Keywords: Population based Incremental Learning, Multi-Population Evolutionary Algorithms, FPGA.

Abstract: Evolutionary-based algorithms play an important role in finding solutions to many problems that are not solved by classical methods, and particularly so for those cases where solutions lie within extreme non-convex multidimensional spaces. The intrinsic parallel structure of evolutionary algorithms are amenable to the simultaneous testing of multiple solutions; this has proved essential to the circumvention of local optima, and such robustness comes with high computational overhead, though custom digital processor use may reduce this cost. This paper presents a new implementation of an old, and almost forgotten, evolutionary algorithm: the population-based incremental learning method. We show that the structure of this algorithm is well suited to implementation within programmable logic, as compared with contemporary genetic algorithms. Further, the inherent concurrency of our FPGA implementation facilitates the integration and testing of micro-populations.

1 INTRODUCTION

Frequently the population-based incremental learning (PBIL) algorithm is defined as a method that combines both the genetic algorithms paradigm and competitive learning for function optimization. It was devised in the ends of the nineties by S. Baluja as a way to circumvent the lack of performance of conventional genetic algorithms in some particular optimization problems (Baluja, 1994).

Unlike genetic algorithms, PBIL does not handle an entire population of potential problem solutions. Rather, it only manipulates a single point around which all the next population elements will be sampled from. This concept was borrowed from the competitive learning paradigm (Rumelhart and Zipser, 1986; Duda et al., 2001; Budura et al., 2006) leading to the introduction of a probability vector. During each running epoch, the probability vector is disturbed toward the best current solution with a strength that depends on the value of a parameter denoted by learning rate. In (Folly and Venayagamoorthy, 2009) the effect of the learning rate on PBIL performance was evaluated within a power system controller design framework. The authors describe that, for high learning rate values, the population diversity is lost. On the other hand, for low learning rate values, the algorithm exploration ability is enhanced leading to a more diversified population.

The PBIL algorithm was initially devised to work with a base-2 solution encoding scheme. However, this is not an absolute condition. Multiple base versions of PBIL have already been devised by (Servais et al., 1997). This approach can lead to an increase solution resolution without incrementing the encoding dimension.

Meta-heuristics algorithms have been applied to dynamic optimization problems (Yang et al., 2007; Nguyen et al., 2012). The key issue in dealing with this type of problems is the ability to maintain the population adaptability. In (Yang and Yao, 2003) a dual population PBIL algorithm was devised. This approach operates on two dual probability vectors regarding the search space central point, in order to maintain the optimum traceability.

One of the main problems in meta-heuristics search algorithms concerns the duality between exploration and exploitation. Given a sufficient number of generations, the typical population becomes biased toward the best search space point (Gonzalez et al., 2001); the algorithm is restricted to searching a narrow region of the space. Even if other strategies are
available, one of the promising techniques requires the parallel evolution, on the same search space, of two or more PBIL algorithms. For example (Folly, 2013) provides some results regarding the use of dual population PBIL for power system controller design. Each population evolves independently. However, the number of solutions sampled from each probability vector is variable and depends on the relative fitness of the best solution found by each population.

The exact nature of this approach claims to be implemented in a dedicated digital processor. In particular within an architecture that allows the execution of true parallel processes as in multi-core processors. Since, in practice, time is a severe handicap associated to all the evolutionary algorithms, the digital processor should exchange computation versatility by computation efficiency and scalability. For this reason, a custom designed processor, based on example for a field programmable gate array (FPGA) architecture, is the obvious choice. On one hand it takes advantage of its combinatory power for fast execution and, on the other hand, it provides the ability to simultaneously run an arbitrary number of PBIL instances.

Hardware implementation of evolutionary algorithms, based on the genetic algorithm paradigm, has already been performed by several authors. Beginning with the work of (Scott et al., 1995) in the middle of the nineties, where a general purpose genetic algorithm was implemented using a decentralized topology. They reported an average time saving, during the search procedure, of 94% when compared with its software implementation. Since the publication of this seminal work, many others have followed. For example (Tommiska and Vuori, 1996), (Tang and Yip, 2004), (Fernando et al., 2010) and (Spina, 2010) just to name a few. However, as far as the authors have knowledge, the hardware implementation of PBIL has never been attempted. Some hardware implementation advantages of PBIL over genetic algorithms can be enumerated. Namely the fact that PBIL leads to a lower computation overhead since it is conceptually simpler and, due to the fact that only the best element of the population is used, the required memory resources are more parsimony leading to the possibility of evolving many more populations simultaneously.

In this line of thoughts, this work presents the results concerning a hardware implementation of both single population and multi-population PBIL. This approach will be compared to an equivalent software implementation using a high level programming language having the checkerboard problem as a benchmark (Garibay et al., 2003).

The remainder of this work is organized as follows. Section 2 describes the PBIL algorithm, its features and how it can be extended to encompass a multi-population framework. Section 3 deals with some issues regarding its hardware implementation. The testbench problem is provided in section 4 together with the obtained experimental results. Finally, the main conclusions, and future research directions, are presented in section 5.

2 THE PBIL ALGORITHM

The population-based incremental learning is a probabilistic search technique which combines notions of both evolutionary simulation and competitive learning (Baluja, 1994). Conceptually it belongs to a class of stochastic search methods generally referred as "estimation of distribution" algorithms (Larranaga and Lozano, 2002; Pelikan et al., 2002; Hauschild and Pelikan, 2011). Transversal to this class of methods is the concept of probabilistic modelling of solutions. In PBIL this approach is carried out by means of a data structure denoted by probability vector. The probability vector is expressed as a real-valued vector whose elements are in the range between 0.0 and 1.0. The probability vector plays a central role in the operation dynamics of PBIL. As a matter of fact, and unlike many evolutionary algorithms, there is no manipulation of individuals using operators such as crossover. There is no individuals update from one generation to another. All the operations are done in the probability vector entity. Hence one can argue that the PBIL conceptual approach leads to a simpler algorithm to implement, when comparing to other meta-heuristic search methods. This fact translates to a more parsimony use of computational resources such as memory and algebraic operations.

On its canonical form, the PBIL algorithm consists on two primitives: update and adjustment of the probability vector. The update primitive is responsible for the learning step and the adjustment primitive to keep the exploration ability of the algorithm.

The probability vector update law represents a disturbance on the actual probability vector toward the binary pattern of the best current solution. Let \( v_i \in [0, 1]^{n \times d} \) denote the probability vector at the current generation \( i \). The probability vector, which will be used to generate the next set of population elements, is computed by:

\[
v_{i+1} = (1 - \rho) \cdot v_i \cdot (1 - (\beta_i \oplus \omega_i)) + \cdots
+ (\rho + \mu) \cdot (\beta_i \land \omega_i) + \rho \cdot (\beta_i \land \omega_i)
\]

where \( \rho \in [0, 1] \) denotes the learning rate, \( \beta_i \in \{0, 1\}^{n \times d} \) is the best found solution at generation \( i \).
and $\omega_i \in \{0, 1\}^{n \times d}$ is the worst solution found at generation $i$. The bar over $\omega$ denotes the bitwise binary complement, $\oplus$ and $\wedge$ the “exclusive or” and “and” logical operators respectively, $I$ is a vector of ones with dimension $n \times d$ and $\mu \in [0, 1]$ is usually referred to as the negative learning rate. This negative learning rate is an additional disturbance applied to the probability vector in the direction where the bits from the best individual differ from the ones of the worst. Notice that the dot operation between two equal length vectors refers to the Hadamard product.

The learning rate parameter has a huge effect on how PBIL navigates along the search space. In general, this coefficient influences the speed with which the probability vector tends to the point that is currently being evaluated. Since in PBIL the probability vector is used to generate the next set of sample points, the learning rate affects the portions of the function space that will be explored. If the learning rate is too low, then the algorithm requires a large number of generations until its behavior deviates from random walk and becomes following a coherent direction. On the other hand, if the learning rate is too high then the initial population best individual will severely bias the rest of the search process toward the space region around it. This effect of early dominance prevents a proper search space exploration. This bias-variance trade-off can be dealt by means of an adaptive learning rate. A common choice is to select a very low learning rate at the beginning of the search process and then increasing it linearly toward some maximum value (Folly and Venayagamoorthy, 2009).

The PBIL algorithm also faces the problem of premature convergence. As the probabilities become closer to their bounds, the lack of diversity becomes gradually more pronounced. One way to prevent this occurrence comprises the definition of a probability vector adjustment operation. This operation is equivalent to the genetic algorithms mutation operator. However, unlike genetic algorithms, it is usually applied on the probability vector and not in the individuals. In PBIL this mutation, or adjustment operation, takes the appearance of a disturbance on each probability vector element.

Let $\zeta_{ij}$ be a vector with dimension $n \times d$, in GF(2), and whose $j^{th}$ element is 1 if, and only if, an uniform generated random number between [0, 1] is lower than a threshold value, $\eta \in [0, 1]$, designated by mutation probability. In this context, the probability vector adjustment operation is governed according to:

$$v_{i+1} = (1 - \delta \cdot \zeta_{ij}) \cdot v_i + \delta \cdot \zeta_{ij} \cdot \epsilon_i$$

(2)

where the parameter $\delta \in [0, 1]$ denotes the mutation level strength and $\epsilon_i \in \{0, 1\}^{n \times d}$ is a binary string whose elements are drawn, in each generation, from an uniform two bits random number generator. Once again $I \in \{1\}^{n \times d}$.

As usual there are no exact rules to define the best parameters. However, as a rule of thumb, it is frequent to select a learning ratio close to $\rho = 0.1$ and a negative learning ratio around $\mu = 0.07$. The mutation level is usually selected near $\delta = 0.05$. Nevertheless those values can be made adaptive and change according to some set of rules like population variance, generation progress, among others.

Before ending this section it is important to emphasize that, in normal operation, the iterative distilling of newer solutions leads to a reduction in the search engine exploration capability. This lack of diversity can be tackled by increasing the mutation probability $\eta$. However, this strategy has always the side effect of corrupting the knowledge gathered by the PBIL algorithm. In order to bypass this exploration-exploitation compromise a multiple populations strategy can be addressed. The following section presents the concept behind this type of solution and highlights its benefits when compared to the single population PBIL.

### 2.1 Multi-Population PBIL

Parallelization is a frequent word when talking about population based search methods. This notion usually refers to the fact that, conceptually, this class of algorithms evaluates a set of solutions in parallel. As a matter of fact, in the common implementation form, those solutions are evaluated sequentially within one generation time window. Nevertheless, this approach leads to a parallel search engine in contrast to the usual gradient-based techniques where only an initial point moves, according to some law, along the search space local gradient.

On the other hand parallelization can be understood in a multi-population paradigm where a number of arbitrary distinct populations evolves simultaneously. This strategy has been proved to be useful when dealing with time-dependent optimization problems (Branke et al., 2000) or as a way to ensure diversity in multi-modal search spaces (Siarry et al., 2002).

Using multiple populations, instead of a single one, presents many challenges. Specially regarding the way the information provided by the set of populations is combined. This issue is transversal to all the multi-population platforms including PBIL. The only thing that changes is the complexity on how those interprocess communications occur.

For example in (Yang and Yao, 2003) and (Folly, 2013) two different PBIL populations are generated over a dynamic search space. Each PBIL instance
has its own probability vector and the search direction is biased according to the overall relative best solution. This is accomplished by providing more sampling from the best of the two PBIL instances. If one probability vector outperforms the other, its sample size is increased by some arbitrary amount $\Delta$ while the other is reduced by the same quantity.

In this article an alternative strategy is proposed. Each PBIL instance will be described within a process and the inter-processes information sharing is defined by means of the following law:

$$v^j = (1 - \gamma) \cdot v^j + \gamma \cdot v^*$$  \hspace{0.5cm} (3)

where the index $j \in \{1, \ldots, p\}$ refers to one of the $p$ populations available from the pool and $v^*$ is the current best population probability vector. The coefficient $\gamma \in [0, 1]$ is used to define the amount of cross-population information sharing. If $\gamma = 0$, each population independently evolves. Alternatively, if $\gamma = 1$, this paradigm collapses into a single population PBIL.

Further information regarding this technique will be provided during section 4. The next section deals with details regarding the hardware implementation of both single population and multi-population PBIL.

3 HARDWARE DEVELOPMENT

This section presents the implementation details concerning the integration of the algorithm described in the previous section into a programmable logic device. This description will be divided into two subsections. The first deals with the hardware structure. In particular the FPGA development board characteristics and remaining interface hardware. The second subsection describes the overall algorithm architecture that will be programmed into the FPGA.

3.1 FPGA Development Board

The multi-population PBIL algorithm, discussed in the previous section, will be embedded into a custom hardware processor where several population instances can run in real parallel. The digital hardware processor devised was built over a FPGA manufactured by ALTERA\textsuperscript{®} Corporation. In particular we will deal with a Cyclone II (EP2C5T144C8) chip which has a core voltage of 1.2V, 4608 logic elements, 89 user input/output lines (I/O), 117 KB memory and 26 embedded 9 bits hardware (Altera, 2008). For an exhaustive information regarding this device characteristics please refer to the device datasheet or to the several booklets provided by ALTERA\textsuperscript{®} on its web site.

The development board used in this work, the EP2C5/EP2C8, is a very low cost solution that includes, besides the FPGA itself, a 50 MHz crystal oscillator, a pair of voltage regulators and a 4 MB FPGA configuration memory (EPCS4Si8). The used hardware is illustrated in Figure 1. The left image presents the overall shape of the development board used and, the right image, a full preview of the installed hardware. Additionally a 20 × 4 lines LCD display was interfaced in order to make easily observable the final simulation parameters such as the elapsed time, the best found solutions and so on.

![Figure 1: At the left, an image of the low-cost FPGA development board used in this work and, at the right, the experimental setup assembled that includes, besides the development board, a 20 × 4 lines LCD display.](image)

The FPGA is set, through a JTAG interface hardware programmer, using the Quartus II software provided by ALTERA\textsuperscript{®}. This software package follows an integrated development environment paradigm where the user accesses to a myriad of different tools from the same infrastructure. Distinct tools and languages can be used to describe the target hardware functionality. Furthermore it is possible to access, from the same software environment, a set of functions that expands from hardware analysis, synthesis, program compilation, device programming and different types of simulation capabilities. VHDL is one of the hardware description languages that the software can handle and is the one used during this work.

3.2 FPGA Multi-Population PBIL

In any evolutionary algorithm, independently of its inspiration, a number of potential solutions are evaluated, in parallel, during each generation. The search through the search space flows from those points toward new ones according to some set of rules. The difference between those rules is what make all the evolutionary algorithms flavours that exist. From genetic algorithms, early in the seventies, to krill-herd optimization passing from ant colonies, cuckoo search, fireflies, glowworms, bats, and so forth. In this context, parallelism does not refer to the ability to parallelize the evolutionary algorithm implementation. It concerns the fact that it is possible to evalu-
ate an arbitrary number of potential solutions in each generation. This is usually known as implicit parallelism. Of course this parallelism idea is, in fact, implemented sequentially in the major part of the computer languages. Additionally this type of parallelism tends to collapse since, after a sufficient number of generations, the selection pressure bias the solutions to became the same. Hence, in fact, when the population converges the algorithm has the task to evaluate a large number of very similar solutions. This lack of population diversity can be tackled by means of several strategies. For example using mutation operators or by means of fitness sharing techniques. Another more interesting technique is multi-population evolution where several populations evolve simultaneously. This paradigm can be easily implemented using programmable logic devices since, within this type of hardware, it is possible to effectively evolve, in true concurrent configuration, a set of smaller size populations. Those populations share information between them by an intelligence exchange mechanism in order to simultaneously explore the full extend of the search space while maintaining inter-population diversity. This kind of concurrent evolution of several populations is usually referred as explicit parallelism.

In the case of genetic algorithms, there have been already many attempts to implement this method into a FPGA. However, they usually involve only a single population with the aim of take advantage of the fast processing power provided by combinatorial processors (Scott et al., 1995; Tommiska and Vuori, 1996; Tang and Yip, 2004; Narayanan, 2005; Fernando et al., 2010; Spina, 2010). In this work an alternative evolutionary structure is embedded into a FPGA. However, as far as the present authors have knowledge, there was never been any attempt to implement the PBIL in hardware. This believe is even stronger given that our aim is to put forward an architecture that is able to handle several populations in parallel. In this context Figure 2 presents the overall multi-population PBIL algorithm structure embedded within the FPGA.

As shown in the figure above, each PBIL instance is executed inside a process and, in abstract, it is possible to set $p$ populations simultaneously. Each population has its own probability vector and, after fitness evaluation, its values are updated. The update is performed taking into consideration each population current best individual and the inter-population best individual. The objective of the inter-process communication module is to provide, at any time instant, the best global individual to each of the running PBIL instances. At each processing cycle, all the processes are executed and, inside each process, a $n$ population PBIL instance is embedded.

Inside the process the single population PBIL operations sequence is performed: first the $N$ population elements are generated according to the present probability vector. Then each element fitness is computed and both the best and worst elements are used in the probability vector update scheme. The probability actualization also requires the knowledge of the current best inter-population individual. This information is provided by the inter-process communication module which is, in its essence, just a shared variable.

A fundamental module, virtually in all evolutionary algorithms, is the random number generator. This block also plays a fundamental role in the PBIL algorithm activity. As a matter of fact its activity range from population generation to the mutation operation.

Even if true randomness is impossible to achieve using deterministic software rules, it is possible to generate number sequences with a very low autocorrelation index for lags higher than zero. There are several methods to obtain those kind of sequences. Some of the most popular ones are the linear feedback shift register (LFSR), the cellular automaton (CA) and the linear congruential generator (LCG). Nevertheless it seems that the choice of the random number generator method is not critical to the evolutionary algorithm performance (Meyenburg and Foster, 1999; Martin, 2002). In this work a LCG random number generator strategy with a 31 bit modulus and a multiplier equal to 2147483629 was used.

Having described the multi-population PBIL hardware architecture, the following section will deal with its use in finding a solution of a classical optimization problem commonly known as the checkerboard challenge.

4 EXPERIMENTAL RESULTS

The problem addressed in this article regards the checkerboard problem referred in (Baluja, 1994). The objective is to be able to find a solution that will
closely match the pattern of a generic checkerboard. A checkerboard is a matricial square structure, with a total of \(d\) elements, with two types of cells, “black” and “white”, arranged in an alternated colour pattern along its lines or columns.

Let the checkerboard colour cells be encoded by an one bit variable. For example “black” is associated to logical “1” and “white” to logical “0”. Each location with a ‘1’ should be surrounded, in all four directions, by a ‘0’ and vice-versa with the exceptions of the cells located at the board boundaries. Following this reasoning, the problem solution will be encoded as a \(d\) bit string. In particular, in this work, a 576 bit solution string will be assumed. This solution can be interpreted as a particular pattern for a \(24 \times 24\) checkerboard grid.

In short, the PBIL algorithm will be tested regarding its ability to generate a solution that matches the checkerboard pattern of ‘0’ and ‘1’ with the highest probability possible. To perform this operation an objective function must be devised that will be used to assign a degree of performance to a given solution. In (Baluja, 1994) this fitness is measured by counting the number of correct surrounding bits, of each bit position, for a subspace grid centred at the space checkerboard. That is, the squares lines that follow the board boundary are not taken into account on the objective function. In this work all the table cells are considered. In particular the objective function regards the product of the number of different bits between a particular solution and two different template vectors that match the two possible board distribution layouts. In order to illustrate this concept refer to Figure 3 where (a) and (b) represent the two valid board configurations for a \(8 \times 8\) cells checkerboard. As it can be easily seen, one of the boards is just a 90 degree rotation of the other. Recall that the state of each board cell is coded using one bit information. In particular a black cell is represented as ‘1’ and a white cell as ‘0’.

For the example illustrated in Figure 3 the value of \(F_a\) is equal to 39 and \(F_b\) equal to 25. Those numbers can be interpreted as the closeness between the arbitrary generated board and the two possible target patterns. The objective function that the algorithm will seek to optimize is the product of \(F_a\) by \(F_b\). This will lead to a fitness value for the board in Figure 3 (c) equal to 975. Hence the problem can be putted as to find an arbitrary board \(b\) which minimizes the objective function:

\[
F = \prod_i F_i
\]  

Notice that no constraints regarding the equilibrium between the number of white and black cells are imposed. Hence the full factorial set of the \(d\) bits strings is considered admissible.

In order to get an intuition about the problem complexity let the board \(b\) be interpreted as the \(d\) bits binary encoding of integers between 0 and \(2^d - 1\). As can be viewed, the number of possible boards combinations grows exponentially with \(d\). For now let’s assume a very small board with \(d = 4\). In this framework the objective function expressed at (5) can be represented, in a 1D plot, by Figure 4.

![Figure 4: Fitness value as a function of all the possible 16 cells combinations for a \(2 \times 2\) checkerboard.](image)

From visual inspection it is possible to observe the multimodal nature of the problem as long as the existence of two minima locations. There are no systematic paths along which the optimization algorithm could infer the optima location. In this context it is a complex problem.

Due to the FPGA true parallel processing capability, the implementation of the PBIL version, which
promotes the co-evolution of many populations simultaneously, is the current addressed methodology.

The first set of experiments will be conducted using a software approach. The PBIL algorithm, described at section 2.1, was coded within a numerical computation environment, using a high level computer language. The implemented programs were fully vectorized for speed purposes and run over an Intel® Core™ i5-3230M processor platform.

A total of 10 PBIL instances, each one evolving 10 population elements, were executed during 2500 generations using \( P = 0.01, \mu = 0.0005, \eta = 0.02 \) and \( \delta = 0.005 \). Remark that, instead of initializing the probability vectors with the constant 0.5, this data structure was loaded, for each of the 10 populations, using values taken from a normal distributed (pseudo) random number process with values in the range \([0, 1]\). With this strategy it is assured that the algorithm explores different points of the search space.

The first set of one hundred experiments was conducted assuming \( \gamma = 0 \). Each of the ten populations average fitness is presented at Figure 5.

![Figure 5: Multi-population average fitness evolution, along 2500 generations, using 100 tryouts.](image)

As can be seen, in average, all the populations have the same behavior regarding its convergence. Moreover, without cross communication between processes, neither one of the ten populations was able to converge consistently to one of the two possible global optima. Regarding the computational load it was measured an average CPU time, per run, of 7.8 seconds. After increasing the cross-population information, by incrementing \( \gamma \) from 0 to 0.1, and repeating the experiment sets, it is now possible to observe, from Figure 5, that the convergence to the global minimum is consistently achieved in contrast to the previous case. Furthermore, by increasing even more the value of \( \gamma \), it is possible to witness a faster convergence rate. To illustrate this statement, Figure 5 presents the convergence rate assuming \( \gamma = 0.8 \). The best solution is now found after less than 2000 generations in contrast with the earlier case where 2500 generations were, in average, needed to find the optima. From the obtained results it is possible to conclude that the PBIL is able to find the solution of the checkerboard problem as initially stated in (Baluja, 1994). In this paper it was shown that this was even possible by dividing a large population into smaller ones. This large population dismemberment, into lower size ones, favors its implementation in a parallel processing environment. Moreover different initial points on the surface can be explored simultaneously by providing different initial probabilities vectors to each population in the pool. It is also possible to confirm the success of the inter-population information exchange strategy devised. Filtering each of the probability vectors using the one from the best fitted population promotes a faster convergence to a global optimum. Having established that this optimization approach is an effective method to solve the checkerboard problem, the next step is to execute it on the dedicated hardware digital processor. Under this condition, the hardware based multi-population PBIL was driven under the same test conditions as the software version regarding both the number of populations, individuals per population and remain tuning parameters. As expected, in term of convergence, the obtained results were equivalent to the ones presented at Figure 5. However, by using dedicated hardware, the execution time was substantially decreased by a factor near 3. That is, similar results were obtained, at the end of 2500 generations, after only 2.8 seconds. This time reduction can be further decreased by using an higher performance FPGA’s such as the ones form the ALTERA® STRATIX family. This can lead to the possibility of using this type of optimization method in real-time applications when high dynamics are involved.

5 CONCLUSIONS

The PBIL has, at the present time, more than two decades of existence. This is a stochastic optimization method belonging to a broad class of methods known under the designation of distribution estimation algorithms. Even if this method has proven to be very effective on solving some types of problems where other meta-heuristic approaches fail, it has become gradually obscured by the proliferation of a countless new evolutionary methods such as particle swarm optimization, cuckoo search, krill heard optimization among many other methods. However, neither of them has reached, in the present authors opinion, the degree of simplicity and fluidity of PBIL. As a matter of fact, the PBIL algorithm is conceptually simpler which leads to faster execution times when compared with the other techniques. Processing time is a very important issue when dealing with problems requiring large population evolving during extensive
generations number or when real-time solution finding must be provided. Allied to the optimization algorithm simplicity, the execution time can be narrow down by using a special designed digital processor instead of a general purpose microprocessor such as the ones that equip the common domestic personal computers. The main contributions of this work can be summarized into three main points: the demonstration that it is possible to execute, in a very efficient fashion, the PBIL algorithm using a programmable logic device; the fact that, in this case, the extension of the original single-population approach to a multi-population one is naturally extended through the instantiation of new VHDL processes; and finally that the interconnection between the populations, in a multi-population framework, can happen easily at the probability vectors level. This multi-population hardware based approach was applied to the checkerboard problem which has been proved to be a deceptive type problem for other evolutionary algorithms. Namely the genetic algorithms. The obtained results show that, not only the PBIL algorithm was able to solve the problem, but it was able to do it in a time fraction when comparing to its implementation using a pure software approach over a generic microprocessor platform.

REFERENCES


