

# Fixed Bed Adsorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> and Their Mixtures in Potassium-Exchanged Binder-Free Beads of Y Zeolite

Ezzeldin Aly, Lucas F.A.S. Zafaneli,\* Adriano Henrique, Marcella Golini Pires, Alirio E. Rodrigues, Kristin Gleichmann, and José A.C. Silva\*

**Cite This:** *Ind. Eng. Chem. Res.* 2021, 60, 15236–15247

**Read Online**

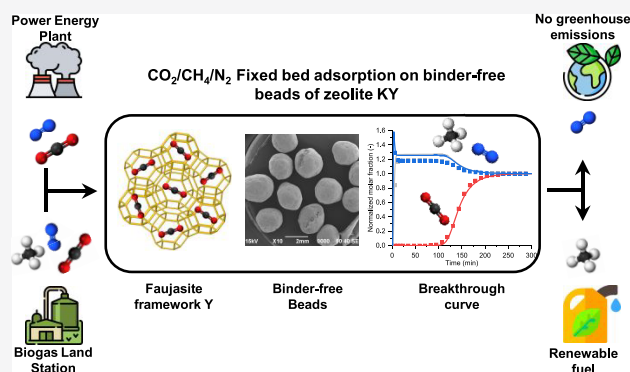
ACCESS |

Metrics & More

Article Recommendations

Supporting Information

**ABSTRACT:** The adsorption of carbon dioxide (CO<sub>2</sub>), methane (CH<sub>4</sub>), and nitrogen (N<sub>2</sub>) has been studied on potassium-exchanged (95%) binder-free beads of Y zeolite through single, binary, and ternary fixed bed breakthrough experiments, covering the temperature range between 313 and 423 K and a pressure of up to 350 kPa. At 313 K and 350 kPa, the single-component data obtained showed that the amounts adsorbed of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> are around 6.42, 1.45, and 0.671 mol kg<sup>-1</sup>, respectively. The binary experiments CO<sub>2</sub>/N<sub>2</sub> carried out under typical post-combustion conditions show a selectivity of CO<sub>2</sub> over N<sub>2</sub> around 104. The ternary experiments resulted in the selectivities of CO<sub>2</sub> over CH<sub>4</sub> and N<sub>2</sub> around 19 and 45, respectively. The adsorption equilibrium data have been modeled by the dual-site Langmuir model, and the breakthrough experiments were numerically simulated with a suitable dynamic fixed bed adsorption model. The model predicts with good accuracy the systematic behavior of all breakthrough experiments. The results shown in the present work prove that the potassium-exchanged binder-free beads of Y zeolite enhance the amount adsorbed of CO<sub>2</sub> at low partial pressure over other alkali metal-exchanged faujasites and efficiently separate it from binary (CO<sub>2</sub>/N<sub>2</sub>) and ternary (CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub>) mixtures by fixed bed adsorption.



## INTRODUCTION

The generation of carbon dioxide is inherent in the combustion of fossil fuels, and the efficient capture of CO<sub>2</sub> from industrial operations is regarded as an important strategy to achieve a significant reduction in atmospheric CO<sub>2</sub> levels.<sup>1–9</sup> Post-combustion capture is referred to as the capture of CO<sub>2</sub> from flue gases produced by the combustion of carbon-based fuels, such as coal<sup>10</sup> or natural gas. It is a crucial capture route as it provides means of CO<sub>2</sub> capture for new and existing combustion technologies without encountering any technological risks or radical changes.<sup>11–13</sup> Adsorption processes are promising capture technologies as they can use specific adsorbents by acting in the limit as molecular sieves to separate CO<sub>2</sub> from other flue gas constituents. Physical adsorbents such as zeolites are safe for the local environment and generally inexpensive to manufacture and scale-up.<sup>12,14</sup>

Major challenges that face post-combustion CO<sub>2</sub> capture technology by adsorption include the low pressure of flue gas (101.3 kPa) and the difficulty to separate the relatively low concentration of CO<sub>2</sub> (10–15%) from the large amounts of nitrogen.<sup>3,15</sup> Processes for removing CO<sub>2</sub> from CH<sub>4</sub> are also important for upgrading both renewable and non-renewable energy sources such as landfill gas, biogas, and natural gas.<sup>16–20</sup> These gases contain significant amounts of methane (50 vol %)

balanced by carbon dioxide, nitrogen, and other contaminants that have to be removed before liquefaction to meet pipeline grade specifications.<sup>21,22</sup>

Adsorption-based gas separations are currently being used to separate CO<sub>2</sub> from mixtures containing CO<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub> for several applications.<sup>23–26</sup> Metal–organic frameworks (MOFs) are considered a new class of adsorbents with great future potential for CO<sub>2</sub> capture due to their high surface area and pore volume.<sup>27</sup> However, MOFs need to be further refined regarding their production in large-scale, chemical, and thermal stability, which are properties already well established in zeolites.<sup>24</sup> Conventional zeolites such as 13X, 4A, and 5A forms are known as having excellent properties to adsorb large amounts of CO<sub>2</sub> while having high CO<sub>2</sub> selectivity in comparison to CH<sub>4</sub> and N<sub>2</sub>.<sup>6,24–26,28–30</sup>

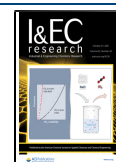
Zeolites Y and X belong to the family of aluminosilicate molecular sieves with a faujasite-type structure (FAU), being

**Received:** June 11, 2021

**Revised:** September 16, 2021

**Accepted:** October 4, 2021

**Published:** October 13, 2021



different only by the Si/Al atomic ratio (1.5–3.0 for NaY compared to 1.0–1.5 for NaX).<sup>31,32</sup> Barrer and Gibbons<sup>33</sup> pioneered the concept of ion exchange by investigating the properties of zeolitic carbon dioxide in different intracrystalline environments in faujasites (Linde Sieve X). It was found that such adsorbents reveal different behaviors and trends based on the modification of the intracrystalline environment through ion exchange. Furthermore, Walton *et al.*<sup>34</sup> and Pirngruber *et al.*<sup>35</sup> have performed studies to examine the CO<sub>2</sub> adsorption on Y and X zeolites modified by alkali metal cation exchange of a parent Na sample. Both studies agree that CO<sub>2</sub> adsorption is influenced by diverse structural characteristics of zeolites such as cation size, acid–base surface properties, size of the pores, number of exchangeable cations, polarizing power, distribution, and Si/Al ratio (details provided in Section S1 of the Supporting Information).<sup>36–39</sup>

By considering all these factors, it is possible to tune the adsorptive properties of zeolites by ion exchange to optimize the most suitable material that enriches substantially the CO<sub>2</sub> adsorption for a specific process. Moreover, zeolite production is well established being an advantage compared to other types of adsorbents to a fast application as they are used industrially for more than 60 years.<sup>40</sup> Furthermore, the development of binder-free zeolite adsorbents has proven to increase the adsorption capacity up to 20%.<sup>24–26,30,41,42</sup>

Experimental and theoretical studies concerning the adsorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> and their mixtures in potassium-exchanged Y zeolite (KY) lack information in the literature. Accordingly, this work aims to investigate by a series of fixed bed breakthrough experiments the adsorption of single, binary, and ternary mixtures of CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub> in binder-free beads of KY zeolite, at temperatures of 313, 373, and 423 K and a total pressure of up to 350 kPa (under compositions typical of post-combustion and biogas upgrading processes). From the data, the single- and multicomponent adsorption equilibrium isotherms were collected and fitted with the single and dual-site Langmuir isotherms. A suitable mathematical model including axial dispersion, mass transfer resistances, and heat effects was also developed and applied to describe and predict numerically the overall dynamics of the experiments. Performance metrics such as selectivities and working capacities were also evaluated. At the same time, the experimental data collected is compared with an already available one in the literature for other ion-exchanged X and Y faujasite zeolites.

## MATERIALS AND METHODS

**Adsorbent and Adsorbate.** The potassium-exchanged (95%) Y zeolite studied in this work was synthesized in the binder-free form in the labs of Chemiewerk Bas Köstritz GmbH (Germany). The bead particle diameter ranges between 1.6 and 2.5 mm. The exchange started from a commercial type of the binder-free Y sodium zeolite form (Köstrolith NaYBFBK) with a Si/Al ratio of 2.5 to achieve the 95% potassium exchange degree value.

Air Liquide supplied the adsorbate and inert gases with the following specifications: He ALPHAGAZ 2 (99.9998%), CO<sub>2</sub> N48 (99.998%), CH<sub>4</sub> N35 (99.95%), and N<sub>2</sub> N50 (99.999%).

**Characterization.** The porous nature of the binder-free zeolite KY was accessed by nitrogen adsorption–desorption at 77 K and a pressure of up to 101.3 kPa using an accelerated surface area and porosimetry system (Micrometrics ASAP

2020 V4.02). Before the experiments, the sample was outgassed at 573 K for 12 h in a vacuum atmosphere.

The porosity of the materials was evaluated by mercury intrusion porosimetry, performed in a pore size analyzer (Micromeritics AutoPore IV 9500), covering the pressure range between 0.003 and 207 MPa, after activation in the same previously described conditions.

The surface morphology of the binder-free zeolite KY was analyzed using a scanning electron microscopy instrument (JEOL Model JSM-6490) with a high resolution of 3.0 nm.

All the characterization studies were performed at the Laboratorio de Sólidos Porosos of Málaga University.

**Experimental Procedure.** A homemade single- and multicomponent breakthrough apparatus was used to study the fixed bed adsorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> and their binary/ternary mixtures. This apparatus was used in previous works<sup>41</sup> and is illustrated in Figure S1 of the Supporting Information. Table S1 shows the properties of the adsorbent and column used in the experiments performed through this work.

The experimental system consists of three main sections, namely, the gas preparation section, adsorption column system, and an analytical system using a thermal conductivity detector (TCD) gas chromatograph (SRI 8610C - Gas Chromatograph equipment, USA).

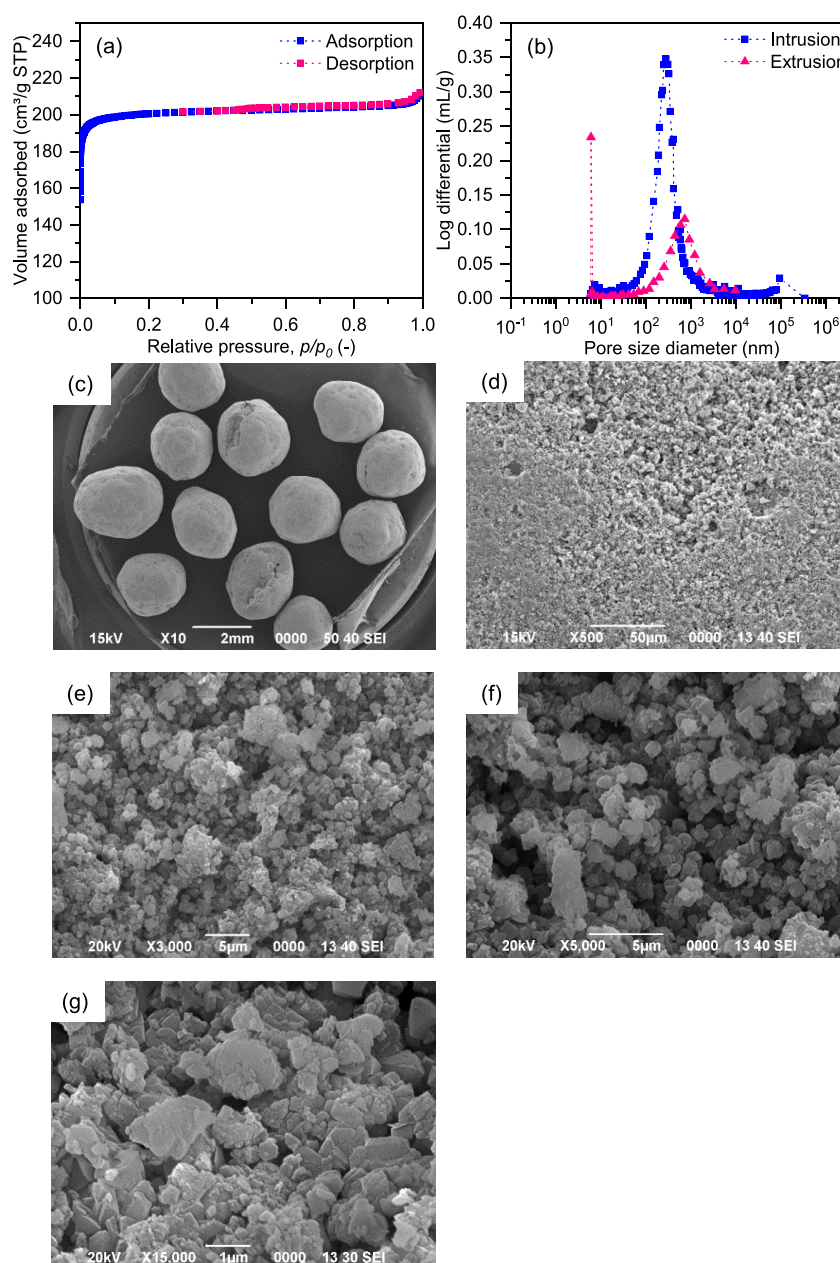
In the gas preparation section, the partial pressure of the adsorbable species was set-up before being introduced in the adsorption column. In the adsorption section, the mixture passes through the adsorption column that is placed inside a temperature-controlled oven. Mass flow controllers (Alicat MFCs, USA) were used to set-up the flow rates of both carrier gas (He) and adsorbate gases (CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub>), and an electronic back-pressure controller (Alicat BPR, USA) was used to establish the total pressure of the system. For single-component experiments, the column gas outlet goes directly to the TCD detector. For binary and ternary experiments, the column gas outlet passes through a six-port VICI-Valco valve gas trapping loop system. This valve was programmed to inject the mixture sample, trapped in the loop, into a gas chromatographic column (HayeSep packed column) at a fixed time step. The species were separated in less than 1 min and analyzed by the TCD-GC system. Before the first run, the adsorption column was activated for 12 h at 623 K under vacuum and pure helium flow (10 mL min<sup>−1</sup>) to remove any pre-absorbed undesirable components, such as water.

In chromatographic breakthrough experiments, the adsorption equilibrium concentration is calculated by integrating the molar flow profiles of the breakthrough curves by using the following equation:<sup>43</sup>

$$q_{\text{exp},i} = \frac{1}{m_{\text{ads}}} \left( F_{f,i} t_n - \int_0^{t_{\infty}} F_i dt - \varepsilon_b V_c C_{0i} \right) \quad (1)$$

where  $q_{\text{exp},i}$  is the experimental measured adsorption equilibrium concentration,  $m_{\text{ads}}$  is the adsorbent mass in the column,  $F_{f,i}$  is the feed molar flow rate of component  $i$  at the inlet of the fixed bed,  $F_i$  is the molar flow rate of component  $i$  at the outlet of the fixed bed,  $t_{\infty}$  is the saturation time,  $\varepsilon_b$  is the bed porosity,  $V_c$  is the adsorption column volume, and  $C_{0i}$  is the feed gas-phase concentration of component  $i$  at the inlet of the fixed bed.

**Adsorption Equilibrium Model.** The dual-site Langmuir (DSL) model isotherm distinguishes two categories of sorption



**Figure 1.** Characterizations: (a) adsorption equilibrium isotherm of N<sub>2</sub> at 77 K on binder-free zeolite KY; (b) differential intrusion and extrusion of Hg in pores on binder-free zeolite KY; SEM images of binder-free zeolite KY at (c) 10X, (d) 500X, (e) 3000X, (f) 5000X, and (g) 15,000X.

sites in the adsorbent, each following the Langmuir model assumption, with different binding energies and maximum adsorption capacities.<sup>43,44</sup> The extended DSL isotherm for a multicomponent system is

$$q_i = q_{m1,i} \frac{b_{1i} p_i}{1 + \sum_{i=1}^n b_{1i} p_i} + q_{m2,i} \frac{b_{2i} p_i}{1 + \sum_{i=1}^n b_{2i} p_i} \quad (2)$$

where  $q_i$  is the adsorbed equilibrium concentration,  $p_i$  is the partial pressure of sorbate, and  $q_{mi}$  and  $b_i$  are the maximum adsorbed equilibrium concentration and the adsorption affinity constant of each site, respectively. The subscripts 1 and 2 indicate the two types of sorption sites, the index  $i$  refers to the sorbate species, and  $n$  refers to the number of components present in the mixture. This model deviates from the ideal Langmuir model accounting for the heterogeneity of the adsorbent surface due to possible different adsorption site

locations on the faujasite framework. It reverts to the Langmuir model if considering only one equivalent energy site.

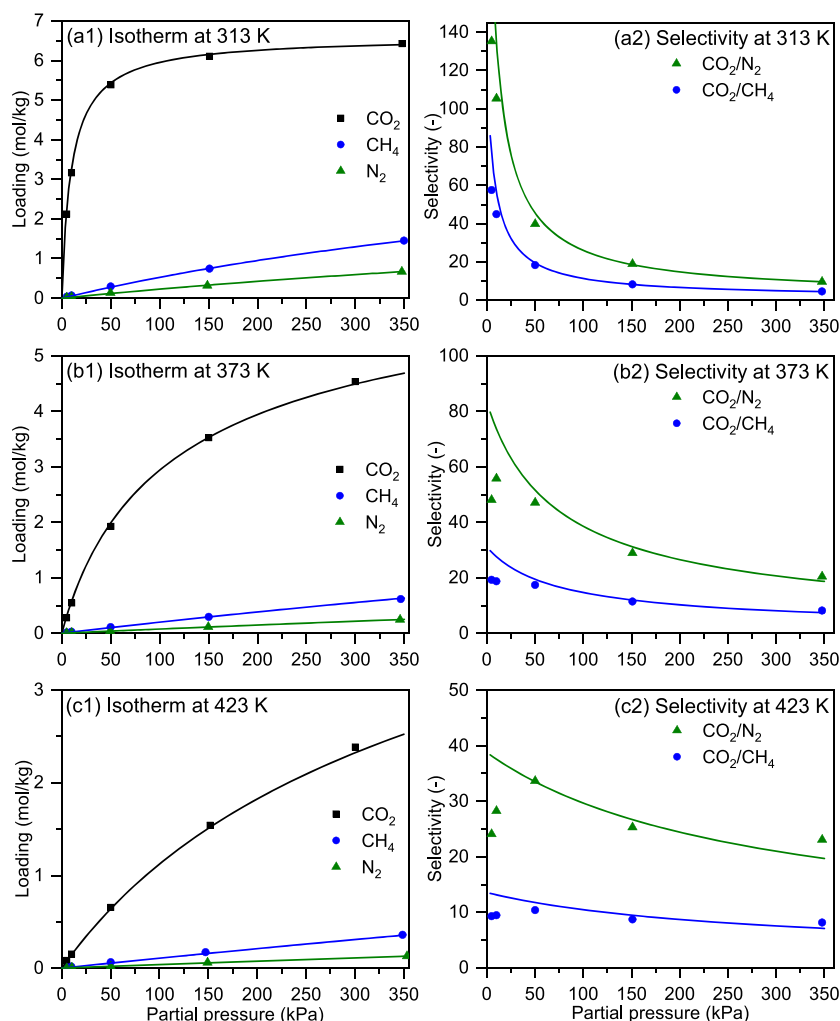
The effect of temperature on the adsorption affinity constant,  $b_i$ , follows a van't Hoff equation

$$b_i = b_{\infty,i} e^{(-\Delta H_i/RT)} \quad (3)$$

where  $b_{\infty,i}$  is the pre-exponential factor of the affinity constant,  $R$  is the ideal gas constant,  $(-\Delta H_i)$  is the heat of adsorption, and  $T$  is the temperature.

**Isosteric Heats.** The isosteric heat can give us an idea of the heterogeneity of the adsorption surface, and its dependence as a function of the adsorbed equilibrium concentration can give us an indication of the contribution of adsorbate–adsorbent interactions.<sup>35</sup> The isosteric heat ( $\Delta H_{st}$ ) as a function of the adsorbed equilibrium concentration is defined by the following equation<sup>45</sup>





**Figure 2.** Adsorption equilibrium isotherms of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> at (a1) 313, (b1) 373, and (c1) 423 K in binder-free zeolite KY; selectivity of CO<sub>2</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> at (a2) 313, (b2) 373, and (c2) 423 K in binder-free zeolite KY. Experimental = symbols; numerical = lines.

$$\frac{\Delta H_{st}}{RT^2} = -\left(\frac{\partial \ln p}{\partial T}\right)_q \quad (4)$$

Assuming that  $\Delta H_{st}$  is independent of the temperature, the isosteric heat can be calculated directly from the experimental adsorption isotherms by integrating eq 4 at a fixed coverage in a plot of  $\ln p$  against  $1/T$ <sup>31</sup>

$$\ln p = \text{constant} - \frac{\Delta H_{st}}{RT} \quad (5)$$

It can be also predicted or calculated numerically by the differentiation of the DSL adsorption isotherm (eq 2), assuming constant loading ( $dq = 0$ ) and substituting the result in the definition of isosteric heat equation (eq 4), resulting in the following equation<sup>41,43,46</sup>

$$(-\Delta H_{st}) = \frac{q_{m1} \frac{b_1 \Delta H_1}{(1+b_1 p)^2} + q_{m2} \frac{b_2 \Delta H_2}{(1+b_2 p)^2}}{q_{m1} \frac{b_1}{(1+b_1 p)^2} + q_{m2} \frac{b_2}{(1+b_2 p)^2}} \quad (6)$$

**Selectivity and Working Capacity.** The selectivity ( $\alpha$ ) of component  $i$  over component  $j$  can be defined as<sup>47,48</sup>

$$\alpha_{i,j} = \frac{q_i/q_j}{p_i/p_j} \quad (7)$$

where  $q_i$  and  $q_j$  are the adsorbed equilibrium concentration of components  $i$  and  $j$  at the same pressure and temperature, respectively.  $p_i$  and  $p_j$  are the respective partial pressures.

The working capacity of an adsorbent can be defined as the difference in the adsorption equilibrium concentration values between the high and low pressures in the case of PSA/VSA (at constant temperature) and from a high and low temperature in the case of TSA (at constant pressure). A general expression including both the temperature and pressure for the calculation of the working capacity is<sup>49</sup>

$$\beta_p = q(T_1, p_1) - q(T_2, p_2) \quad (8)$$

where  $q(T_1, p_1)$  is the adsorbed equilibrium concentration at the temperature  $T_1$  and partial pressure  $p_1$  in the adsorption step and  $q(T_2, p_2)$  is the adsorbed equilibrium concentration at temperature  $T_2$  and regenerating pressure  $p_2$  in the desorption step.

**Breakthrough Mathematical Modeling.** A mathematical model has been developed to predict the dynamic behavior of the fixed bed adsorption process for the single- and multicomponent breakthrough curves, which is described in

Table 1. Adsorption Equilibrium Model Parameters for Sorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> on Binder-Free Zeolite KY

species	$q_m$ (mol kg <sup>-1</sup> )		$b$ (kPa <sup>-1</sup> ) <sup>a</sup>		$(\Delta H_i)$ (kJ mol <sup>-1</sup> )		$R^2$
	$q_{m1}$	$q_{m2}$	$b_1$	$b_2$	$(\Delta H_i)_1$	$(\Delta H_i)_2$	
CO <sub>2</sub>	3.35	3.25	$6.27 \times 10^{-2}$	$1.62 \times 10^{-1}$	-45.0	-37.4	0.9990
CH <sub>4</sub>	4.81		$1.23 \times 10^{-3}$		-16.9		0.9994
N <sub>2</sub>	2.98		$8.30 \times 10^{-4}$		-18.7		0.9990

<sup>a</sup>The reference temperature used is 313 K.

Section S2 of the Supporting Information. Briefly, the mathematical model is based on the mass and energy conservation law principles including both the effect of the longitudinal axial dispersion of the flowing gas through the bed and an overall effective kinetic rate mechanism for mass transfer of the sorbates between the bulk gas phase and adsorbent particles (linear driving force model, LDF). The adsorption equilibrium isotherm is described by the DSL model. The resulting set of coupled partial and algebraic differential equations is summarized in Table S2, and the correlations used to estimate the mathematical model parameters are shown in Table S3.

## RESULTS AND DISCUSSION

**Adsorbent Properties and Characterization.** N<sub>2</sub> gas sorption measurements were performed to describe the porous nature of the binder-free zeolite KY studied. The corresponding adsorption and desorption isotherms at 77 K are shown in Figure 1a. It can be seen that the isotherms are of type I according to the new IUPAC classification,<sup>50</sup> being concave to the  $p/p_0$  axis with the loading reaching a limiting value, which is a signature characteristic of microporous materials. At the low-pressure region (between  $p/p_0 = 0.01$  and 0.10), the adsorbed amount increases from approximately 150 to 200 cm<sup>3</sup><sub>STP</sub>/g and then it practically remains constant until  $p/p_0 = 1$ . The textural properties of the material are summarized in Table S4.

The mercury (Hg) intrusion porosimetry outcomes are shown in Figure 1b, which are presented by differential intrusion/extrusion as a function of the pore size diameter. A pore size range is detected from nano- to micropore sizes (according to the new IUPAC scheme<sup>50</sup>) between 0.01 and 10 μm. The average pore size by extrusion is observed to be around 1 μm, indicating that most of the pores in the binder-free zeolite KY are considered to be between the size classes of sub- and intermicropores.

Scanning electron microscopy (SEM) images of the zeolite KY samples are presented in Figure 1c–g. Foggy crystals with an average size of around 1 μm with cubic/spherical characteristics can be observed in Figure 1f. However, in Figure 1g, it is possible to see the crystal intergrowth in the interior forming polycrystalline morphology, and a single zeolite crystal inside the beads is almost not perceptible. This behavior has already been observed<sup>51</sup> and was related to the manufacturing process of binder-free zeolite crystals.

**Adsorption Equilibrium of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> on Binder-Free Zeolite KY.** The single-component adsorption equilibrium data of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> on binder-free zeolite KY were collected at three temperatures, 313, 373, and 423 K, and for partial pressures up to 350 kPa directly from a series of fixed bed breakthrough experiments using eq 1. The experimental conditions for the single component breakthrough runs of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> are summarized in Table

S5. All the single-component breakthrough curves measured are depicted in Figures S2–S4.

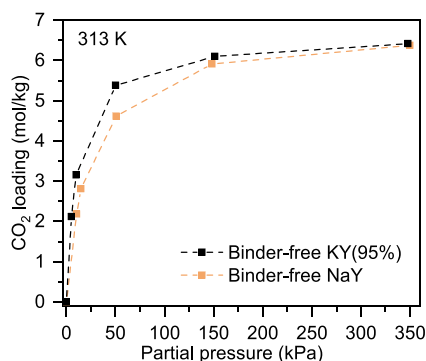
Figure 2a1–c1 shows the isotherms collected for CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> as well as the fitting with the standard Langmuir (for CH<sub>4</sub> and N<sub>2</sub>) and dual-site Langmuir (for CO<sub>2</sub>) models, at (a1) 313, (b1) 373, and (c1) 423 K. As can be seen, the amount adsorbed of all components increases by enhancing the partial pressure and decreases by enhancing the temperature. At 313 K and 350 kPa, the adsorbed equilibrium concentrations for CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> in binder-free zeolite KY are around 6.42, 1.45, and 0.671 mol kg<sup>-1</sup>, respectively. Regarding the CO<sub>2</sub> isotherms, it is clear that this guest molecule presents a much higher affinity with the binder-free zeolite KY than the other components, with this result being especially due to its large linear quadrupole moment and consequently strong interaction with the intracrystalline charge density framework.

Figure 2a2–c2 shows the numerical (eq 7) and experimental selectivities of CO<sub>2</sub> over N<sub>2</sub> (green) and CO<sub>2</sub> over CH<sub>4</sub> (blue) at the temperatures of (a2) 313, (b2) 373, and (c2) 423 K. At 313 K (Figure 2a2), it is visible that, at the interval of lower pressure from 5 to 10 kPa, the selectivity of CO<sub>2</sub> over N<sub>2</sub> is the highest ranging from 105 to 135. Under the same conditions, the selectivity of CO<sub>2</sub> over CH<sub>4</sub> is between 45 and 57. As the temperature increases, the selectivity of CO<sub>2</sub> over N<sub>2</sub> and CH<sub>4</sub> decreases as it does not exceed 29 and 10, respectively, at 423 K (Figure 2c2). At higher pressures from 150 to 350 kPa, the CO<sub>2</sub> selectivity over the other components generally becomes practically constant, as it is shown in Figure 2a2–c2. It is worth mentioning that, at the higher temperatures (373 and 423 K) and low pressures (below 50 kPa), CH<sub>4</sub> and N<sub>2</sub> concentration curves break through the column very fast (less than a minute), which can contribute to experimental errors in the measurement of the adsorption equilibrium experimental data (please see Figures S3 and S4 in the Supporting Information). Accordingly, this can lead to an under or over-measurement of the compounds adsorbed in equilibrium concentration, which results in the calculation of an unexpected lower experimental selectivity of CO<sub>2</sub> over N<sub>2</sub> and CH<sub>4</sub> at low pressure, as can be seen in Figure 2b2,c2.

Regarding the isotherm model fitting (lines in Figure 2a1–c1), the standard Langmuir model is reasonable to describe CH<sub>4</sub> and N<sub>2</sub> data because the adsorption binding sites in the surface can be considered practically homogeneous for the guest molecules. However, for the guest CO<sub>2</sub>, the DSL isotherm model is more appropriate because the adsorbent surface can be considered energetically heterogeneous due to the different cation site locations.<sup>35</sup> Table 1 summarizes the DSL and Langmuir isotherm parameters for the adsorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> in the binder-free zeolite KY as well as the respective fitting correlation coefficients. The extended dual-site Langmuir (DSL) model (eq 2) was used to fit the multicomponent data (binary and ternary adsorption equilibrium data), according to the approach presented by Ritter et

*al.*<sup>52</sup> and Tynan *et al.*<sup>53</sup> (details are given in Section S6 in the Supporting Information). From the fitting procedure, the values calculated for  $q_{mi}$  follow the order  $\text{CO}_2(6.60 \text{ mol kg}^{-1}) > \text{CH}_4(4.81 \text{ mol kg}^{-1}) > \text{N}_2(2.98 \text{ mol kg}^{-1})$ , giving rise to some thermodynamic inconsistency of the models. However, these values should be read as empirical values valid only for the proper description of experimental data by the simple DSL/Langmuir isotherm models in the range of temperature and pressure studied (extrapolation is not recommended). The same is true for the values of the adsorption affinity constant  $b_i$  reported in Table 1.

Figure 3 depicts the  $\text{CO}_2$  isotherms at 313 K in the binder-free ion-exchanged KY and in the as-synthesized NaY form



**Figure 3.** Comparison between the  $\text{CO}_2$  adsorption equilibrium isotherm at 313 K and up to 350 kPa obtained in the binder-free ion-exchanged KY(95%) (black) with the one in the binder-free beads of NaY (light orange) from where the ion exchange is performed. Experimental = symbols.

(from where the ion exchange had been performed), for a comparison. As can be observed, the loading of  $\text{CO}_2$  in the binder-free zeolite KY is higher up to 350 kPa. This result clearly indicates that the potassium ion exchange of Y zeolite enhances the amount adsorbed of  $\text{CO}_2$  at low partial pressure, as already shown/predicted by other authors.<sup>34,35</sup> At 313 K and below 150 kPa, the difference in the loadings of  $\text{CO}_2$  in the KY and NaY binder-free beads may reach up to  $0.77 \text{ mol kg}^{-1}$ , representing an increase of 16.6% in these conditions.

Figure S5a shows a comparison of the  $\text{CO}_2$  isotherm data collected in this work with the ones in LiY(73%), KY(100%), and CsY(89%) zeolites in powder form prepared by ion exchange of a parent NaY sample with a Si/Al ratio of 2.5.<sup>35</sup> The results show that the adsorption capacity of the binder-free KY studied in this work is also very competitive compared to most of the studied alkali metal exchanged zeolites. At 150 kPa and 323 K, the adsorption equilibrium concentration of  $\text{CO}_2$  in the binder-free KY is equal to  $5.89 \text{ mol kg}^{-1}$ , compared to 5.24 for NaY, 5.07 for KY, 4.45 for LiY, and  $2.98 \text{ mol kg}^{-1}$  for CsY (more details are provided in the Supporting Information Section S4). Another comparison with the powder form of KY zeolite is shown in Figure S5b for the  $\text{CO}_2$  isotherms at 333 K,<sup>35</sup> which has a comparable ion exchange degree, in the pressure range until 100 kPa. As can be seen, the loading of  $\text{CO}_2$  in the binder-free zeolite KY is systematically higher and follows a similar trend for this range of pressure.

The 13X zeolite reported by Hefti *et al.*<sup>34</sup> contains an adsorption inert binder (between 15 and 25%) that reduces its adsorption capacity. In this way, for the comparison of the 13X zeolite with the binder-free KY studied in this work, it was

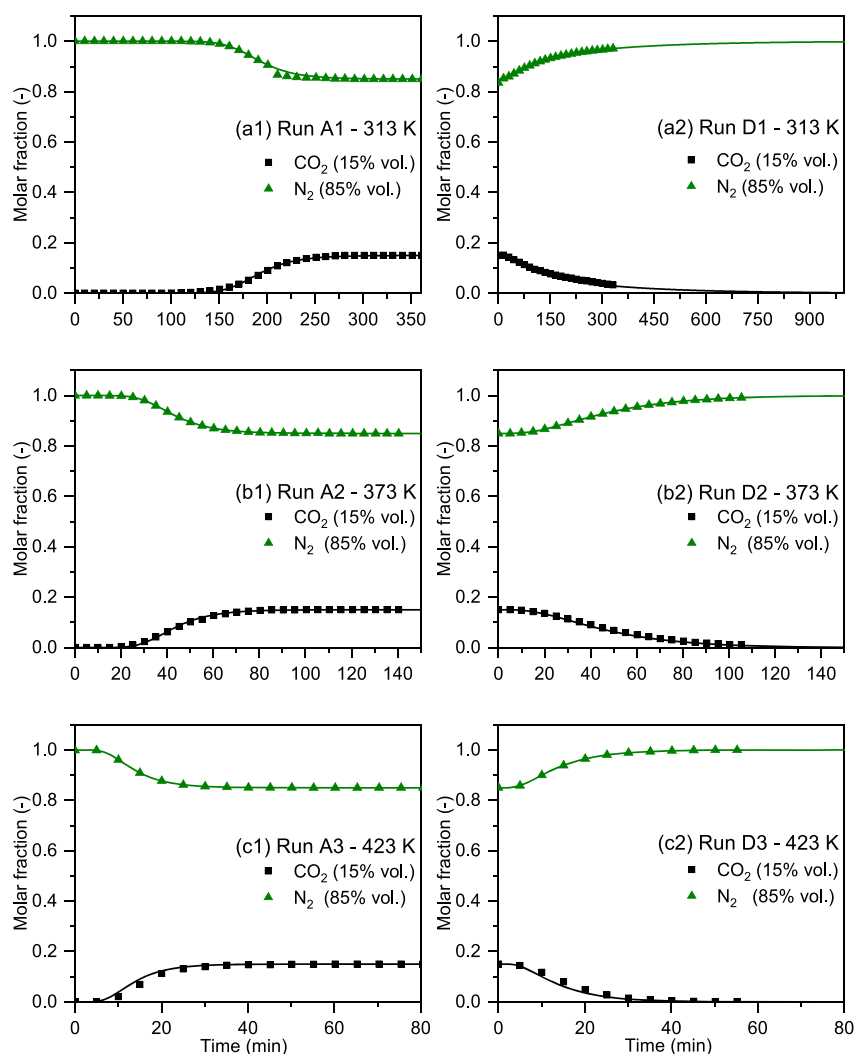
assumed that the 13X zeolite has a 15–25% higher capacity than the values reported by the authors. Accordingly, the amounts adsorbed of  $\text{CO}_2$  at 15 kPa and 298 K in the binder-free zeolite KY are 9.3 and 0.5% higher than in 13X zeolite, respectively.

The isosteric heats of adsorption are calculated from the adsorption equilibrium data using eq 4 (details are shown in Figure S6 for all the compounds). Figure S7 shows the numerical predicted isosteric heat (eq 6) along with the calculated experimental values as a function of coverage, where the DSL model predicts the experimental observation of a practically constant net isosteric heat for  $\text{CO}_2$ ,  $\text{CH}_4$ , and  $\text{N}_2$  as a function of coverage with values around 39.9, 16.9, and  $18.7 \text{ kJ mol}^{-1}$ , respectively. The isosteric heat for  $\text{N}_2$  is slightly higher than the one for  $\text{CH}_4$ , probably because it has also a quadrupole moment despite  $\text{CH}_4$ , which is an apolar molecule.

**Binary Adsorption for Mixtures  $\text{CO}_2/\text{N}_2$ .** Figure 4 shows the adsorption (a1–c1) and desorption (a2–c2) breakthrough curves for the mixture ( $\text{CO}_2/\text{N}_2$ :15/85) at 313, 373, and 423 K. The desorption step was performed with pure  $\text{N}_2$  at the same flow rate used in the adsorption step. The experimental conditions for these set of runs can be found in Table S6 in the Supporting Information.

As can be seen in Figure 4a1,  $\text{CO}_2$  starts to elute from the column at around 150 min with a mass transfer zone that reaches the inlet concentration (saturation of the bed) at around 250 min. The effect of temperature in the binary breakthrough curves  $\text{CO}_2/\text{N}_2$  is shown in Figure 4a1–c1, where it can be observed that the saturation time decreases with increasing temperature as expected (313–423 K). Regarding the desorption curves with pure  $\text{N}_2$  (Figure 4a2–c2), the time to clean the column is much higher than the time to saturate it, especially at 313 K (a2). This trend can be explained from the type I IUPAC classification of the isotherms, which are considered favorable for the adsorption and consequently unfavorable for desorption, resulting in a spreading of the mass transfer zone in the desorption step, which contributes to the longer time needed for the regeneration of the column. As the temperature increases from 313 to 423 K, the desorption time decreases from 1000 (numerical curve in Figure 4a2) to 40 min (Figure 4c2).

The working capacity for a TSA process, calculated between two different temperatures (313 and 423 K, eq 8) keeping the same feed conditions ( $\text{CO}_2/\text{N}_2$ :15/85 vol %) at constant 100 kPa, is equal to  $3.7 \text{ mol kg}^{-1}$ , which compares to  $3.3 \text{ mol kg}^{-1}$  observed in pellets of 13X zeolite<sup>48</sup> (we note that these pellets of 13X zeolite have an inert clay binder content that can reach up to 25% in weight according to Zeochem). Therefore, by using the binder-free zeolite KY, it is possible to achieve an increase in the working capacity for the TSA process up to 12.0%. The working capacity for a PSA process, calculated between two different partial pressures (15 and 3 kPa, eq 8) at a constant temperature of 298 K, is equal to  $2.4 \text{ mol kg}^{-1}$ , which compares to  $1.3 \text{ mol kg}^{-1}$  observed in pellets of 13X zeolite.<sup>48</sup> Therefore, by using the binder-free zeolite KY, it is possible to achieve an increase in working capacity for the PSA process up to 84.0%. These results show that the binder-free beads (ready to use for large-scale production) should be regarded as an important adsorbent material to be used to near atmospheric pressure for  $\text{CO}_2$  capture for TSA or PSA processes. However, further comprehensive experimental investigation needs to be performed to confirm the effectiveness of the binder-free KY applied for the cyclic



**Figure 4.** (a1, b1, c1) Adsorption (Run A) and (a2, b2, c2) desorption (Run D) breakthrough curves for CO<sub>2</sub> and N<sub>2</sub> on binder-free zeolite KY at 313, 373, and 423 K. Experimental = symbols; numerical = lines. Experimental conditions are summarized in Table S6 in the Supporting Information.

adsorption process for CO<sub>2</sub> post-combustion capture and biogas upgrading processes, but the results arising for this experimental study are very promising.

A comparison breakthrough study between experiments in the ion-exchanged binder-free KY and the as-synthesized NaY has been performed for the mixture CO<sub>2</sub>/N<sub>2</sub> (15/85 vol %) at 313 K and a total pressure of 100 kPa. The result is illustrated in Figure S8a where it is clear that CO<sub>2</sub> elutes earlier in the fixed bed column with binder-free NaY, which means that CO<sub>2</sub> selectivity is higher in the KY form. This result is in accordance with the literature<sup>34,35</sup> predictions proving the advantage of using the potassium form to increase CO<sub>2</sub> selectivity compared to the NaY faujasite form, especially for CO<sub>2</sub> capture from post-combustion streams.

Additionally, Table S12 in the Supporting Information shows a comparison of the calculated values of binder-free KY metrics along with other adsorbents such as zeolite 13X, activated carbon (CS-AC), UTSA-16, and Mg-MOF-74, under post-combustion capture conditions shown in the literature.<sup>48</sup>

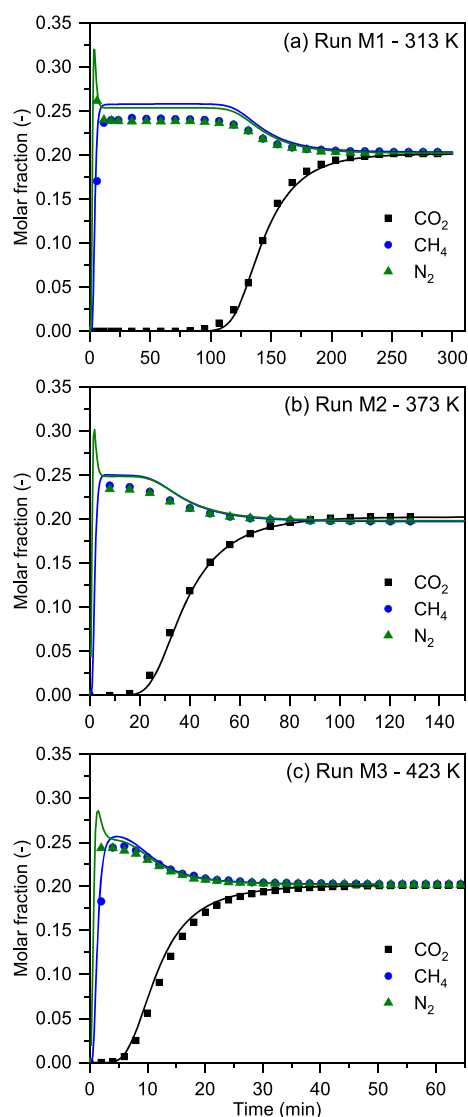
**Ternary Adsorption of Mixtures CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub>.** Figure 5 shows breakthrough curves for ternary mixture feeds of CO<sub>2</sub>/CH<sub>4</sub>/N<sub>2</sub> (20/20/20 vol % balanced with He) on binder-free zeolite KY at 100 kPa and (a) 313, (b) 373, and (c) 423 K,

under conditions typically used for biogas upgrading. As can be seen, the binder-free zeolite KY acts as an efficient separator of CO<sub>2</sub> from CH<sub>4</sub>/N<sub>2</sub>. CH<sub>4</sub> and N<sub>2</sub> practically elute from the column at the beginning of the experiments. Additionally, the ternary breakthrough curves exhibit the so-called roll-up phenomenon,<sup>55</sup> where the least adsorbed solutes (following the hierarchy order N<sub>2</sub> < CH<sub>4</sub> < CO<sub>2</sub>) are desorbed by the more strongly adsorbed ones by an adsorption equilibrium competition displacement process. This phenomenon makes the concentration of the least adsorbed components (moving faster in the column: CH<sub>4</sub> and N<sub>2</sub>) overcome the feed concentration until the strongest adsorbed component (moving slower in the column: CO<sub>2</sub>) starts to elute the column, as is clearly shown in Figure 5.

Table S7 in the Supporting Information shows the experimental conditions for the runs involving the ternary mixture.

Similar to the binary experiments, values of the adsorption capacity, selectivity, and working capacity were determined for the experiments at 100 kPa. At 313 K, the selectivities of CO<sub>2</sub> over CH<sub>4</sub> are around 19 and 45 over N<sub>2</sub>. The working capacity was predicted between 313 and 423 K while keeping the same feed conditions, where the value is equal to 4.0 mol kg<sup>-1</sup>.





**Figure 5.** Ternary adsorption breakthrough curves for  $\text{CO}_2/\text{CH}_4/\text{N}_2$  on binder-free zeolite KY at (a) 313, (b) 373, and (c) 423 K. Experimental = symbols; numerical = lines. Experimental conditions are summarized in Table S7 in the Supporting Information.

These results indicate also an efficient separation of  $\text{CO}_2$  from the  $\text{CO}_2/\text{CH}_4/\text{N}_2$  ternary mixture.

Also, a comparison study between breakthrough experiments in the ion-exchanged binder-free KY and the as-synthesized NaY has been performed for the mixture  $\text{CO}_2/\text{CH}_4/\text{N}_2$  (20/20/20 vol % balanced with He) at 313 K and 100 kPa. Once more, in Figure S8b, it is possible to observe that  $\text{CO}_2$  breaks through the column earlier in the bed containing binder-free NaY, proving once more the advantage of using the potassium form to increase  $\text{CO}_2$  selectivity, also under biogas upgrading conditions.

To verify the lifetime/recyclability of the binder-free zeolite KY, at the end of the single and multicomponent experiments, five  $\text{CO}_2$  breakthrough experiments were repeated at the experimental conditions of RUN 1.3 (50 kPa and 313 K). After each run, the material was cleaned at 473 K with a pure He stream ( $80 \text{ mL min}^{-1}$ ) for at least 2 h. Table S14 summarizes the experimental conditions for these runs. Figure S9a illustrates the  $\text{CO}_2$  breakthrough curves plotted in terms of the normalized molar fraction ( $y_i/y_{i0}$ ) as a function of moles

fed per unit mass of the adsorbent, and Figure S9b shows the loadings of  $\text{CO}_2$  calculated for each run. It can be observed that the calculated  $\text{CO}_2$  loadings for all runs are almost identical (c.a.  $5.37 \text{ mol kg}^{-1}$ ), which confirms that the material can be regenerated and reused several times without capacity lost.

**Modeling of Binary and Ternary Breakthrough Data  $\text{CO}_2/\text{CH}_4/\text{N}_2$ .** The modeling of breakthrough curves is important to understand physically the overall fixed bed adsorption experimental dynamics for thereafter design cyclic adsorption processes. Accordingly, the fixed bed adsorption model (shown in Table S2 in the Supporting Information) was used to simulate/predict the binary and ternary breakthrough experimental data.<sup>41,56</sup>

The spreading of mass transfer zones in a fixed bed is influenced mainly by (i) the nature of adsorption equilibrium (favorable or unfavorable), (ii) mass transfer of sorbates between the bulk gas phase and the interior of the porous particles, and (iii) the flow pattern of the gas in the fixed bed, which can be characterized by an axial dispersion model. Accordingly, it is important to evaluate the relative importance of each type of mechanism on the overall dynamics and respective influence in the spreading of mass transfer zones of the breakthrough curves.

Concerning the adsorption equilibrium, the isotherms are all type I (favorable for adsorption), so their effect is to narrow the length of the mass transfer zone. The mass transfer kinetics mechanism analysis of the adsorbable species from the bulk gas phase to the interior of the adsorbent can be very complex, but generally, it can be simplified by the so-called linear driving force model (LDF).<sup>57,58</sup> In this approach, a lumped parameter called the overall mass transfer coefficient,  $K_{\text{LDF}}$ , can be related to the several possible resistances to mass transfer in a bidisperse porous adsorbent such as film diffusion, macropore diffusion, and micropore diffusion, linked by the following equation, which takes into account the relative importance of each mechanism based on the respective time constants

$$\frac{1}{K_{\text{LDF}}} = \frac{R_p}{3k_f} + \frac{R_p^2}{15\epsilon_p D_p} + \frac{r_c^2}{15KD_c} \quad (9)$$

where  $K$  is the dimensionless Henry's law equilibrium constant,  $R_p$  is the particle (bead) radius,  $\epsilon_p$  is the particle porosity,  $D_p$  is the effective macropore diffusivity,  $r_c$  is the zeolite crystal radius (from where the beads were made), and  $D_c$  is the intracrystalline/framework zeolite diffusivity.

Ruthven<sup>31</sup> used the method of moments for a linear system to evaluate also the relative importance of the axial dispersion of the gas flowing through the bed relatively to the mass-transfer resistances (eq 9) providing an overall effective rate coefficient  $k'$ , given by the following equation

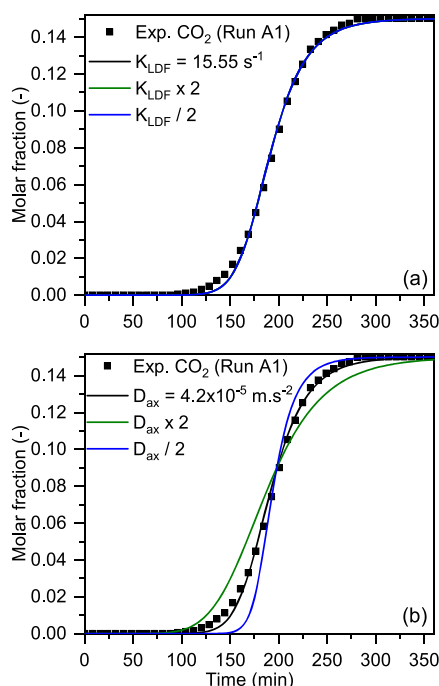
$$\frac{1}{k'K} = \frac{D_{\text{ax}}}{v_i^2} \left( \frac{1 - \epsilon_b}{\epsilon_b} \right) + \frac{R_p}{3k_f} + \frac{R_p^2}{15\epsilon_p D_p} + \frac{r_c^2}{15KD_c} \quad (10)$$

where  $k'$  is the overall effective rate coefficient,  $D_{\text{ax}}$  is the axial dispersion of the gas in the bed,  $v_i$  is the interstitial velocity, and  $\epsilon_b$  is the bed porosity.

By comparing the relative values of the time constants of each mechanism (terms of the r.h.s. in eq 10), it is possible to evaluate roughly which is the relevant one that influences the spreading of the mass transfer zones of the breakthrough curves. Table S3 in the Supporting Information summarizes



the correlations used to predict the values of each parameter of the l.h.s. of eq 9 and r.h.s. of eq 10, and Tables S8 and S9 in the Supporting Information summarize the values calculated for each term of eqs 9 and 10 for the binary ( $\text{CO}_2/\text{N}_2$ ) and ternary ( $\text{CO}_2/\text{CH}_4/\text{N}_2$ ) experiments at 313, 373, and 423 K, respectively. For the binary experiments (Table S8), we can read that the values of the term related to axial dispersion vary from 1.81 to 2.75 s being much higher than the reverse of the overall mass-transfer coefficient  $K_{\text{LDF}}$ , which varies from 0.04 to 0.06 s, indicating that the axial dispersion of the flowing gas through the bed will have a significant influence on the length of the mass transfer zones of the experimental breakthrough curves studied in this work. Similarly, for the ternary experiments, the same behavior is observed (Table S9). This is demonstrated in Figure 6a where a selected binary



**Figure 6.** Influence of changing overall mass transfer coefficient  $K_{\text{LDF}}$  (a) and axial dispersion  $D_{\text{ax}}$  (b) on the numerical breakthrough curves of  $\text{CO}_2$  at 313 K and 0.15 bar partial pressure balanced with  $\text{N}_2$  (Run A1, see Tables S6 and S8 in the Supporting Information for experimental conditions and model parameters, respectively). Experimental = symbols; numerical = lines.

experiment (Run A1) is simulated by changing the values of the overall mass-transfer coefficient ( $K_{\text{LDF}}$ ) for a fixed value of  $D_{\text{ax}}$ . It can be observed in Figure 6a that there is no effect in the spreading of the breakthrough curves. On the contrary, Figure 6b shows that the spread of the mass transfer zone of the breakthrough curves is strongly affected by changing the values of the axial dispersion ( $D_{\text{ax}}$ ) for a constant value of  $K_{\text{LDF}}$ . This parametric study clearly shows that the spreading of the breakthrough curves is completely dominated by the axial dispersion, a result confirmed by the values of each term of eq 10, as shown in Tables S8 and S9 in the Supporting Information.

Overall, the numerical simulations (lines in Figures 4 and 5) describe with good accuracy the dynamics of the fixed bed adsorption system for both the adsorption and desorption steps, in binary and ternary experiments, being the

mathematical model that developed a valuable tool for the design and prediction of the cyclic operation of industrial processes (PSA and TSA) using binder-free zeolite beads of KY for post-combustion and biogas upgrading processes.

Finally, we should remark that the previously described methodology for calculating model parameters to be used as a predictive tool is based on the assumption that the interior of the binder-free beads is made with very well-identified single crystals (as in typical commercial binder pellets/beads) with a size of around 1  $\mu\text{m}$  from where they were synthesized and also on framework/crystal diffusivities ( $D_c$ ) calculated from molecular dynamics simulations (MDS) and the experimental quasi-elastic neutron scattering (QENS) technique<sup>59,60</sup> (a microscopic experimental technique where the values of  $D_c$  are generally much higher than the ones measured by the macroscopic ones<sup>61</sup>). Accordingly, very small values for the micropore diffusion time constant term  $r_c^2/(15KD_c)$  in eqs 9 and 10 (values given in Tables S8 and S9 in the Supporting Information) are obtained, and consequently, the micropore diffusion resistance mechanism effect is negligible for the value of the global mass transfer coefficient. However, the manufacture of mechanically stable binder-free beads is a complex process,<sup>51</sup> where in the end, the interior of the binder-free beads is made of random-sized polycrystals, as can be observed in the SEM photographs shown in Figure 1f. Accordingly, in practice, the value of the crystal size ( $r_c$ ) to be used in eqs 9 and 10 is indeed very difficult to select. This means also that, in eqs 9 and 10, we should correctly write an average  $\langle r_c \rangle$  for the polycrystals observed in Figure 1f, where the true value is unknown, and the value of  $D_c$  could be also different from the one measured by MDS, QENS, or even NMR. This particularity can significantly affect the relative importance of micropore versus macropore diffusion in these bidisperse binder-free adsorbents, or we can assume that we have an unknown rate mechanism in the binder-free beads<sup>62</sup> due to the presence of polycrystals. However, for the present system studied, since the gas flow through the fixed bed is very small, we believe that the system is with no doubt dominated by the effect of the longitudinal degree of backmixing of the gas flow pattern through the fixed bed quantified by the axial dispersion coefficient ( $D_{\text{ax}}$ ) from where the respective time constant term and respective value in eq 10 (ranging from 1.81 to 2.75 s) superimpose largely to the importance of the global mass transfer coefficient ( $K_{\text{LDF}}$ ) (values ranging from 0.04 to 0.06 s), as demonstrated in Tables S8 and S9, and globally shown by the goodness of the fits of the simulated breakthrough curves presented in Figures 4 and 5.

## CONCLUSIONS

This work presents a systematic study of new potassium-exchanged binder-free beads of Y zeolite for the fixed bed adsorption of  $\text{CO}_2$ ,  $\text{CH}_4$ , and  $\text{N}_2$  and their mixtures, with interest for  $\text{CO}_2$  post-combustion capture and biogas upgrading strategies. It was demonstrated experimentally, from binary/ternary breakthrough curves, that this new binder-free zeolite KY (ready to be used and scaled up for large production) separates with a very high selectivity  $\text{CO}_2$  from mixtures containing  $\text{CO}_2/\text{CH}_4/\text{N}_2$  and enhances the  $\text{CO}_2$  adsorption uptake at 15 kPa up to 10% regarding commercial 13X (NaX) zeolite beads in the presence of  $\text{N}_2$ . The selectivity of  $\text{CO}_2$  over  $\text{N}_2$ , from post-combustion streams conditions, is around 104 at 298 K, and the selectivities of  $\text{CO}_2$  over  $\text{CH}_4$  and  $\text{N}_2$  in the ternary system are around 14 and 32 at

313 K, respectively. The experimental data have been modeled through a suitable mathematical model that provides a good description of the overall breakthrough data, being a useful tool for the design of cyclic adsorption processes using the new binder-free beads.

## ■ ASSOCIATED CONTENT

### ■ Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.iecr.1c02261>.

Effect of zeolite structural characteristics and ion exchange on CO<sub>2</sub> adsorption; mathematical modeling of single- and multicomponent fixed bed breakthrough curves; conversion from molecules/UC into mol kg<sup>-1</sup>; comparison of CO<sub>2</sub> adsorption equilibrium data in different ion-exchanged zeolites; comparison of adsorbent metrics with different zeolites under flue gas conditions; experimental conditions for single, binary, and ternary experiments; and multicomponent equilibria prediction (PDF)

## ■ AUTHOR INFORMATION

### Corresponding Authors

Lucas F.A.S. Zafanelli — Centro de Investigação de Montanha (CIMO), Instituto Politécnico de Bragança, 5300-253 Bragança, Portugal; Laboratory of Separation and Reaction Engineering (LSRE), Associate Laboratory LSRE/LCM, Department of Chemical Engineering, Faculty of Engineering, University of Porto, 4099-002 Porto, Portugal; [orcid.org/0000-0001-5187-2042](https://orcid.org/0000-0001-5187-2042); Email: [zafanelli@ipb.pt](mailto:zafanelli@ipb.pt)

José A.C. Silva — Centro de Investigação de Montanha (CIMO), Instituto Politécnico de Bragança, 5300-253 Bragança, Portugal; [orcid.org/0000-0003-1778-3833](https://orcid.org/0000-0003-1778-3833); Email: [jsilva@ipb.pt](mailto:jsilva@ipb.pt)

### Authors

Ezzeldin Aly — Centro de Investigação de Montanha (CIMO), Instituto Politécnico de Bragança, 5300-253 Bragança, Portugal; [orcid.org/0000-0003-4840-2597](https://orcid.org/0000-0003-4840-2597)

Adriano Henrique — Centro de Investigação de Montanha (CIMO), Instituto Politécnico de Bragança, 5300-253 Bragança, Portugal; Laboratory of Separation and Reaction Engineering (LSRE), Associate Laboratory LSRE/LCM, Department of Chemical Engineering, Faculty of Engineering, University of Porto, 4099-002 Porto, Portugal; [orcid.org/0000-0002-5227-9790](https://orcid.org/0000-0002-5227-9790)

Marcella Golini Pires — Centro de Investigação de Montanha (CIMO), Instituto Politécnico de Bragança, 5300-253 Bragança, Portugal

Alirio E. Rodrigues — Laboratory of Separation and Reaction Engineering (LSRE), Associate Laboratory LSRE/LCM, Department of Chemical Engineering, Faculty of Engineering, University of Porto, 4099-002 Porto, Portugal; [orcid.org/0000-0002-0715-4761](https://orcid.org/0000-0002-0715-4761)

Kristin Gleichmann — Chemiewerk Bad Köstritz GmbH, 07586 Bad Köstritz, Germany

Complete contact information is available at:

<https://pubs.acs.org/doi/10.1021/acs.iecr.1c02261>

### Notes

The authors declare no competing financial interest.

## ■ ACKNOWLEDGMENTS

The authors thank the Foundation for Science and Technology (FCT, Portugal) and ERDF under Programme PT2020 to CIMO (UID/AGR/00690/2019) and POCI-01-0145-FEDER006984-Associate Laboratory LSRE-LCM. The authors also thank the Foundation for Science and Technology (FCT, Portugal) under Programme PTDC 2020 \* 3599-PPCDTI \* Engenharia dos Processos Químicos \* project PTDC/EQU-EPQ/0467/2020. Last, the authors thank the Foundation for Science and Technology (FCT, Portugal) through the individual research grants SFRH/BD/148525/2019 for A.H. and DFA/BD/7925/2020 for L.F.A.S.Z.

## ■ NOMENCLATURE

$a_p$	specific area of the pellet (m <sup>-1</sup> )
$a_c$	specific area of the column (m <sup>-1</sup> )
$b_i$	adsorption equilibrium affinity constant of component $i$ (Pa <sup>-1</sup> )
$b_\infty$	pre-exponential factor of the affinity constant (Pa <sup>-1</sup> )
$C$	total gas concentration (mol m <sup>-3</sup> )
$C_{0i}$	feed gas-phase concentration at the inlet of the fixed bed (mol m <sup>-3</sup> )
$C_{pg}$	heat capacity of gas (J mol <sup>-1</sup> K <sup>-1</sup> )
$C_{ps}$	heat capacity of the adsorbent (J mol <sup>-1</sup> K <sup>-1</sup> )
$d_p$	bead diameter (m)
$d_c$	column diameter (m)
$D_{ax}$	axial mass dispersion coefficient (m <sup>2</sup> s <sup>-1</sup> )
$D_c$	intracrystalline diffusivity (m <sup>2</sup> s <sup>-1</sup> )
$D_k$	Knudsen diffusivity (m <sup>2</sup> s <sup>-1</sup> )
$D_m$	molecular diffusivity (m <sup>2</sup> s <sup>-1</sup> )
$D_p$	effective macropore diffusivity (m <sup>2</sup> s <sup>-1</sup> )
$F_{i,i}$	feed molar flow rate of component $i$ at the inlet of the bed (mol m <sup>-2</sup> s <sup>-1</sup> )
$F_i$	feed molar flow rate of component $i$ at the outlet of the bed (mol m <sup>-2</sup> s <sup>-1</sup> )
$h_p$	film heat transfer coefficient (W m <sup>-2</sup> K <sup>-1</sup> )
$h_w$	wall heat transfer coefficient (W m <sup>-2</sup> K <sup>-1</sup> )
$k'$	overall effective rate coefficient (s <sup>-1</sup> )
$K$	dimensionless Henry's law equilibrium constant (—)
$K_{LDF}$	linear driving force coefficient (s <sup>-1</sup> )
$K_{ax}$	effective axial bed thermal conductivity (W m <sup>-1</sup> K <sup>-1</sup> )
$L$	length of the column (m)
$Nu$	Nusselt number
$p_i$	partial pressure of component $i$ (Pa)
$P$	total pressure of the column (Pa)
$Pe$	Peclet number
$q_i$	adsorption concentration of component $i$ (mol kg <sup>-1</sup> )
$\bar{q}_i$	average adsorption concentration of component $i$ (mol kg <sup>-1</sup> )
$q_{cal}$	calculated adsorption concentration (mol kg <sup>-1</sup> )
$\bar{q}_{cal}$	average adsorption concentration (mol kg <sup>-1</sup> )
$q_m$	maximum adsorption equilibrium concentration (mol kg <sup>-1</sup> )
$r_p$	pore radius (Å)
$r_c$	crystal radius (m)
$R_p$	pellet radius (m)
$R$	universal gas constant (J mol <sup>-1</sup> K <sup>-1</sup> )
$Re$	Reynolds number
$S_{BET}$	BET surface area (m <sup>2</sup> g <sup>-1</sup> )
$S_{ext}$	external surface area (m <sup>2</sup> g <sup>-1</sup> )
$S_{Langmuir}$	Langmuir surface area (m <sup>2</sup> g <sup>-1</sup> )
$S_{mic}$	micropore surface area (m <sup>2</sup> g <sup>-1</sup> )

$t$	time (s)
$t_n$	saturation time (s)
$T$	temperature in the bulk gas phase (K)
$T_s$	temperature in the solid phase (K)
$T_w$	column wall temperature (K)
$v$	superficial velocity ( $\text{m s}^{-1}$ )
$v_i$	interstitial velocity ( $\text{m s}^{-1}$ )
$V_c$	column volume ( $\text{m}^3$ )
$V_{\text{mic}}$	micropore volume ( $\text{mm}^3 \text{ g}^{-1}$ )
$V_{\text{Total}}$	total pore volume ( $\text{mm}^3 \text{ g}^{-1}$ )
$V_{\text{mic}}$	average pore width (nm)
$y_i$	molar fraction of sorbate species $i$ in the bulk phase
$y_{i0}$	feed molar fraction of sorbate species $i$ in the bulk phase
$z$	axial coordinate in bed (m)

## GREEK LETTERS

$\alpha_p$	pure component selectivity (-)
$\alpha_c$	competitive component selectivity (-)
$\beta_p$	pure working capacity ( $\text{mol kg}^{-1}$ )
$\beta_c$	competitive working capacity ( $\text{mol kg}^{-1}$ )
$\Delta H_i$	isosteric heat adsorption of species $i$ ( $\text{J mol}^{-1}$ )
$\varepsilon_b$	bed porosity
$\varepsilon_p$	solid porosity
$\rho_s$	apparent adsorbent density ( $\text{kg m}^{-3}$ )
$\tau$	tortuosity
$\theta$	$=q/q_m$

## REFERENCES

- Gabrielli, P.; Gazzani, M.; Mazzotti, M. The Role of Carbon Capture and Utilization, Carbon Capture and Storage, and Biomass to Enable a Net-Zero- $\text{CO}_2$  Emissions Chemical Industry. *Ind. Eng. Chem. Res.* **2020**, *59*, 7033–7045.
- Jiménez, V.; Ramírez-Lucas, A.; Díaz, J. A.; Sánchez, P.; Romero, A.  $\text{CO}_2$  Capture in Different Carbon Materials. *Environ. Sci. Technol.* **2012**, *46*, 7407–7414.
- D'Alessandro, D. M.; Smit, B.; Long, J. R. Carbon Dioxide Capture: Prospects for New Materials. *Angew. Chem. Int. Ed.* **2010**, *49*, 6058–6082.
- Stuckert, N. R.; Yang, R. T.  $\text{CO}_2$  Capture from the Atmosphere and Simultaneous Concentration Using Zeolites and Amine-Grafted SBA-15. *Environ. Sci. Technol.* **2011**, *45*, 10257–10264.
- Zhao, Y.; Shen, Y.; Ma, G.; Hao, R. Adsorption Separation of Carbon Dioxide from Flue Gas by a Molecularly Imprinted Adsorbent. *Environ. Sci. Technol.* **2014**, *48*, 1601–1608.
- Yucel, H.; Ruthven, D. M. Diffusion in 5A Zeolite. Study of the Effect of Crystal Size. *J. Chem. Soc. Faraday Trans. 1 Phys. Chem. Condens. Phases* **1980**, *76*, 71.
- Espinal, L.; Poster, D. L.; Wong-Ng, W.; Allen, A. J.; Green, M. L. Measurement, Standards, and Data Needs for  $\text{CO}_2$  Capture Materials: A Critical Review. *Environ. Sci. Technol.* **2013**, *47*, 11960–11975.
- Bui, M.; Adjiman, C. S.; Bardow, A.; Anthony, E. J.; Boston, A.; Brown, S.; Fennell, P. S.; Fuss, S.; Galindo, A.; Hackett, L. A.; Hallett, J. P.; Herzog, H. J.; Jackson, G.; Kemper, J.; Krevor, S.; Maitland, G. C.; Matuszewski, M.; Metcalfe, I. S.; Petit, C.; Puxty, G.; Reimer, J.; Reiner, D. M.; Rubin, E. S.; Scott, S. A.; Shah, N.; Smit, B.; Trusler, J. P. M.; Webley, P.; Wilcox, J.; Mac Dowell, N. Carbon Capture and Storage (CCS): The Way Forward. *Energy Environ. Sci.* **2018**, *11*, 1062–1176.
- Al-Mamoori, A.; Krishnamurthy, A.; Rownaghi, A. A.; Rezaei, F. Carbon Capture and Utilization Update. *Energy Technol.* **2017**, *5*, 834–849.
- Xiao, G.; Xiao, P.; Hoadley, A.; Webley, P. Integrated Adsorption and Absorption Process for Post-Combustion  $\text{CO}_2$  Capture. *Front. Chem. Sci. Eng.* **2021**, *15*, 483–492.
- Wang, M.; Lawal, A.; Stephenson, P.; Sidders, J.; Ramshaw, C. Post-Combustion  $\text{CO}_2$  Capture with Chemical Absorption: A State-of-the-Art Review. *Chem. Eng. Res. Des.* **2011**, *89*, 1609–1624.
- Dantas, T. L.; Rodrigues, A. E.; Moreira, R. F. P. M. Separation of Carbon Dioxide from Flue Gas Using Adsorption on Porous Solids. In *Greenhouse Gases - Capturing, Utilization and Reduction*; InTech: 2012, DOI: 10.5772/31917.
- Jiang, K.; Feron, P.; Cousins, A.; Zhai, R.; Li, K. Achieving Zero/Negative-Emissions Coal-Fired Power Plants Using Amine-Based Postcombustion  $\text{CO}_2$  Capture Technology and Biomass Cocombustion. *Environ. Sci. Technol.* **2020**, *54*, 2429–2438.
- Lee, S.-Y.; Park, S.-J. A Review on Solid Adsorbents for Carbon Dioxide Capture. *J. Ind. Eng. Chem.* **2015**, *23*, 1–11.
- Bhown, A. S.; Freeman, B. C. Analysis and Status of Post-Combustion Carbon Dioxide Capture Technologies. *Environ. Sci. Technol.* **2011**, *45*, 8624–8632.
- Sircar, S. Separation of Methane and Carbon Dioxide Gas Mixtures by Pressure Swing Adsorption. *Sep. Sci. Technol.* **1988**, *23*, 519–529.
- Bari, S. Effect of Carbon Dioxide on the Performance of Biogas/Diesel Dual-Fuel Engine. *Renewable Energy* **1996**, *9*, 1007–1010.
- Yousef, A. M. I.; Eldrainy, Y. A.; El-Maghlany, W. M.; Attia, A. Upgrading Biogas by a Low-Temperature  $\text{CO}_2$  Removal Technique. *Alexandria Eng. J.* **2016**, *55*, 1143–1150.
- Ghoufi, A.; Gaberova, L.; Rouquerol, J.; Vincent, D.; Llewellyn, P. L.; Maurin, G. Adsorption of  $\text{CO}_2$ ,  $\text{CH}_4$  and Their Binary Mixture in Faujasite NaY: A Combination of Molecular Simulations with Gravimetry–Manometry and Microcalorimetry Measurements. *Microporous Mesoporous Mater.* **2009**, *119*, 117–128.
- Shen, X.; Yan, F.; Li, C.; Qu, F.; Wang, Y.; Zhang, Z. Biogas Upgrading via Cyclic  $\text{CO}_2$  Adsorption: Application of Highly Regenerable PEI@nano- $\text{Al}_2\text{O}_3$  Adsorbents with Anti-Urea Properties. *Environ. Sci. Technol.* **2021**, *55*, 5236–5247.
- Cavenati, S.; Grande, C. A.; Rodrigues, A. E. Layered Pressure Swing Adsorption for Methane Recovery from  $\text{CH}_4/\text{CO}_2/\text{N}_2$  Streams. *Adsorption* **2005**, *11*, 549–554.
- Mulgundmath, V. P.; Tezel, F. H.; Saatcioglu, T.; Golden, T. C. Adsorption and Separation of  $\text{CO}_2/\text{N}_2$  and  $\text{CO}_2/\text{CH}_4$  by 13X Zeolite. *Can. J. Chem. Eng.* **2012**, *90*, 730–738.
- Sun, Q.; Li, H.; Yan, J.; Liu, L.; Yu, Z.; Yu, X. Selection of Appropriate Biogas Upgrading Technology—a Review of Biogas Cleaning, Upgrading and Utilisation. *Renewable Sustainable Energy Rev.* **2015**, *51*, 521–532.
- Silva, J. A. C.; Schumann, K.; Rodrigues, A. E. Sorption and Kinetics of  $\text{CO}_2$  and  $\text{CH}_4$  in Binderless Beads of 13X Zeolite. *Microporous Mesoporous Mater.* **2012**, *158*, 219–228.
- Silva, J. A. C.; Ferreira, A.; Mendes, P. A. P.; Cunha, A. F.; Gleichmann, K.; Rodrigues, A. E. Adsorption Equilibrium and Dynamics of Fixed Bed Adsorption of  $\text{CH}_4/\text{N}_2$  in Binderless Beads of 5A Zeolite. *Ind. Eng. Chem. Res.* **2015**, *54*, 6390–6399.
- Silva, J. A. C.; Cunha, A. F.; Schumann, K.; Rodrigues, A. E. Binary Adsorption of  $\text{CO}_2/\text{CH}_4$  in Binderless Beads of 13X Zeolite. *Microporous Mesoporous Mater.* **2014**, *187*, 100–107.
- Burns, T. D.; Pai, K. N.; Subraveti, S. G.; Collins, S. P.; Krykunov, M.; Rajendran, A.; Woo, T. K. Prediction of MOF Performance in Vacuum Swing Adsorption Systems for Postcombustion  $\text{CO}_2$  Capture Based on Integrated Molecular Simulations, Process Optimizations, and Machine Learning Models. *Environ. Sci. Technol.* **2020**, *54*, 4536–4544.
- Mohr, R. J.; Vorkapic, D.; Rao, M. B.; Sircar, S. Pure and Binary Gas Adsorption Equilibria and Kinetics of Methane and Nitrogen on 4A Zeolite by Isotope Exchange Technique. *Adsorption* **1999**, *5*, 145–158.
- Ahn, H.; Moon, J. H.; Hyun, S. H.; Lee, C. H. Diffusion Mechanism of Carbon Dioxide in Zeolite 4A and CaX Pellets. *Adsorption* **2004**, *10*, 111–128.
- Seabra, R.; Ribeiro, A. M.; Gleichmann, K.; Ferreira, A. F. P.; Rodrigues, A. E. Adsorption Equilibrium and Kinetics of Carbon



Dioxide, Methane and Nitrogen on Binderless Zeolite 4A Adsorbents. *Microporous Mesoporous Mater.* **2019**, *277*, 105–114.

(31) Ruthven, D. M. *Principles of Adsorption and Adsorption Processes*; 1st ed.; John Wiley & Sons: New York, 1984.

(32) Stamires, D. N. Properties of the Zeolite, Faujasite, Substitutional Series: A Review with New Data. *Clays Clay Miner.* **1973**, *21*, 379–389.

(33) Barrer, R. M.; Gibbons, R. M. Zeolitic Carbon Dioxide: Energetics and Equilibria in Relation to Exchangeable Cations in Faujasite. *Trans. Faraday Soc.* **1965**, *61*, 948.

(34) Walton, K. S.; Abney, M. B.; Douglas LeVan, M. CO<sub>2</sub> Adsorption in Y and X Zeolites Modified by Alkali Metal Cation Exchange. *Microporous Mesoporous Mater.* **2006**, *91*, 78–84.

(35) Pirngruber, G. D.; Raybaud, P.; Belmabkhout, Y.; Čejka, J.; Zúkal, A. The Role of the Extra-Framework Cations in the Adsorption of CO<sub>2</sub> on Faujasite Y. *Phys. Chem. Chem. Phys.* **2010**, *12*, 13534.

(36) Bonenfant, D.; Kharoune, M.; Niquette, P.; Mimeault, M.; Hausler, R. Advances in Principal Factors Influencing Carbon Dioxide Adsorption on Zeolites. *Sci. Technol. Adv. Mater.* **2008**, *9*, No. 013007.

(37) Khvoshchev, S. S.; Zverev, A. V. Calorimetric Study of NH<sub>3</sub> and CO<sub>2</sub> Adsorption on Synthetic Faujasites with Ca<sup>2+</sup>, Mg<sup>2+</sup>, and La<sup>3+</sup> Cations. *J. Colloid Interface Sci.* **1991**, *144*, 571–578.

(38) Shah, D. B.; Ruthven, D. M. Measurement of Zeolitic Diffusivities and Equilibrium Isotherms by Chromatography. *AIChE J.* **1977**, *23*, 804–809.

(39) Ruthven, D. M.; Kumar, R. A Chromatographic Study of the Diffusion of N<sub>2</sub>, CH<sub>4</sub> and Binary CH<sub>4</sub>-N<sub>2</sub> Mixtures in 4A Molecular Sieve. *Can. J. Chem. Eng.* **1979**, *57*, 342–348.

(40) Gleichmann, K.; Unger, B.; Brandt, A. Industrial Zeolite Molecular Sieves. In *Intech*; 2016; Vol. i, p 13.

(41) Zafaneli, L. F. A. S.; Henrique, A.; Karimi, M.; Rodrigues, A. E.; Silva, J. A. C. Single- and Multicomponent Fixed Bed Adsorption of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> in Binder-Free Beads of 4A Zeolite. *Ind. Eng. Chem. Res.* **2020**, *59*, 13724–13734.

(42) Schumann, K.; Brandt, A.; Unger, B.; Scheffler, F. Bindemittelfreie Zeolithische Molekularsiebe Der Typen LTA Und FAU. *Chem. Ing. Tech.* **2011**, *83*, 2237–2243.

(43) Do, D. D. Series on Chemical Engineering. *Adsorption Analysis: Equilibria and Kinetics*; Imperial College Press, 1998, Vol. 2.

(44) Hammed, B. H.; Foo, K. Y. Insights into the Modeling of Adsorption Isotherm Systems. *Elsevier* **2010**, *8*, 2–10.

(45) Barrer, R. M. *Zeolites and Clay Minerals as Sorbents and Molecular Sieves, VII*; Academic Press: London, 1978.

(46) Henrique, A.; Karimi, M.; Silva, J. A. C.; Rodrigues, A. E. Analyses of Adsorption Behavior of CO<sub>2</sub>, CH<sub>4</sub>, and N<sub>2</sub> on Different Types of BETA Zeolites. *Chem. Eng. Technol.* **2019**, *42*, 327–342.

(47) Harlick, P. J. E.; Tezel, F. H. An Experimental Adsorbent Screening Study for CO<sub>2</sub> Removal from N<sub>2</sub>. *Microporous Mesoporous Mater.* **2004**, *76*, 71–79.

(48) Rajagopalan, A. K.; Avila, A. M.; Rajendran, A. Do Adsorbent Screening Metrics Predict Process Performance? A Process Optimisation Based Study for Post-Combustion Capture of CO<sub>2</sub>. *Int. J. Greenhouse. Gas Control* **2016**, *46*, 76–85.

(49) Zhao, Q.; Wu, F.; Men, Y.; Fang, X.; Zhao, J.; Xiao, P.; Webley, P. A.; Grande, C. A. CO<sub>2</sub> Capture Using a Novel Hybrid Monolith (H-ZSM5/Activated Carbon) as Adsorbent by Combined Vacuum and Electric Swing Adsorption (VESA). *Chem. Eng. J.* **2019**, *358*, 707–717.

(50) Mays, T. J. A New Classification of Pore Sizes. In *Studies in Surface Science and Catalysis*; Elsevier Inc., 2007; Vol. 160, pp. 57–62.

(51) Schumann, K.; Unger, B.; Brandt, A.; Scheffler, F. Investigation on the Pore Structure of Binderless Zeolite 13X Shapes. *Microporous Mesoporous Mater.* **2012**, *154*, 119–123.

(52) Ritter, J. A.; Bumiller, K. C.; Tynan, K. J.; Ebner, A. D. On the Use of the Dual Process Langmuir Model for Binary Gas Mixture Components That Exhibit Single Process or Linear Isotherms. *Adsorption* **2019**, *25*, 1511–1523.

(53) Tynan, K. J.; Tosso, S.; Ebner, A. D.; Ritter, J. A. On the Use of Single, Dual and Three Process Langmuir Models for Binary Gas

Mixtures That Exhibit Unique Combinations of These Processes. *Adsorption* **2021**, *27*, 637–658.

(54) Hefti, M.; Marx, D.; Joss, L.; Mazzotti, M. Adsorption Equilibrium of Binary Mixtures of Carbon Dioxide and Nitrogen on Zeolites ZSM-5 and 13X. *Microporous Mesoporous Mater.* **2015**, *215*, 215–228.

(55) Helfferich, F.; Klein, G. *Multicomponent Chromatography: Theory of Interference*. Marcel Dekker New York, USA 1970.

(56) Henrique, A.; Rodrigues, A. E.; Silva, J. A. C. Separation of Hexane Isomers in ZIF-8 by Fixed Bed Adsorption. *Ind. Eng. Chem. Res.* **2019**, *58*, 378–394.

(57) Glueckauf, E. Theory of Chromatography. *J. Chromatogr. Libr.* **1955**, *51*, A1–A68.

(58) Streb, A.; Mazzotti, M. Adsorption for Efficient Low Carbon Hydrogen Production: Part 1—Adsorption Equilibrium and Break-through Studies for H<sub>2</sub>/CO<sub>2</sub>/CH<sub>4</sub> on Zeolite 13X. *Adsorption* **2021**, *27*, 541–558.

(59) Déroche, I.; Maurin, G.; Borah, B. J.; Yashonath, S.; Jobic, H. Diffusion of Pure CH<sub>4</sub> and Its Binary Mixture with CO<sub>2</sub> in Faujasite NaY: A Combination of Neutron Scattering Experiments and Molecular Dynamics Simulations. *J. Phys. Chem. C* **2010**, *114*, 5027–5034.

(60) Plant, D.; Jobic, H.; Llewellyn, P.; Maurin, G. CO<sub>2</sub> Diffusivity in LiY and NaY Faujasite Systems: A Combination of Molecular Dynamics Simulations and Quasi-Elastic Neutron Scattering Experiments. *Adsorption* **2007**, *13*, 209–214.

(61) Onyestyák, G.; Rees, L. V. C. Frequency Response Study of Adsorbate Mobilities of Different Character in Various Commercial Adsorbents. *J. Phys. Chem. B* **1999**, *103*, 7469–7479.

(62) Roberts, C. Molecular Sieves for Industrial Separation and Adsorption Applications. *The Properties and Applications of Zeolites*; 1980, *33*, 103.