_phi[m];
```

```

10     previous_theta := (180 * GetRobotTheta(GetRobotIndex('
        AGV')))) / pi;
11     gama := 0;
12     end;
13 end;
14 for n := 0 to 3 do
15     begin
16         if actual_phi[n] <> previous_phi[n] then
17             begin
18                 actual_theta := previous_theta + previous_phi[0] -
                    actual_phi[0];
19                 previous_phi[n] := actual_phi[n];
20                 previous_theta := actual_theta;
21             end;
22 end;

```

First the code sum the distances and angles of each beacon and finds its average to each beacon and defines the current ϕ as the value of the average angle. There is one first time exception that is to set the values of previous ϕ as the current ϕ and the previous θ as the initial θ of the robot, that is got by the procedure `GetRobotTheta()`.

After that, if the current ϕ is different from the previous one, then the value is calculated as shown before.

3.5 Beacon identification

Considering the general transformation of a vector shown in Figure 3.4.

The general equation for translation and rotation is defined as [4]:

$${}^A P = {}_B^A R^B P + {}^A P_{BORG} \quad (3.4)$$

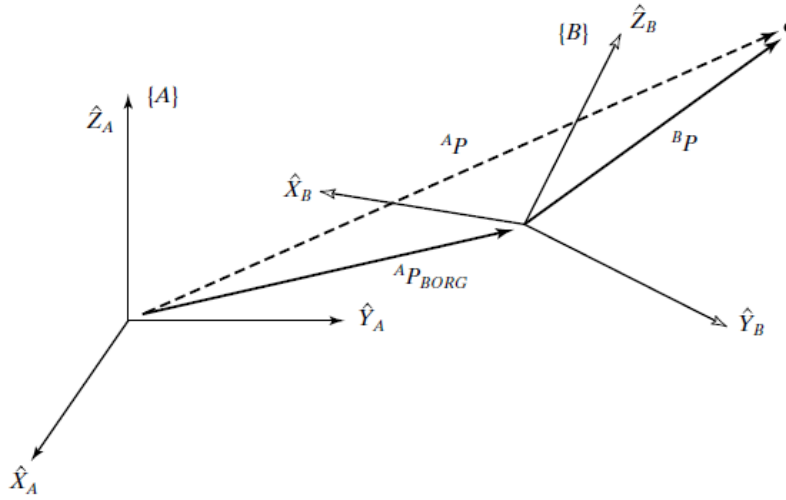


Figure 3.4: General transformation of a vector [4]

Where ${}^A P$ is the position of P regarding to frame A, ${}^A_B R$ is the Rotation Matrix in z axis, ${}^B P$ is the position of P regarding to frame B and ${}^A P_{BORG}$ is the position of the origin of frame B regarding frame A. When applied to the problem context, it is given this equation:

$${}^G_B P = {}^G_R R_B^R P + {}^R P_{ROORG} \quad (3.5)$$

Where ${}^G_B P$ is the global position of the beacon, ${}^G_R R$ is the rotation matrix in z axis, ${}^R_B P$ is the position of the beacon regarding the robot's position and ${}^R P_{ROORG}$ is the global position of the robot. In other words:

$$\begin{bmatrix} X_{bfn}^G \\ Y_{bfn}^G \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} X_{bfn}^R \\ Y_{bfn}^R \end{bmatrix} + \begin{bmatrix} X_{RG} \\ Y_{RG} \end{bmatrix} \quad (3.6)$$

Where X_{bfn}^G and Y_{bfn}^G are the coordinates of Beacon found n regarding the global frame, X_{bfn}^R and Y_{bfn}^R are the coordinates of the beacon found n regarding the robot's frame and X_{RG} and Y_{RG} are the global coordinates of the robot. If X_{bfn}^R and Y_{bfn}^R are decomposed:

$$\begin{bmatrix} X_{bfn}^R \\ Y_{bfn}^R \end{bmatrix} = \begin{bmatrix} d_n \cdot \cos(\beta) \\ d_n \cdot \sin(\beta) \end{bmatrix} \quad (3.7)$$

By substituting Equation 3.7 in Equation 3.6 , it is obtained the following:

$$\begin{bmatrix} X_{bfn}^G \\ Y_{bfn}^G \end{bmatrix} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix} \begin{bmatrix} d_n \cdot \cos(\beta) \\ d_n \cdot \sin(\beta) \end{bmatrix} + \begin{bmatrix} X_{RG} \\ Y_{RG} \end{bmatrix} \quad (3.8)$$

In order to consider the first iteration, a variable fi was created to set the current value of x and y as 0,0 once, as defined in the initialization. In the next iteration, the pose used is going to be the global position calculated in the next section (Section 3.6). The code was written as following:

```

1 if fi=1 then begin
2   xactual:=0;
3   yactual:=0;
4   fi:=0;
5 end;
6   for j:=0 to 3 do
7     begin
8       xb[j]:=average[j]*(cos(rad(actual_theta))*cos(rad
          (averageangle[j]))-sin(rad(actual_theta))*sin(
          rad(averageangle[j]))) +xactual;
9       yb[j]:=average[j]*(sin(rad(actual_theta))*cos(rad
          (averageangle[j]))+cos(rad(actual_theta))*sin(
          rad(averageangle[j]))) +yactual;
10      end;

```

To organize the code, each beacon is going to be defined as: Beacon 4 refers to B1, Beacon 2 refers to B2, Beacon 1 refers to B3 and Beacon 3 refers to B4.

After calculating the value of each beacon found, the algorithm it is going to be compare the value of the global coordinates of the n beacons found with the nominal global value of the beacons, using quadrants. It is possible to have 4 valid scenarios:

- If the first beacon found coordinates are both positives, that means $x_{bf1} > 0$ and

$y_{bf1} > 0$, then the sequence of measurements are B1, B2, B3 and B4.

- If the first beacon found x coordinate is negative and the y is positive, that means $x_{bf1} < 0$ and $y_{bf1} > 0$, then the sequence of measurements are B2, B3, B4 and B1.
- If the first beacon found coordinates are both negatives, that means $x_{bf1} < 0$ and $y_{bf1} < 0$, then the sequence of measurements are B3, B4, B1 and B2.
- If the first beacon found x coordinate is positive and the y is negative, that means $x_{bf1} > 0$ and $y_{bf1} < 0$, then the sequence of measurements are B4, B1, B2 and B3.

The integral code is in Appendix C.

3.6 Robot estimated global position

Once the beacons have been correctly identified, a system of equations will be set up to determine the values of $X_{RG,estimated}$ and $Y_{RG,estimated}$. In this simulated plant were placed four beacons (B1, B2, B3 and B4), as shown in the Figure 3.2. The global coordinates x_{Bn} , y_{Bn} (for $n = 1, \dots, 4$) of each beacon are known, the relative distance d_{Bn} between the robot's sensor and the beacon found B_{fn} and the angle ϕ_{Bn} between the beacon and the robot's frame reference can be calculated from the LiDAR data.

The coordinates of each beacon are given as following:

$$B1 = (0.90, 0.65)$$

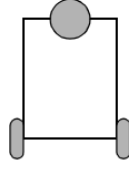
$$B2 = (-0.90, 0.65)$$

$$B3 = (-0.90, -0.65)$$

$$B4 = (0.90, -0.65)$$

The AGV is differential with two drive wheels and a castor wheel, as shown in the Figure 3.5.

The objective is to know the global pose $\zeta_{current}$ of the robot using the coordinates and measurements from the robot's sensor that is defined as the Equation 2.1:



$$\begin{array}{l} \text{Differential} \\ \delta_M = 2 \\ \delta_m = 2 \\ \delta_s = 0 \end{array}$$

Figure 3.5: Differential AGV [15]

$$\zeta_{current} = [x, y, \theta]^T \quad (3.9)$$

In order to do that, the trilateration equations are going to be applied.

As seen in Chapter 2, the distance between the robot and each beacon is defined as the equation 2.10, when applied to the problem context:

$$d_{Bn}^2 = (x_{Bn} - x)^2 + (y_{Bn} - y)^2 \quad (3.10)$$

Where x and y are the global coordinates of the robot. Expanding Equation 3.10:

$$d_{Bn}^2 = x_{Bn}^2 - 2.x_{Bn}.x + x^2 + y_{Bn}^2 - 2.y_{Bn}.y + y^2 \quad (3.11)$$

By isolating x^2+y^2 , it is obtained:

$$x^2 + y^2 = 2.x_{Bn}.x + 2.y_{Bn}.y + d_{Bn}^2 - y_{Bn}^2 - x_{Bn}^2 \quad (3.12)$$

To simplify the problem, it is going to set the constants as:

$$a_{Bn} = 2.x_{Bn} \quad (3.13)$$

$$b_{Bn} = 2.y_{Bn} \quad (3.14)$$

$$c_{Bn} = d_{Bn}^2 - y_{Bn}^2 - x_{Bn}^2 \quad (3.15)$$

Replacing equations 3.13, 3.14 and 3.15 in equation 3.9:

$$x^2 + y^2 = a_{Bn}.x + b_{Bn}.y + c_{Bn} \quad (3.16)$$

For n=1,2,3,4:

$$x^2 + y^2 = a_{B1}.x + b_{B1}.y + c_{B1} \quad (3.17)$$

$$x^2 + y^2 = a_{B2}.x + b_{B2}.y + c_{B2} \quad (3.18)$$

$$x^2 + y^2 = a_{B3}.x + b_{B3}.y + c_{B3} \quad (3.19)$$

$$x^2 + y^2 = a_{B4}.x + b_{B4}.y + c_{B4} \quad (3.20)$$

As there are four beacons positioned in a mirrored manner, there will be some ambiguities. When is used two horizontal beacons in a row, the value of y_{Bn} are the same, so, $b_{Bn} = b_{Bn+1}$ so in this case, it is just possible to calculate $x_{n,n+1}$. On the other hand, when it is used two vertical beacons in a row, the value of x_{Bn} are the same, so $a_{Bn} = a_{Bn+1}$, so it is only possible to calculate $y_{n,n+1}$. It is going to be used Beacons (4,2), (2,1), (1,3), and (3,4) with bilaterations, and along with the diagonals (4,1) and (2,3) with two bilaterations combined.

3.6.1 Robot global position based on beacons B1 and B2

In this particular case, $b_{B1} = b_{B2}$, so no $y_{1,2}$ can be calculated. Equating Equation (3.17) to Equation (3.18):

$$a_{B1}.x + b_{B1}.y + c_{B1} = a_{B2}.x + b_{B2}.y + c_{B2} \quad (3.21)$$

Isolating x, and calling as $x_{1,2}$:

$$x_{1,2} = \frac{c_{B2} - c_{B1}}{a_{B1} - a_{B2}} \quad (3.22)$$

To $y_{1,2}$ the value is going to be undefined, so:

$$y_{1,2} = NaN \quad (3.23)$$

3.6.2 Robot global position based on beacons B2 and B3

In this particular case, $a_{B2} = a_{B3}$, so no $x_{2,3}$ can be calculated. Equating Equation (3.18) to Equation (3.19):

$$a_{B2}.x + b_{B2}.y + c_{B2} = a_{B3}.x + b_{B3}.y + c_{B3} \quad (3.24)$$

So:

$$x_{2,3} = NaN \quad (3.25)$$

Isolating $y_{2,3}$:

$$y_{2,3} = \frac{c_{B3} - c_{B2}}{b_{B2} - b_{B3}} \quad (3.26)$$

3.6.3 Robot global position based on beacons B3 and B4

Similar to B1 and B2, $b_{B3} = b_{B4}$, so no $y_{3,4}$ can be calculated. Equating Equation (3.19) to Equation (3.20):

$$a_{B3}.x + b_{B3}.y + c_{B3} = a_{B4}.x + b_{B4}.y + c_{B4} \quad (3.27)$$

Isolating x, and calling as $x_{3,4}$:

$$x_{3,4} = \frac{c_{B4} - c_{B3}}{a_{B3} - a_{B4}} \quad (3.28)$$

To $y_{3,4}$ the value is going to be undefined, so:

$$y_{3,4} = NaN \quad (3.29)$$

3.6.4 Robot global position based on beacons B4 and B1

Similar to B2 and B3, $a_{B4} = a_{B1}$, so no $x_{4,1}$ can be calculated. Equating Equation (3.20) to Equation (3.17):

$$a_{B4}.x + b_{B4}.y + c_{B4} = a_{B1}.x + b_{B1}.y + c_{B1} \quad (3.30)$$

So:

$$x_{4,1} = NaN \quad (3.31)$$

Isolating $y_{4,1}$:

$$y_{4,1} = \frac{c_{B1} - c_{B4}}{b_{B4} - b_{B1}} \quad (3.32)$$

3.6.5 Robot global position based on diagonal beacons B1,B3 and B2,B4

To diagonal B1,B3:

$$a_{B1}.x + b_{B1}.y + c_{B1} = a_{B3}.x + b_{B3}.y + c_{B3} \quad (3.33)$$

Isolating x:

$$x = \frac{c_{B3} - c_{B1}}{a_{B1} - a_{B3}} + \frac{b_{B3} - b_{B1}}{a_{B1} - a_{B3}}y \quad (3.34)$$

Isolating y:

$$y = \frac{c_{B3} - c_{B1}}{b_{B1} - b_{B3}} + \frac{a_{B3} - a_{B1}}{b_{B1} - b_{B3}}x \quad (3.35)$$

To diagonal B2, B4:

$$a_{B2}.x + b_{B2}.y + c_{B2} = a_{B4}.x + b_{B4}.y + c_{B4} \quad (3.36)$$

Similarly to x and y:

$$x = \frac{c_{B4} - c_{B2}}{a_{B2} - a_{B4}} + \frac{b_{B4} - b_{B2}}{a_{B2} - a_{B4}}y \quad (3.37)$$

$$y = \frac{c_{B4} - c_{B2}}{b_{B2} - b_{B4}} + \frac{a_{B4} - a_{B2}}{b_{B2} - b_{B4}}x \quad (3.38)$$

From Equation (3.35) = (3.38):

$$\frac{c_{B3} - c_{B1}}{b_{B1} - b_{B3}} + \frac{a_{B3} - a_{B1}}{b_{B1} - b_{B3}}x = \frac{c_{B4} - c_{B2}}{b_{B2} - b_{B4}} + \frac{a_{B4} - a_{B2}}{b_{B2} - b_{B4}}x \quad (3.39)$$

$$x \left[\frac{a_{B3} - a_{B1}}{b_{B1} - b_{B3}} - \frac{a_{B4} - a_{B2}}{b_{B2} - b_{B4}} \right] = \frac{c_{B4} - c_{B2}}{b_{B2} - b_{B4}} - \frac{c_{B3} - c_{B1}}{b_{B1} - b_{B3}} \quad (3.40)$$

Isolating x and calling as $x_{d(1,3),d(2,4)}$:

$$x_{d(1,3),d(2,4)} = \frac{(c_{B4} - c_{B2})(b_{B1} - b_{B3}) - (c_{B3} - c_{B1})(b_{B2} - b_{B4})}{(a_{B3} - a_{B1})(b_{B2} - b_{B4}) - (a_{B4} - a_{B2})(b_{B1} - b_{B3})} \quad (3.41)$$

From Equation (3.34) = (3.37):

$$\frac{c_{B3} - c_{B1}}{a_{B1} - a_{B3}} + \frac{b_{B3} - b_{B1}}{a_{B1} - a_{B3}}y = \frac{c_{B4} - c_{B2}}{a_{B2} - a_{B4}} + \frac{b_{B4} - b_{B2}}{a_{B2} - a_{B4}}y \quad (3.42)$$

$$y \left[\frac{b_{B3} - b_{B1}}{a_{B1} - a_{B3}} - \frac{b_{B4} - b_{B2}}{a_{B2} - a_{B4}} \right] = \frac{c_{B4} - c_{B2}}{a_{B2} - a_{B4}} - \frac{c_{B3} - c_{B1}}{a_{B1} - a_{B3}} \quad (3.43)$$

Finally:

$$y_{d(1,3),d(2,4)} = \frac{(c_{B4} - c_{B2})(a_{B1} - a_{B3} - (c_{B3} - c_{B1})(a_{B2} - a_{B4}))}{(b_{B3} - b_{B1})(a_{B2} - a_{B4}) - (b_{B4} - b_{B2})(a_{B1} - a_{B3})} \quad (3.44)$$

To have a best global position estimate of the robot, it is going to be used the average value, as shown in the next equations:

$$x_{RG,estimated} = \frac{x_{1,2} + x_{2,3} + x_{3,4} + x_{4,1} + x_{d(1,3),d(2,4)}}{5} \quad (3.45)$$

$$y_{RG,estimated} = \frac{y_{1,2} + y_{2,3} + y_{3,4} + y_{4,1} + y_{d(1,3),d(2,4)}}{5} \quad (3.46)$$

SimTwo provides the global position of the robot, so it is possible to calculate the absolute error in order to compare the accuracy of the results:

$$E_x = x - x_{RG} \quad (3.47)$$

$$E_y = y - y_{RG} \quad (3.48)$$

$$E_\theta = \theta - \theta_{estimated} \quad (3.49)$$

In the code, after identifying each beacon, the constants a, b and c are calculated and the equations are applied. The algorithm fluxogram is shown in the Appendix B and the code is shown in the Appendix C.

In the next chapter it is going to be shown the results and errors obtained.

Chapter 4

Results Obtained and Analysis of Results

This chapter presents the tests carried out to verify that the developed project meets the assumed objectives and, if solves the problem described in the previous chapter. The first part is to validate the beacon identification algorithm in order to see its problems and limitations and to test the robot estimated position algorithm, testing some poses and calculating respective errors.

4.1 Testing the Beacon Identification algorithm

In order to calculate the global position of the robot it is first needed to identify each beacon. To do that, the beacon identification algorithm is tested for 4 known scenarios, for $\theta=[0,90, 180, 270]$ degrees set in Config tab on SimTwo. In each of these θ values is expected that one of each beacons be the first detected. For instance, for $\theta = 0$ degrees, is expected that the first beacon detected be Beacon 4, if $\theta = 90$ degrees, the first one should be Beacon 2, if $\theta = 180$ degrees, the first one should be Beacon 1 and lastly, if $\theta = 270$ degrees, the first one should be Beacon 3. The subsections below will show the coordinates found and errors.

4.1.1 Sequence of Beacon detected: 4, 2, 1 and 3

The angle was set to 0 degrees in the config tab as shown in Figure 4.1 . The Table 4.1 shows the coordinates of each beacon found and its errors.

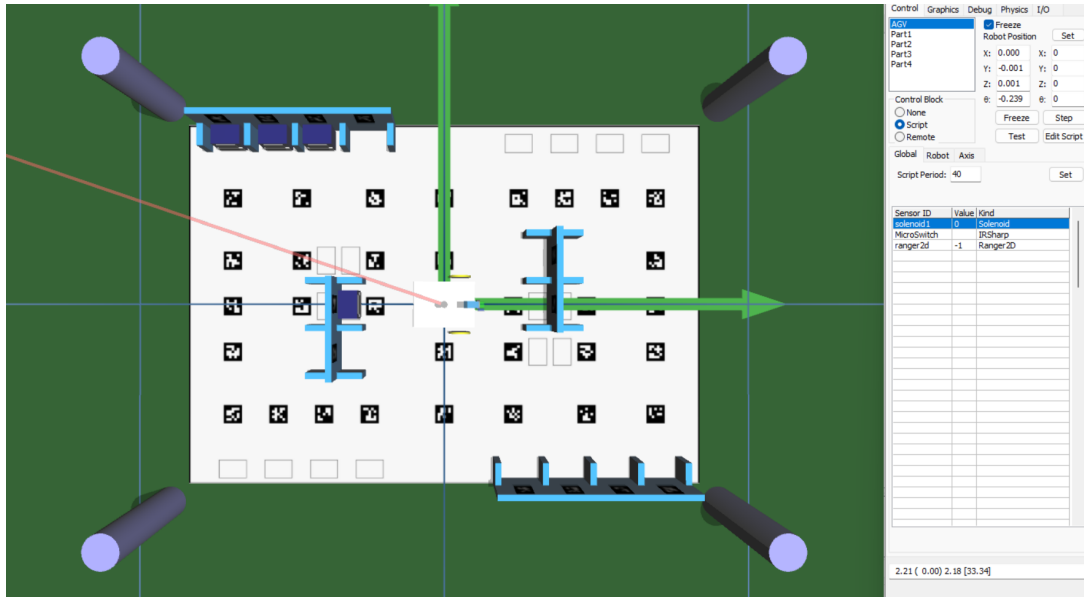


Figure 4.1: Beacon identification for $\theta = 0$ degrees

Table 4.1: Calculated coordinates of Beacons 4, 2, 1 and 3

	B_{f1}	Error	B_{f2}	Error	B_{f3}	Error	B_{f4}	Error
x_{bfn}	0,907883	-0,00788	-0,89861	-0,00139	-0,91118	0,01118	0,898925	0,001075
y_{bfn}	0,653851	-0,00385	0,658621	-0,00862	-0,63237	-0,01763	-0,65885	0,00885

4.1.2 Sequence of Beacon detected: 2, 1, 3 and 4

The angle was set to 90 degrees in the config tab as shown in Figure 4.2 . The Table 4.2 shows the coordinates of each beacon found and its errors.

Table 4.2: Calculated coordinates of Beacons 2, 1, 3 and 4

	B_{f1}	Error	B_{f2}	Error	B_{f3}	Error	B_{f4}	Error
xbfn	-0,90214	0,00214	-0,90992	0,00992	0,900571	-0,00057	0,916214	-0,01621
ybfn	0,656396	-0,0064	-0,63619	-0,01381	-0,65525	0,00525	0,640596	0,009404

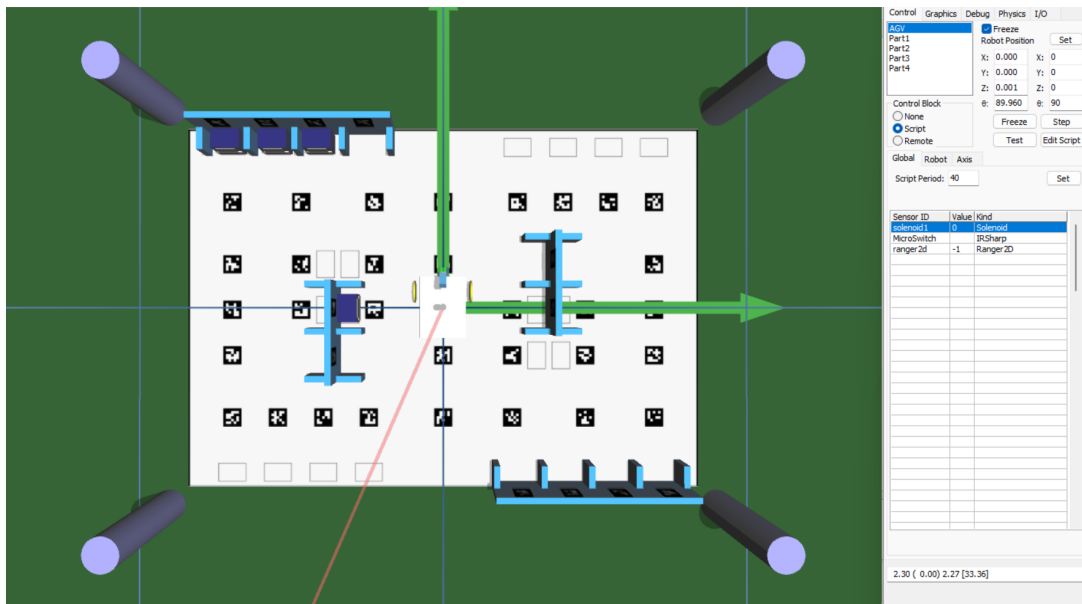


Figure 4.2: Beacon identification for $\theta = 90$ degrees

4.1.3 Sequence of Beacon detected: 1, 3, 4 and 2

The angle was set to 180 degrees in the config tab as shown in Figure 4.3 . The Table 4.3 shows the coordinates of each beacon found and its errors.

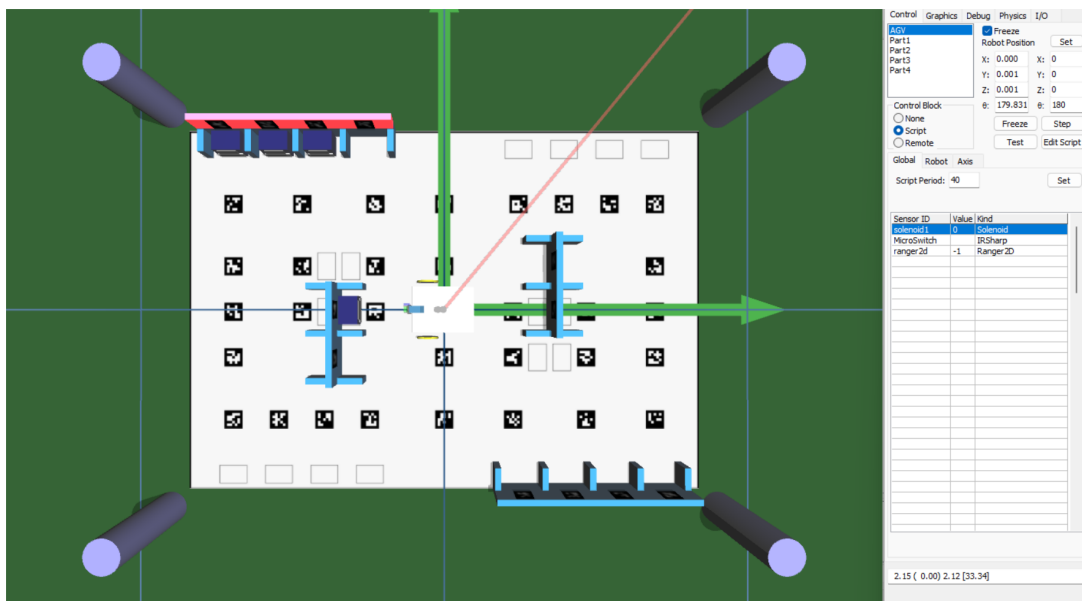


Figure 4.3: Beacon identification for $\theta = 180$ degrees

Table 4.3: Calculated coordinates of Beacons 1, 3, 4 and 2

	B_{f1}	Error	B_{f2}	Error	B_{f3}	Error	B_{f4}	Error
xbf_n	-0,91122	0,01122	0,901195	-0,00119	0,914454	-0,01445	-0,8967	-0,0033
ybf_n	-0,64591	-0,00409	-0,65883	0,00883	0,636286	0,013714	0,65555	-0,00555

4.1.4 Sequence of Beacon detected: 3, 4, 2 and 1

The angle was set to 270 degrees in the config tab as shown in Figure 4.4 . The Table 4.4 shows the coordinates of each beacon found and its errors.

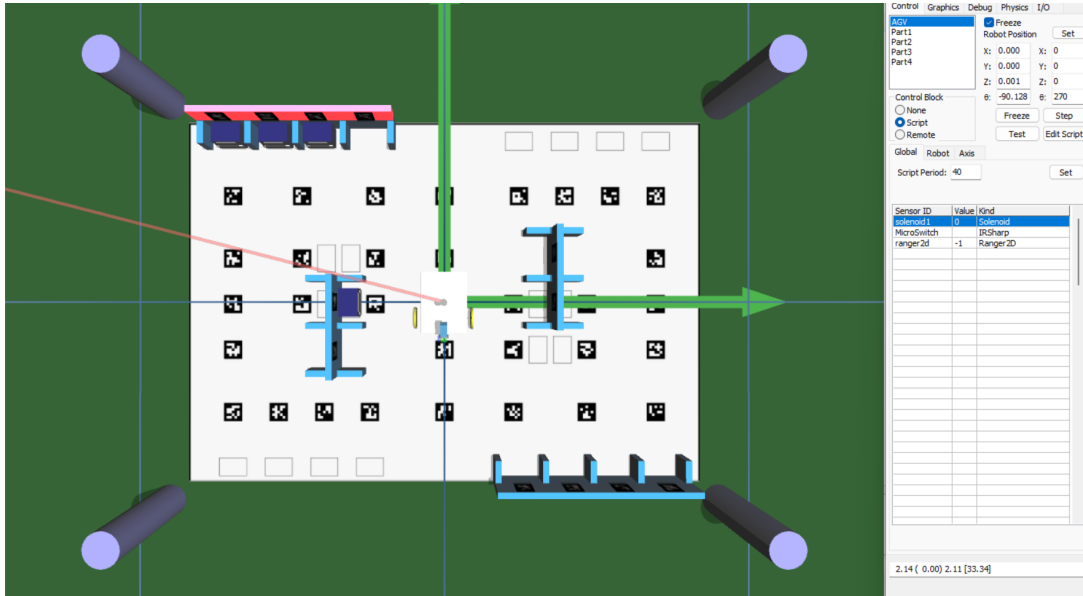


Figure 4.4: Beacon identification for $\theta = 270$ degrees

Table 4.4: Calculated coordinates of Beacons 3, 4, 2 and 1

	B_{f1}	Error	B_{f2}	Error	B_{f3}	Error	B_{f4}	Error
xbf_n	-0,91122	0,01122	0,901195	-0,00119	0,914454	-0,01445	-0,8967	-0,0033
ybf_n	-0,64591	-0,00409	-0,65883	0,00883	0,636286	0,013714	0,65555	-0,00555

While testing various positions, some limitations were found:

- If the robot is moved outside of the factory this algorithm loses its function
- If the robot approaches one of the beacons, the error increases significantly, but it does not invalidate the algorithm used (quadrants).

- The solution used is very specific because of the mirrored manner, so can not be applied in different beacon's layouts.

4.2 Testing the Robot Estimated Position algorithm

To test the algorithm, it was simulated 8 random points in order to test if the equations work properly and the values are consistent. These are shown in table 4.5 below.

Table 4.5: Positions estimated versus Real positions

i	$x_{RG,i,estimated}$	$x_{RG,i,groundtruth}$	$E_{x,i}$	$y_{RG,i,estimated}$	$y_{RG,i,groundtruth}$	$E_{y,i}$	$\theta_{i,estimated}$	$\theta_{i,groundtruth}$	$E_{i,\theta}$
1	-0,002807443	-0,001309687	0,00149775583	-0,00369	-0,00122	0,002473013	-0,004711633	-0,004711633	0,00
2	0,217148249	0,21541205	-0,00173619826	0,392511	0,401497	0,008985478	0,232106514	0,232106514	0,00
3	0,651283112	0,635270596	-0,01601251687	0,306509	0,321843	0,015334638	-0,284538315	-0,284538315	0,00
4	0,492428655	0,478093535	-0,01433511997	-0,29024	-0,3042	-0,013962186	-0,343633163	-0,343633163	0,00
5	-0,406991609	-0,395926952	0,01106465654	-0,44061	-0,4586	-0,017998068	2,829766579612	2,829766579612	0,00
6	-0,634434132	-0,616434634	0,01799949841	-0,12655	-0,13469	-0,008137588	1,320969797123	1,320969797123	0,00
7	-0,691740357	-0,667012274	0,02472808308	-0,30572	-0,32189	-0,016169444	2,013420540873	2,013420540873	0,00
8	-0,615873271	-0,597346663	0,01852660750	0,151066	0,155716	0,004650174	1,504164717567	1,504164717567	0,00

The Figure 4.5 below shows the real position of the robot in the global frame versus the estimated robot's position.

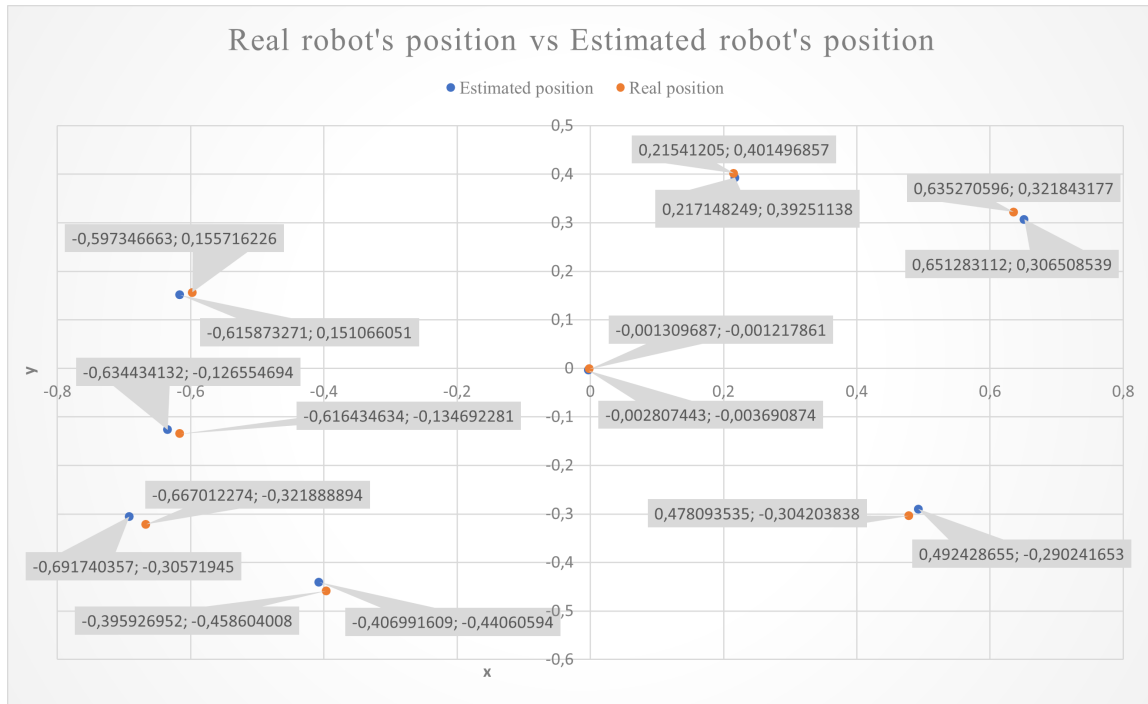


Figure 4.5: Real robot's position versus Estimated Robot's position

Analysing the results obtained, it is possible to see that:

- There is some issue calculating the θ value, because the error is "zero" to all points.
- On the other hand, the error found regarding the x_{RG} and y_{RG} coordinates were pretty low, considering the dimension of the model (1,68m x 1,18m). In these points, the maximum error was 0,02472808308, that it is approximately 2,47 cm. These errors can be associated to the approximations used when the average value is considered. Other point is that in this particular work trilateration was not properly used. Considering the layout of the beacons, bilateration was enough to solve the problem of sequential beacons, but with two reference points the consequence is increasing the error.
- Another point that was not taken in consideration was the angle of the LiDAR and the center of the beacon. The beacon has a significant radius that can interfere in the final calculation of the robot's global position, in this work, instead of calculating this angle, the value of the radius was just summed to the average distance in order to simplify the problem.

Each position is shown in the Figures 4.6, 4.7, 4.8, 4.9, 4.10, 4.11,4.12 and 4.13 below.

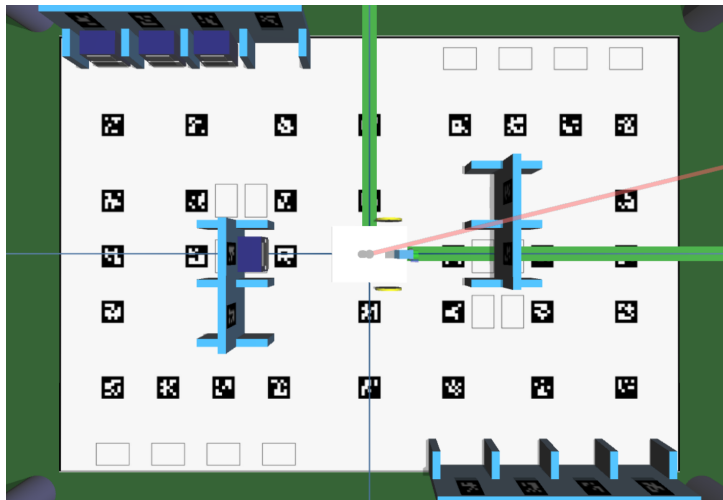


Figure 4.6: Position $i=1$

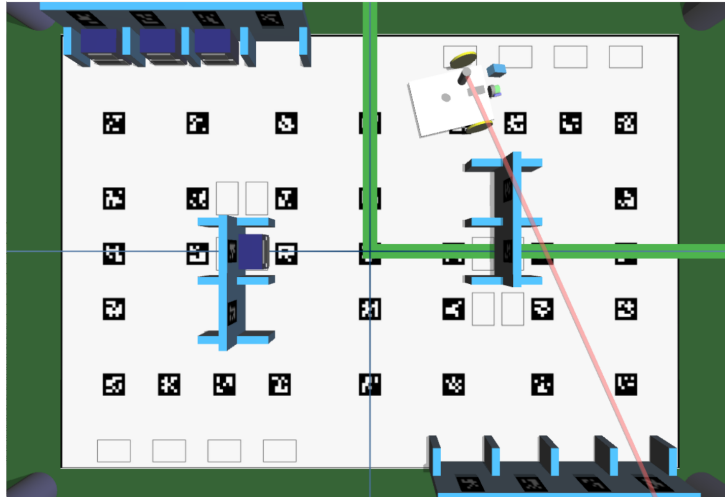


Figure 4.7: Position $i=2$

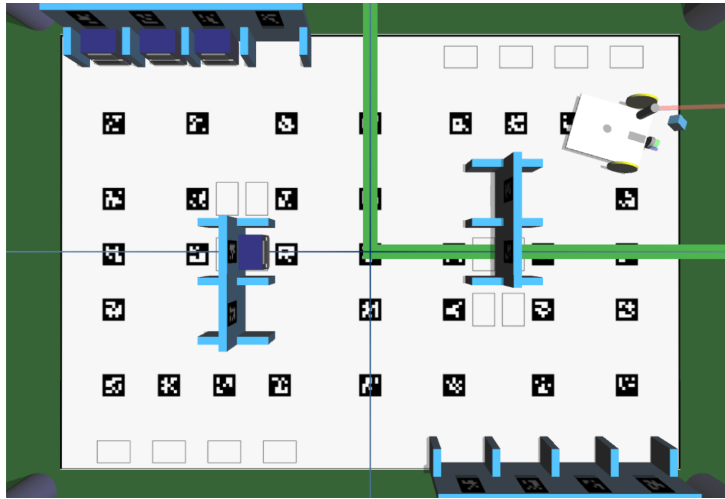


Figure 4.8: Position $i=3$

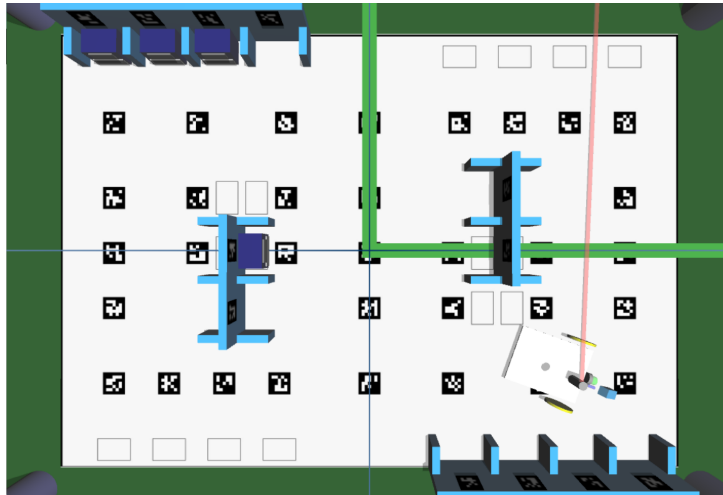


Figure 4.9: Position $i=4$

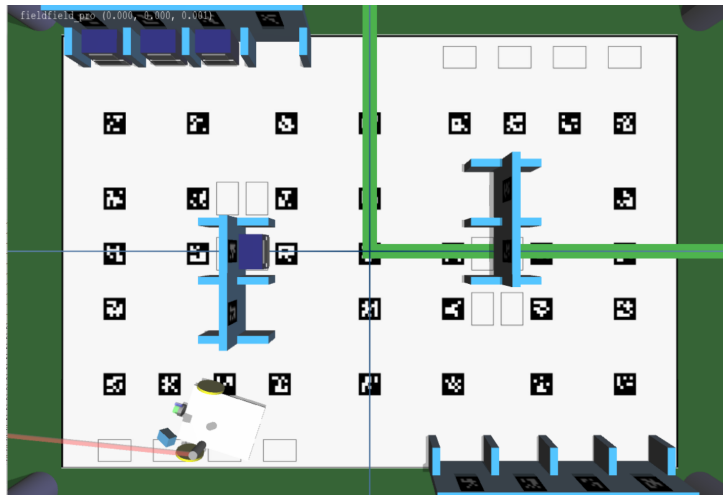


Figure 4.10: Position $i=5$

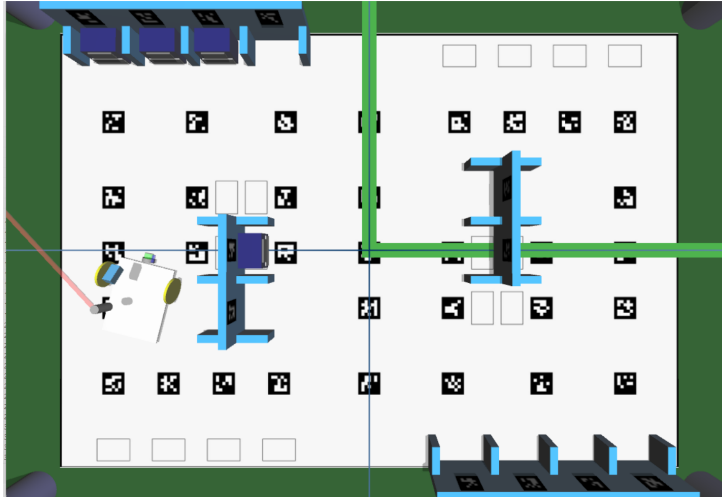


Figure 4.11: Position $i=6$

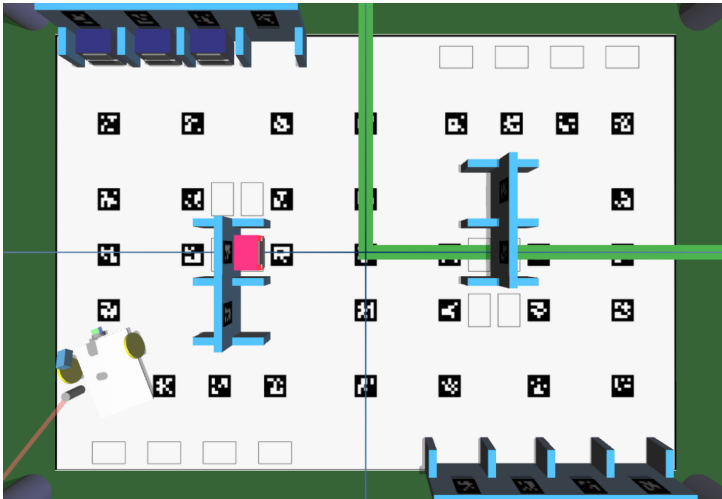


Figure 4.12: Position $i=7$

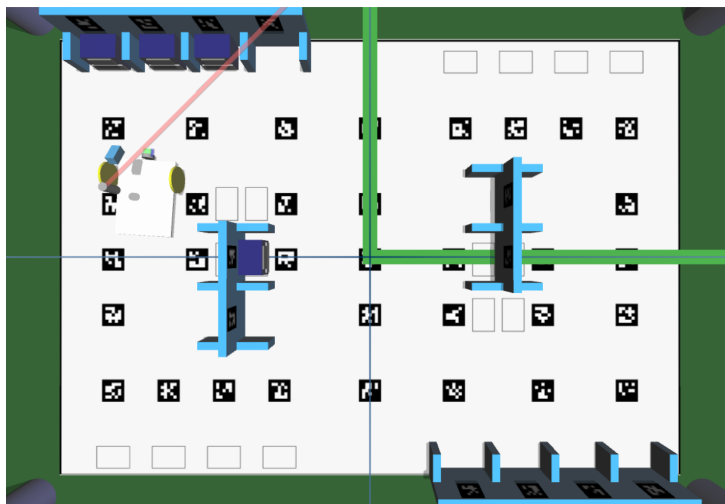


Figure 4.13: Position $i=8$

Chapter 5

Conclusions

Considering the objectives set on Chapter 1, the results of this work were plausible. Even though the trilateration technique was not properly used, but a modified bilateration, the errors found were acceptable. The results obtained from the Beacon Identification algorithm and the Robot Estimated Position algorithm provide valuable insights into the effectiveness and limitations of the developed project.

In the case of the Beacon Identification algorithm, it was observed that the algorithm successfully identified beacons and calculated their coordinates for various robot orientations. However, some limitations were identified, such as the algorithm's inability to function if the robot is moved outside the factory area, and an increase in error when the robot approaches one of the beacons. Additionally, the algorithm's applicability is limited to this specific beacon layout due to its mirrored approach.

Regarding the Robot Estimated Position algorithm, the results showed that the algorithm accurately estimated the robot's global position in terms of x and y coordinates, with errors within a reasonable range given the dimensions of the model. However, there was an issue in calculating the θ value, as the error remained consistently at zero for all tested points. This suggests that further refinement is needed in determining the orientation of the robot.

The study also highlighted the impact of using bilateration instead of trilateration for sequential beacons and the need to consider the angle of the LiDAR in relation to the

beacon's center for more accurate results.

In retrospect, there are several aspects that could have been approached differently, such as improving the accuracy of θ calculation and addressing the limitations of the algorithm when the robot is outside the factory area. Nevertheless, the project succeeded in going beyond the initial objectives by developing functional algorithms for beacon identification and robot position estimation.

Overall, the results obtained in this study contribute to the understanding of the project's strengths and weaknesses and provide a foundation for future improvements and enhancements in the field of robotics and localization systems.

5.1 Future work

In future work, it would be prudent to explore alternative avenues for the simulation framework utilized in this project. Although SimTwo was employed for the entirety of the code development, it became apparent that the simulation imposed a substantial computational load. Therefore, one promising direction for improvement could involve transitioning to a more computationally efficient programming language, such as Python or C++. Given that SimTwo offers UDP communication capabilities, this migration could facilitate a smoother and more streamlined simulation process.

Furthermore, enhancing the beacon identification algorithm represents another promising avenue for future research. While the current approach relies on a quadrant-based methodology, which may not be suitable for all layouts, a more sophisticated and adaptable beacon identification system could be developed. This would not only make the system more versatile but also align it with a broader range of real-world scenarios, providing enhanced accuracy and applicability in diverse contexts.

About the calculation of the robot's orientation angle, θ , in future studies should be a key focal point. As observed in the current work, the error associated with θ remained consistently at zero for all tested points, indicating a potential issue in the calculation process. Investigating and refining the method for determining the robot's orientation

angle is paramount to achieving more accurate and reliable results in future applications.

By resolving these limitations and improving the accuracy of θ calculation, the project's overall performance can be significantly enhanced, making it more robust and adaptable to a wider range of scenarios and layouts. This step would be critical for achieving comprehensive and precise localization of the robot in real-world environments, thereby broadening the practical applications of the developed algorithms.

Bibliography

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Appendix A

Proposta Original do Projeto



Mestrado em Engenharia Industrial - Eletrotécnica

Desenvolvimento e Avaliação de um Sistema de Localização por Trilateração Utilizando Quatro Beacons na Plataforma Simtwo

Orientador: José Luís Sousa de Magalhães Lima

Coorientador: Marcos Banheti Rabello Vallim

1 Objetivo

Implementar um sistema de localização por trilateração através da plataforma Simtwo utilizando quatro beacons. Fazer análise de erros, comparando aos dados reais fornecidos pela plataforma.

2 Detalhes

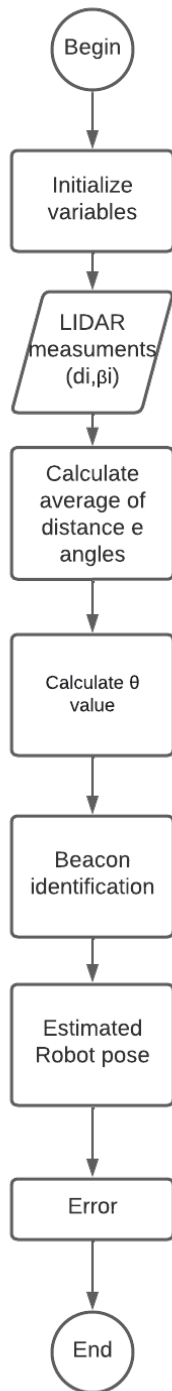
A localização precisa é uma necessidade crítica em várias aplicações, como rastreamento de ativos, navegação indoor, e automação industrial. A trilateração é uma técnica comum usada para determinar a localização de um objeto com base nas medições de distância de múltiplos beacons. Este projeto de tese visa desenvolver e avaliar um sistema de localização por trilateração utilizando a plataforma Simtwo, empregando quatro beacons para melhorar a precisão da localização. O objetivo é analisar a eficácia do sistema, comparando os resultados com dados reais fornecidos pela plataforma.

3 Metodologia de trabalho

- **Configuração da Plataforma Simtwo:** Configurar um ambiente simulado na plataforma Simtwo, com quatro beacons posicionados estrategicamente e um objeto a ser localizado.
 - **Desenvolvimento do Sistema de Trilateração:** Implementar o sistema de localização por trilateração, que coleta medições de distância dos beacons para calcular a posição estimada do objeto.
 - **Coleta de Dados:** Realizar uma série de experimentos nos quais o objeto se move dentro do ambiente simulado, coletando dados de medições de distância.
 - **Análise de Erros:** Analisar os erros de localização, considerando fatores como ruído nas medições, interferência e propagação do sinal, e outros possíveis desafios.
-

Appendix B

Fluxogram



Appendix C

Code

```
1  function PrepareLaserSweepPackage(LaserScanRays: Matrix) :  
    string;  
2  
3  
4  var  
5      i, j, l, m, alfa, bf, k11, k12, k13, nrows, gama, n, fi  
        : integer;  
6      xcal1, ycal1, xcal2, ycal2, xcal3, ycal3, xcal4, ycal4,  
        xdiag, ydiag, xavg, yavg, a1, b1, c1, a2, b2, c2,  
        a3, b3, c3, a4, b4, c4, m31, n31, m24, n24, m34, n34  
        , m41, n41, rb: double;  
7      previous_phi : array of double;  
8      actual_theta: double;  
9      vx, vy, xanterior, yanterior, omega, yactual, xactual:  
        double;  
10     previous_theta: double;  
11     actual_phi : array of double;  
12     temp : string;
```

```

13     averageangle: array of double;
14     distance : array of double;
15     angle : array of double;
16     numberofpoints: array of double;
17     sumdistance: array of double;
18     sumangle: array of double;
19     average: array of double;
20     bf1,bf2,bf3,bf4: array of double;
21     xb: array of double;
22     yb: array of double;
23     bi1: array of double;
24     bi2: array of double;
25     bi3: array of double;
26     bi4: array of double;
27 begin
28     temp := '';
29     nrows := MNumRows(LaserScanRays); // numero de linhas
30
31     SetLength(distance, nrows - 1);
32     SetLength(angle, nrows - 1);
33     SetLength(sumdistance, 5);
34     SetLength(sumangle, 5);
35     SetLength(numberofpoints, 5);
36     SetLength(average, 5);
37     SetLength(averageangle, 5);
38     SetLength(previous_phi,5);
39     SetLength(actual_phi,5);
40     SetLength(xb, 4);
41     SetLength(yb, 4);

```

```
42  SetLength(bi1, 3);
43  SetLength(bi2, 3);
44  SetLength(bi3, 3);
45  SetLength(bi4, 3);
46
47  vx:=0;
48  vy:=0;
49  omega:=0;
50  fi:=1;
51  actual_theta:= 0;
52  a1:=0;
53  a2:=0;
54  a3:=0;
55  a4:=0;
56  b1:=0;
57  b2:=0;
58  b3:=0;
59  b4:=0;
60  c1:=0;
61  c2:=0;
62  c3:=0;
63  c4:=0;
64  m31:=0;
65  n31:=0;
66  m24:=0;
67  n24:=0;
68  xcal1:=0;
69  ycal1:=0;
70  xcal2:=0;
```

```
71     ycal2:=0;
72     xcal3:=0;
73     ycal3:=0;
74     m34:=0;
75     n34:=0;
76     m41:=0;
77     n41:=0;
78     rb:=0.05;
79     gama:=1;
80     n:=0;
81     l:=0;
82
83
84     j:= 1; // coluna da matriz
85     k11:=1;
86     k12:=1;
87     k13:=1;
88
89 // beacon:=[4, 2, 1,3];
90
91     bf1:=[0.9,0.65,0.150]; // 4
92     bf2:=[-0.9,0.650,0.150]; // 2
93     bf3:=[-0.900,-0.65,0.150]; // 1
94     bf4:=[0.9,-0.650,0.150]; // 3
95
96
97     bf:=0; // beacon found
98     alfa:=0;
99
```

```

100  begin
101  bf:=0; // nenhum beacon encontrado
102      for i := 0 to nrows - 1 do
103          begin
104              temp := temp + FloatToStr( Mgetv(LaserScanRays,
105                  i, 0) ) + ','; // armazena a leitura do
106                  LIDAR em um array temp
107          end;
108
109  // ATRIBUTES VALUES TO DISTANCE AND ANGLE ARRAY OK
110      for i:= 1 to (length(distance)-1) do
111          begin
112              distance[i-1]:= Mgetv(LaserScanRays, i, 0); //
113                  atribui o valor da distancia no array
114              angle[i-1]:=i; // atribui os valores dos angulos
115                  no array
116              j:=j+1;
117          end;
118
119  // SUM DISTANCES FROM EACH UNKNOWN BEACON AND NUMBER OF
120  POINTS MEASURED PER BEACON
121  for i:=1 to (length(distance)) do
122      begin
123
124          if (((distance[i-1])<0) and ((distance[i])>0)) or
125              ((distance[0])> 0) and (i =1)) then
126              begin
127
128                  bf:=bf+1;

```

```

123     if (i = 1) and (distance[0] > 0) then begin
124         sumdistance[bf-1] := sumdistance[bf-1] + distance
           [0];    //@Stefany: distance[i], not distance
           [i-1] (Also need to include the first
           iteration exception
125         sumangle[bf-1] := sumangle[bf-1] + angle[0];
126         numberofpoints[bf-1] := numberofpoints[bf-1] + 1;
127     end;

128
129         sumangle[bf-1] := sumangle[bf-1] + angle[i];
130         sumdistance[bf-1] := sumdistance[bf-1] + distance[i]
           ];    //@Stefany: distance[i], not distance[i]
           -1] (Also need to include the first
           iteration exception
131         numberofpoints[bf-1] := numberofpoints[bf-1] + 1;
132
133     end
134
135     else if (((distance[i-1]) > 0) and ((distance[i])
           > 0)) then    // @Stefany: Use elseif here to
           optimize
136     begin
137
138         sumdistance[bf-1] := sumdistance[bf-1] + distance[i]
           ];
139         sumangle[bf-1] := sumangle[bf-1] + angle[i];
140         numberofpoints[bf-1] := numberofpoints[bf-1] + 1;
141
142     end

```

```

143
144     end;
145
146
147     if (bf=5) then
148     begin
149
150         sumdistance[0]:=sumdistance[0]+ sumdistance[4];
151         sumangle[0]:=sumangle[0]+ sumangle[4] - 360*
152             numberofpoints[4];
153         numberofpoints[0]:=numberofpoints[0]+ numberofpoints
154             [4];
155         bf := 4;
156
157     end;
158
159     // SHOWS THE AVERAGE OF THE ANGLE OF EACH BEACON
160     AND THE DISTANCE
161     begin
162     for m := 0 to 3 do
163     begin
164         average[m] := ((sumdistance[m]) / numberofpoints[m]) + rb
165             ;
166         averageangle[m] := (sumangle[m]) / numberofpoints[m];
167         // if ((averageangle[m] >= 0) and (averageangle[m] <= 90))
168         then
169             actual_phi[m] := averageangle[m]
170         // else if ((averageangle[m] > 90) and (averageangle[m] <=
171             180)) then

```

```

166 //    actual_phi[m] := 180 - averageangle[m]
167 //    else if ((averageangle[m] > 180) and (averageangle[m]
    <= 270)) then
168 //    actual_phi[m] := averageangle[m] - 180
169 //    else if ((averageangle[m] > 270) and (averageangle[m]
    <= 360)) then
170 //    actual_phi[m] := 360 - averageangle[m];
171
172 if (gama = 1) then
173 begin
174     previous_phi[m] := actual_phi[m];
175     previous_theta := (180 * GetRobotTheta(irobot)) / pi;
176     gama := 0;
177 end;
178 end;
179
180 for n := 0 to 3 do
181 begin
182     if actual_phi[n] <> previous_phi[n] then
183     begin
184         actual_theta := previous_theta + previous_phi[0] -
            actual_phi[0]; //corrigir
185         previous_phi[n] := actual_phi[n];
186         previous_theta := actual_theta;
187     end;
188 end;
189
190     SetRCValue(33,1,FloatToStr(actual_phi[0]));
191     SetRCValue(33,2,FloatToStr(actual_phi[1]));

```

```

192         SetRCValue(33,3,FloatToStr(actual_phi[2]));
193         SetRCValue(33,4,FloatToStr(actual_phi[3]));
194
195
196     // BEACON IDENTIFICATION
197     if fi=1 then begin
198         xactual:=0;
199         yactual:=0;
200         fi:=0;
201     end;
202     for j:=0 to 3 do
203
204         begin
205             xb[j]:=average[j]*(cos(rad(actual_theta))*cos(rad
                (averageangle[j]))-sin(rad(actual_theta))*sin(
                rad(averageangle[j]))) + xactual;
206             yb[j]:=average[j]*(sin(rad(actual_theta))*cos(rad
                (averageangle[j])) + cos(rad(actual_theta))*sin(
                rad(averageangle[j]))) + yactual;
207         end;
208
209         if ((xb[0]>0) and (yb[0]>0)) then // starts at
                B4
210
211             begin
212
213                 for l:=0 to 1 do
214
215                     begin

```

```

216
217         bi1[1]:=bf1[1]; //4
218         bi2[1]:=bf2[1]; // 2
219         bi3[1]:=bf3[1]; // 1
220         bi4[1]:=bf4[1]; // 3
221
222         end;
223     a1:=2*bi1[0]; // a1 se refers to beacon 4
224     b1:=2*bi1[1];
225     c1:=((average[0]*average[0])-(bi1[1]*bi1[1])-(bi1
        [0]*bi1[0]));
226
227     a2:=2*bi2[0]; // a2 se refers to beacon 2
228     b2:=2*bi2[1];
229     c2:=(average[1]*average[1]-bi2[1]*bi2[1]-bi2[0]*bi2
        [0]);
230
231     a3:=2*bi3[0]; // a3 se refers to beacon 1
232     b3:=2*bi3[1];
233     c3:=(average[2]*average[2]-bi3[1]*bi3[1]-bi3[0]*bi3
        [0]);
234
235     a4:=2*bi4[0]; // a4 se refers to beacon 3
236     b4:=2*bi4[1];
237     c4:=(average[3]*average[3]-bi4[1]*bi4[1]-bi4[0]*bi4
        [0]);
238
239     end
240

```

```

241         else if ((xb[0]>0) and (yb[0]<0)) then //
                starts at beacon B3
242
243         begin
244
245             bi1:=[0.9,-0.65,0.150]; //3
246             bi2:=[0.9,0.65,0.150]; // 4
247             bi3:=[-0.9,0.65,0.150]; // 2
248             bi4:=[-0.9,-0.65,0.150]; // 1
249
250
251
252         a1:=2*bi2[0]; // a1 se refers to beacon 4
253         b1:=2*bi2[1];
254         c1:=((average[1]*average[1])-(bi2[1]*bi2[1])-(bi2[0]*
                bi2[0]));
255
256         a2:=2*bi3[0]; // a2 se refers to beacon 2
257         b2:=2*bi3[1];
258         c2:=(average[2]*average[2]-bi3[1]*bi3[1]-bi3[0]*bi3[0])
                ;
259
260         a3:=2*bi4[0]; // a3 se refers to beacon 1
261         b3:=2*bi4[1];
262         c3:=(average[3]*average[3]-bi4[1]*bi4[1]-bi4[0]*bi4[0])
                ;
263
264         a4:=2*bi1[0]; // a4 se refers to beacon 3
265         b4:=2*bi1[1];

```

```

266     c4:=(average [0]*average [0]-bi1 [1]*bi1 [1]-bi1 [0]*bi1 [0])
        ;
267     end
268     else if ((xb [0]<0) and (yb [0]<0)) then begin
269     for l:=0 to 1 do
270
271         begin
272
273             bi1 [1]:=bf3 [1]; // 1
274             bi2 [1]:=bf4 [1]; // 3
275             bi3 [1]:=bf1 [1]; // 4
276             bi4 [1]:=bf2 [1]; // 2
277
278
279
280             end;
281     a1:=2*bi3 [0]; // a1 se refers to beacon 4
282     b1:=2*bi3 [1];
283     c1:=((average [2]*average [2])-(bi3 [1]*bi3 [1])-(bi3 [0]*
        bi3 [0]));
284
285     a2:=2*bi4 [0]; // a2 se refers to beacon 2
286     b2:=2*bi4 [1];
287     c2:=(average [3]*average [3]-bi4 [1]*bi4 [1]-bi4 [0]*bi4 [0])
        ;
288
289     a3:=2*bi1 [0]; // a3 se refers to beacon 1
290     b3:=2*bi1 [1];

```

```

291     c3:=(average [0]*average [0]-bi1 [1]*bi1 [1]-bi1 [0]*bi1 [0])
        ;
292
293     a4:=2*bi2 [0]; // a4 se refers to beacon 3
294     b4:=2*bi2 [1];
295     c4:=(average [1]*average [1]-bi2 [1]*bi2 [1]-bi2 [0]*bi2 [0])
        ;
296
297     end
298         else if ((xb [0]<0) and (yb [0]>0)) then begin //
                starts at B2
299
300         for l:=0 to 1 do
301
302             begin
303
304                 bi1 [1]:=bf2 [1]; // 2
305                 bi2 [1]:=bf3 [1]; // 1
306                 bi3 [1]:=bf4 [1]; // 3
307                 bi4 [1]:=bf1 [1]; // 4
308
309             end;
310
311     a1:=2*bi4 [0]; // a1 se refers to beacon 4
312     b1:=2*bi4 [1];
313     c1:=((average [3]*average [3])-(bi4 [1]*bi4 [1])-(bi4 [0]*
        bi4 [0]));
314
315     a2:=2*bi1 [0]; // a2 se refers to beacon 2

```

```

316     b2:=2*bi1[1];
317     c2:=(average[0]*average[0]-bi1[1]*bi1[1]-bi1[0]*bi1[0])
        ;
318
319     a3:=2*bi2[0]; // a3 se refers to beacon 1
320     b3:=2*bi2[1];
321     c3:=(average[1]*average[1]-bi2[1]*bi2[1]-bi2[0]*bi2[0])
        ;
322
323     a4:=2*bi3[0]; // a4 se refers to beacon 3
324     b4:=2*bi3[1];
325     c4:=(average[2]*average[2]-bi3[1]*bi3[1]-bi3[0]*bi3[0])
        ;
326
327     end;
328
329
330         SetRCValue(29,1,'BF1');
331         SetRCValue(29,2,'BF2');
332         SetRCValue(29,3,'BF3');
333         SetRCValue(29,4,'BF4');
334         SetRCValue(30,1,FloatToStr(xb[0]));
335         SetRCValue(31,1,FloatToStr(yb[0]));
336
337         SetRCValue(30,2,FloatToStr(xb[1]));
338         SetRCValue(31,2,FloatToStr(yb[1]));
339
340         SetRCValue(30,3,FloatToStr(xb[2]));
341         SetRCValue(31,3,FloatToStr(yb[2]));

```

```

342
343         SetRCValue(30,4,FloatToStr(xb[3]));
344         SetRCValue(31,4,FloatToStr(yb[3]));
345
346
347     xcal1:=(c2-c1)/(a1-a2);    // B4 e B2
348     ycal1:=999;
349
350     xcal2:=999;    // B2 e B3
351     ycal2:=(c3-c2)/(b2-b3);
352
353     xcal3:=(c4-c3)/(a3-a4);    // B3 e B4
354     ycal3:=999;
355
356     xcal4:=999;    // B4 e B1
357     ycal4:=(c1-c4)/(b4-b1);
358
359     xdiag:= ((c4-c2)*(b1-b3)-(c3-c1)*(b2-b4))/((a3-a1)*(b2-
360         b4)-(a4-a2)*(b1-b3));
361     ydiag:= ((c4-c2)*(a1-a2)-(c3-c1)*(a2-a4))/((b3-b1)*(a2-
362         a4)-(b4-b2)*(a1-a3));
363
364
365     xavg:=(xcal1+xcal2+xcal3+xcal4+xdiag-999-999)/3;
366     yavg:=(ycal1+ycal2+ycal3+ycal4+ydiag-999-999)/3;
367
368     xatual:=xavg;
369     yatual:=yavg;
370
371     SetRCValue(23,2,'1');

```

```

369 SetRCValue(23,3,'2');
370 SetRCValue(23,4,'3');
371 SetRCValue(23,5,'4');
372 SetRCValue(23,6,'Diagonal');
373 SetRCValue(23,7,'Average');
374 SetRCValue(23,8,'Error');
375 SetRCValue(23,9,'Real Value');
376
377 SetRCValue(24,1,'x');
378 SetRCValue(25,1,'y');
379 SetRCValue(24,2,FloatToStr(xcal1));
380 SetRCValue(24,3,FloatToStr(xcal2));
381 SetRCValue(24,4,FloatToStr(xcal3));
382 SetRCValue(24,5,FloatToStr(xcal4));
383 SetRCValue(24,6,FloatToStr(xdiag));
384 SetRCValue(24,7,FloatToStr(xavg));
385 SetRCValue(24,8,FloatToStr(GetRobotX(irobot)-xavg));
386 SetRCValue(24,9,FloatToStr(GetRobotX(irobot)));
387
388 SetRCValue(25,2,FloatToStr(ycal1));
389 SetRCValue(25,3,FloatToStr(ycal2));
390 SetRCValue(25,4,FloatToStr(ycal3));
391 SetRCValue(25,5,FloatToStr(ycal4));
392 SetRCValue(25,6,FloatToStr(ydiag));
393 SetRCValue(25,7,FloatToStr(yavg));
394 SetRCValue(25,8,FloatToStr(GetRobotY(irobot)-yavg));
395 SetRCValue(25,9,FloatToStr(GetRobotY(irobot)));
396
397 SetRCValue(26,1,'Theta');

```

```
398     SetRCValue(26,2,FloatToStr(rad(actual_theta)));
399     SetRCValue(26,3,FloatToStr(GetRobotPos2D(irobot).angle))
400         ;
401     end;
402
403     Delete(temp, Length(temp), 1);
404     Result:=temp;
405
406
407     end;
408
409
410     end;
```